

Software Reliability & Security Engineering

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- Demarcating, measuring, counting: definitions
- Science & engineering of reliability growth
- Those pesky residual defects
- Components & systems
- Vulnerability: special defects



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Time to go Wholistic

- We have data on different aspects of reliability to have reasonable hypotheses.
- We know limitations of the hypotheses.
- We have enough techniques & tools to start engineering.
- Accuracy **comparable or better** than established hardware reliability methods.



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Why It's Needed Now

- **Craft:** incremental intuitive refinement
- **Science:** *why* it is so
 - Observe, hypothesize, assess accuracy
- **Engineering:** *how* to get what we want
 - Approximate, integrate, evaluate
- Are we ready to engineer software reliability?
 - Reliability expectations growing fast
 - Large projects, little time
 - Quick changes in developing environments
 - Reliance on a single technique not enough
 - Pioneering work has already been done.



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Hardware Reliability: The Status

- Well known , well established methods
 - Now standard practice
 - Used by government and industrial org worldwide
- Earliest tube computers: MTTF comparable to some computation times!
- 1959-95: MIL-HDBK-217A-F, Still widely used.
 - Failure rates predicted higher by a factor of 2-4.
 - Constant failure-rate, the bathtub curve, the Arrhenius relationship have been questioned.
- Several commercial tools available.



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Hardware Reliability: The Status (2)

- Why use hardware reliability prediction?
 - Feasibility Study: initial design
 - Compare Design Alternatives: Reliability along with performance and cost
 - Find Likely Problem Spots- high contributors to the product failure rate
 - Track Reliability Improvements

Hardware vs Software Reliability

	Models	Parameters
Hardware	Past experience with similar units	Past experience with similar units
Software	Past experience* with similar units	Early: past experience with similar units Later: from the same unit

* Also suggested: from the same unit

Basic Definitions

- Defect: requires a corrective action
- Defect density: defects per 1000 non-comment source lines.
- Failure intensity: rate at which failures are encountered during execution.
- MTTF (mean time to failure): inverse of failure intensity



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Basic Definitions (2)

- Reliability
 - $R(t) = p\{\text{no failures in time } (0, t)\}$
- Transaction reliability: probability that a single transaction will be executed correctly.
- Time: may be measures in CPU time or some measure of testing effort.

Limited use in
SRE



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Why is Defect Density Important?

- Important measurement of reliability
- Often used as release criteria

Beginning Of Unit Testing	Release		
	Frequently Cited	Highly Tested	NASA
16	2.0	0.33	0.1

Static and Dynamic Modeling

- Reliability at release depends on
 - Initial number of defects (parameter)
 - Effectiveness of defect removal process (parameter)
 - Operating environment
- **Static modeling:** estimate parameters before testing begins
 - Use static data like software size etc.
- **Dynamic modeling:** estimate parameters during testing
 - Record when defects are found etc.
 - *Time or coverage* based

What factors control defect density?

- **Need to know for**
 - *static estimation of initial defect density*
 - *Find room for process improvement*
- **Static defect density models:**
 - *Additive (ex: Takahashi-Kamayachi)*
$$D=a_1f_1+a_2f_2+a_3f_3...$$
 - *Multiplicative (ex. MIL-HDBK-217, COCOMO, RADC)*
$$D=C.F_1(f_1).F_2(f_2).F_3(f_3)...$$

A Static Defect Density Model

- Li, Malaiya, Denton (93, 97)

Phase
Programming Team
Process Maturity
Structure
Requirement
Volatility
- $$D=C.F_{ph}.F_{pr}.F_m.F_s.F_{rv}$$
- *C is constant of proportionality, based on prior data.*
- *Default value of each function (submodel) is 1.*
- *Calibration based on past, similar projects*

Submodels: F_{ph} , F_{pt}

- Phase Factor F_{ph} Based on Musa, Gaffney, Piwowski et al.

At beginning of phase	Multiplier
Unit testing	4
Subsystem testing	2.5
System testing	1 (default)
Operation	0.35

- Programming Team Factor F_{pt} : Based on Takahashi, Kamayachi.
Decline by 14% per year up to seven years.

Team's average skill level	Multiplier
High	0.4
Average	1 (default)
Low	2.5



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Process Maturity Factor F_m
SRI Capability Maturity Model

- Statistical quality control (Deming's TQM, Juran, Crosby),
- Process Maturity Factor F_m : data by Jones, Keene, Motorola

Level	Feature	How many	Multiplier F_m
1.Initial	ad hoc	80%	1.5
2. Repeatable	basic management	15%	1
3. Defined	standardized	5%	0.4
4. Managed	quantitative control	4%	0.1
5. Optimizing	continuous improvement	Handful	0.05



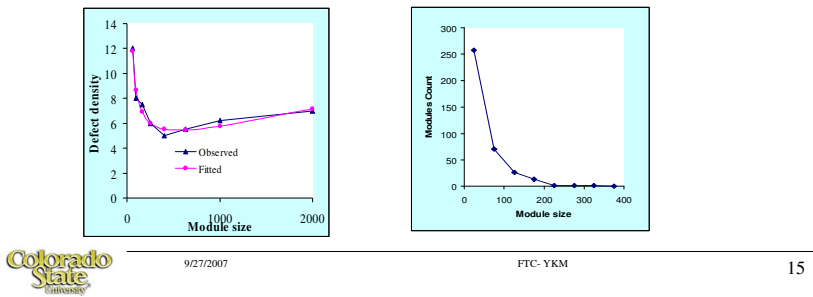
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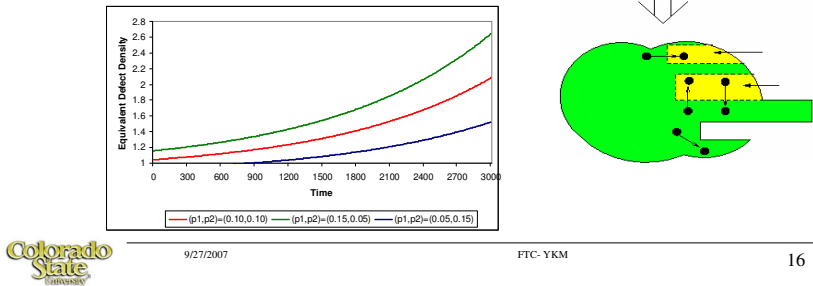
Submodel: Structure Factor F_s

- Assembly code fraction: assuming assembly has 40% more defects
 - Factor= $1+0.4\times$ fraction in assembly
- Complexity: Complex modules are more fault prone, but there may be compensating factors.
- Module size: research reported at ISSRE 2000!



Submodel: Requirement volatility Factor F_{ph}

- Degree of changes and when they occur
- Most impact when changes occur near the end of testing
- Malaiya & Denton: ISSRE 99



Using the Defect Density Model

- Calibrate submodels before use using data from a project as similar as possible.
- Constant C can range between 6-20 (Musa).
- Static models are very valuable, but high accuracy is not expected.
- Useful when dynamic test data is not yet significant.

For an organization, C is between 12 and 16. Average team and SEI maturity level is II. About 20% of code in assembly. Other factors are average (or *same as past projects*).

Estimate defect density at beginning of subsystem test phase.

•Upper estimate= $16 \times 2.5 \times 1 \times (1 + 0.4 \times 0.2) \times 1 = 43.2/\text{KSLOC}$

•Lower estimate= $12 \times 2.5 \times 1 \times (1 + 0.4 \times 0.2) \times 1 = 32.4/\text{KLOC}$



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Test methodologies

- **Static** (review, inspection) vs. **dynamic** (execution)
- **Test views**
 - Black-box (functional): input/output description
 - White box (structural): implementation used
- **Test generation**
 - Partitioning
 - Random/Antirandom/Deterministic
- **Input mix**



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Operational Profile

- **Profile:** set of disjoint actions, operations that a program may perform, and their probabilities of occurrence.
- **Operational profile:** probabilities that occur in actual operation
 - Begin-to-end operations & their probabilities
 - Markov: states & transition probabilities
- There may be multiple operational profiles.
- Accurate operational profile determination may not be needed.

A	Voice call	0.74
B	FAX call	0.15
C	New number entry	0.10
D	Data base audit	0.009
E	Add subscriber	0.0005
F	Delete subscriber	0.000499
G	Hardware failure recovery	0.000001

- "Phone follower" call types (Musa)



Input Mix: Operational Profile?

- **Need to do**
 - find bugs fast?
 - estimate operational failure intensity?
- Best mix for efficient bug finding (Li & Malaiya)
 - Quick & limited testing: *Use operational profile*
 - High reliability: *Probe input space evenly*
 - Operational profile will not execute rare and special cases
 - In general: Use combination
- For acceptance testing: Need Operational profile



Modeling Reliability Growth

- Testing cost can be 60% or more
- Careful planning to release by target date
- Decision making using a *software reliability growth model* (SRGM). Obtained using
 - Analytically using assumptions, or and
 - Based on experimental observation
- A model describes a real process approximately
- Ideally should have good predictive capability and a reasonable interpretation



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Exponential Reliability Growth Model

- We need a model to describe
 - **Undetected defects present at time t:** $N(t)$
 - **Faults detected by time t:** $\mu(t) = N_0(t) - N(t)$
 - **Failure intensity: fault detection rate** $\lambda(t)$
- **Note that**

$$\lambda(t) = \frac{d}{dt} \mu(t)$$



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Exponential SRGM (cont)

▪ Assumption: $-\frac{dN(t)}{dt} = \beta_1 N(t)$

▪ Solution: $N(t) = N(0) e^{-\beta_1 t}$

$$\mu(t) = \beta_o (1 - e^{-\beta_1 t}) \quad \lambda(t) = \beta_o \beta_1 e^{-\beta_1 t}$$

- For $t \rightarrow \infty$, total $\beta_o = N(0)$ faults would be eventually detected.
 - A “finite-faults-model”.
 - Jelinski-Muranda ‘71, Shooman ‘71, Goel-Okumoto ‘79 and Musa ‘75-’80. also called Basic



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A Basic SRGM (Cont.)

- **Parameter β_1 is given by:**

$$\beta_1 = \frac{K}{T_L} = \frac{K}{(S.Q.\frac{1}{r})}$$

- S: source instructions,
- Q: number of object instructions per source instruction,
- r: object instruction execution rate of the computer
- K: *fault-exposure ratio*, range 1×10^{-7} to 10×10^{-7} , (t is in CPU seconds). Assumed constant here.



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SRGM : “Logarithmic Poisson”

- Many SRGMs have been proposed.
- Logarithmic** model, by Musa-Okumoto, found to have a good predictive capability

$$\mu(t) = \beta_o \ln(1 + \beta_1 t) \qquad \lambda(t) = \frac{\beta_o \beta_1}{1 + \beta_1 t}$$

- Applicable as long as $\mu(t) \leq N(0)$. Practically always satisfied. Term *infinite-faults-model* misleading.
- Parameters β_o and β_1 don't have a simple interpretation. A useful interpretation by Malaiya and Denton.

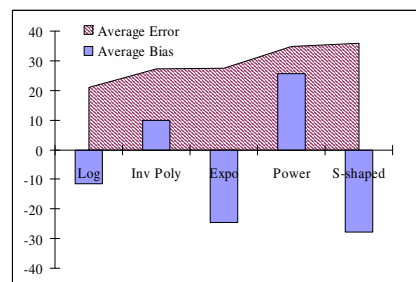
Comparing Models

- Goodness of fit: may be misleading
- Predictive capability
 - Data points: (λ_i, t_i) , $i=1$ to n
 - Total defects found: D , estimated at i : D_i

$$\text{Average error : AE} = \frac{1}{n} \sum_{i=1}^{n-1} \left| \frac{D_i - D}{D} \right|$$

$$\text{Average bias : AB} = \frac{1}{n} \sum_{i=1}^{n-1} \frac{D_i - D}{D}$$

- We used a many datasets from diverse projects for comparing different models.



SRGM: Preliminary Planning: Example

- Example:
 - initial defect density estimated 25 defects/KLOC
 - 10,000 lines of C code
 - computer 70 million object instructions per second
 - *fault exposure ratio* K estimated to be 4×10^{-7}
 - Estimate the testing time for defect density 2.5/KLOC
- Procedure:
 - $\beta_0 = 250$ defects, $\beta_1 = 11.2 \times 10^4$ per sec
 - Thus Testing time $t_1 = 2056$ sec.

Value of fault exposure ratio (K) may depend on initial defect density and testing strategy (Li, Malaiya '93).



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SRGM: During Testing

- Collect and pre-process data:
 - To extract the long-term trend, data needs to be smoothed
 - *Grouped* data: test duration intervals, average failure intensity in each interval.
- Select a model and determine parameters:
 - past experience with projects using same process
 - exponential and logarithmic models often good choices
 - model that fits early data well, may not have best predictive capability
 - parameters estimated using *least square* or *maximum likelihood*
 - parameter values used when *stable* and *reasonable* 



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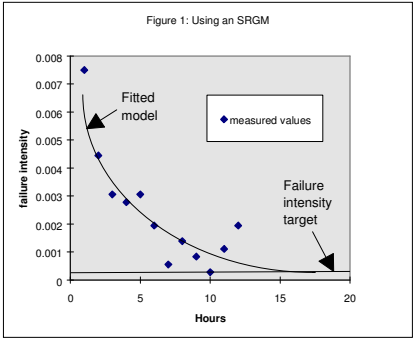
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SRGM: During Testing (cont.)

- Compute how much more testing is needed:
 - fitted model to project additional testing needed
 - desired failure intensity
 - estimated defect density
 - recalibrating a model can improve projection accuracy
 - Interval estimates can be obtained using statistical methods.

Example: SRGM with Test Data

CPU Hours	Failures
1	27
2	16
3	11
4	10
5	11
6	7
7	2
8	5
9	3
10	1
11	4
12	7



- Target failure intensity 1/hour ($2.78 \cdot 10^{-4}$ per sec.)
- $\beta_0 = 101.47$ and $\beta_1 = 5.22 \times 10^{-5}$
- Stopping time $t_f = 56,473$ sec

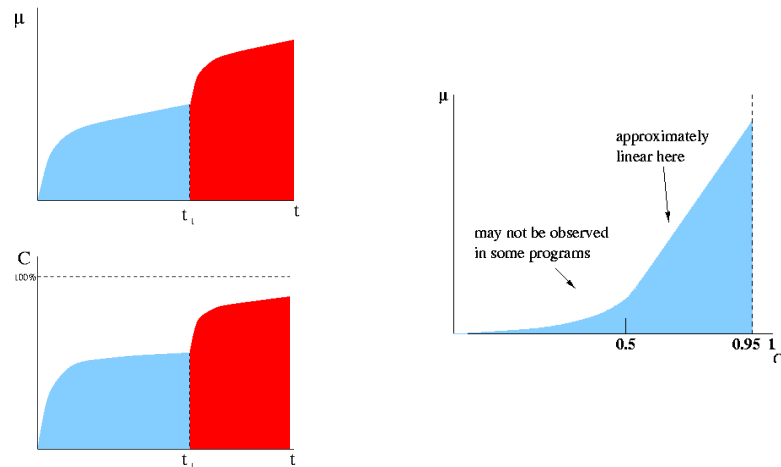
Test Coverage & Defect Density: Yes, they are related.

- Defect vs. Test Coverage model, 1994:
 - Malaiya, Li, Bieman, Karcich, Skibbe
- Estimation of number of defects, 1998
 - Li, Malaiya, Denton

Test Coverage Measures

- Statement or Block coverage
- Branch or decision coverage
- P-use coverage: p-use pair: variable defined/modified - use as predicate
- Subsumption hierarchy:
 - Covering *all branches* cover *all statements*
 - Covering *all p-uses* cover *all branches*

Modeling : Defects, Time, & Coverage



Coverage Based Defect Estimation

- Coverage is an objective measure of testing
 - Directly related to test effectiveness
 - Independent of processor speed and testing efficiency
- Lower defect density requires higher coverage to find more faults
- Once we start finding faults, expect coverage vs. defect growth to be linear

Logarithmic-Exponential Coverage Model

- Hypothesis 1: defect coverage growth follows logarithmic model

$$C^0(t) = \frac{\beta_0^0}{N^0} \ln(1 + \beta_1^0 t), \quad C^0(t) \leq 1$$

- Hypothesis 2: test coverage growth follows logarithmic model

$$C^i(t) = \frac{\beta_0^i}{N^i} \ln(1 + \beta_1^i t), \quad C^i(t) \leq 1$$



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Log-Expo Coverage Model (2)

- Eliminating t and rearranging,

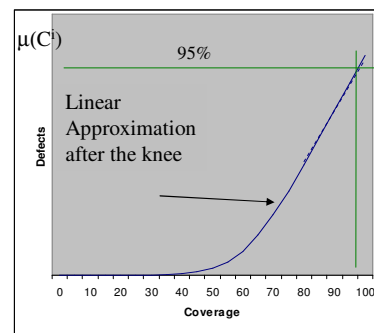
$$C^0 = a_0^i \ln[1 + a_1^i (\exp(a_2^i C^i) - 1)], \quad C^0 \leq 1$$

C^0 : defect coverage, C^i : test coverage

- For “large” $C_i \gg C_{\text{knee}}$, we can approximate

$$C^0 = -A^i + B^i C^i$$

- Assumes stable software



Location of knee based on initial defect density
Lower defect densities cause knee to occur at higher coverage
Malaiya and Denton (HASE '98)



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Data Sets Used Vouk and Pasquini

- Vouk data
 - from N version programming project to create a flight controller
 - Three data sets, 6 to 9 errors each
- Pasquini data
 - Data from European Space Agency
 - C Program with 100,000 source lines
 - 29 of 33 known faults uncovered

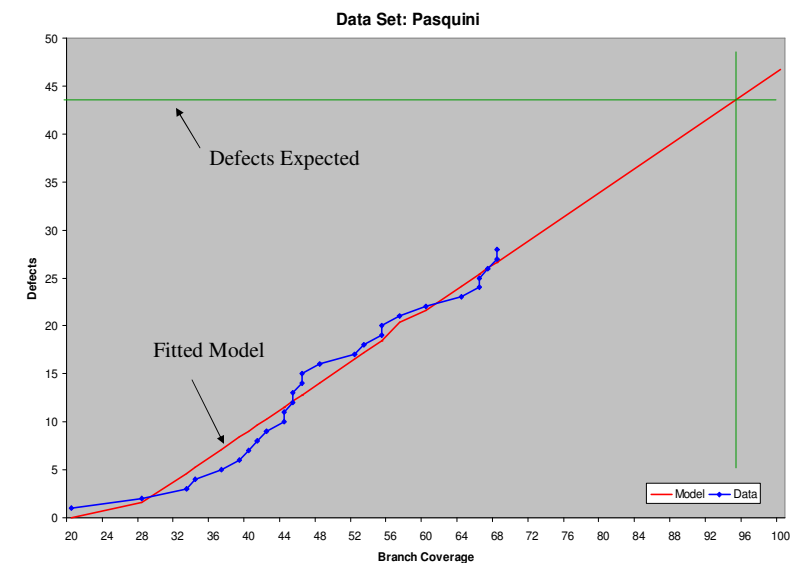


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Defects vs. Coverage



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Estimation of Defect Density

- Estimated defects at 95% coverage, for Pasquini data (assume 5% *dead code*)
- 28 faults found, and 33 known to exist

Measure	Coverage Achieved	Expected Defects
Block	82%	36
Branch	70%	44
P-uses	67%	48

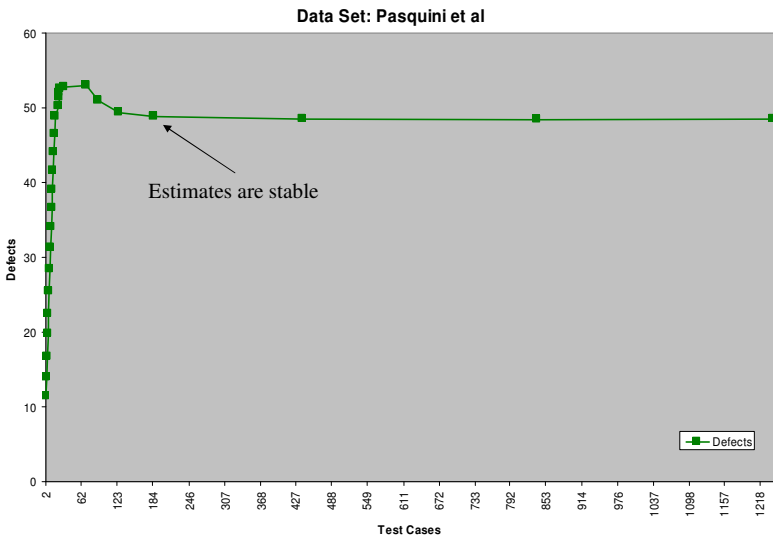


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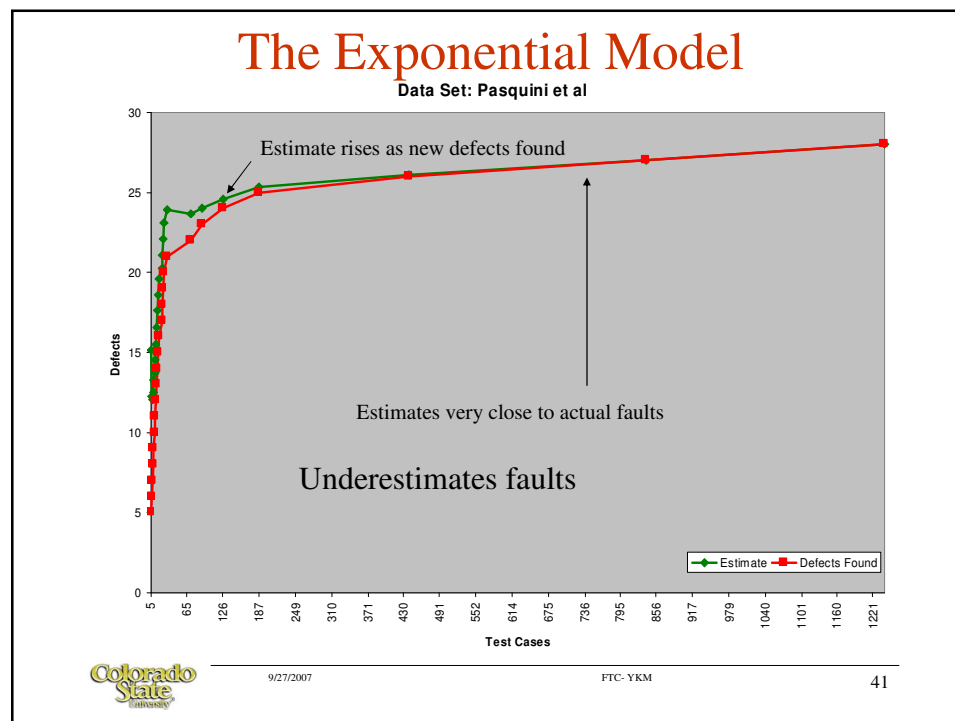
Comparison: Coverage Based Estimation



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Recent Conformation of Model

- Frankl & Iakouneno, Proc. SIGSOFT '98
 - 8 versions of European Space Agency program, 10K LOC
 - Single fault reinsertion
- Tom Williams, 1999
 - analysis from first principles