

CS220 Spring 2018 Written Homework 1: Induction

name:

id:

1. Prove using induction that the predicate $P(n): 1 \cdot 1! + 2 \cdot 2! + \dots + n \cdot n! = (n+1)! - 1$ is true for any positive integer n .

a) Show that $P(1)$ is true, completing the base of the induction.

b) What do you need to prove in the inductive step? Write out $P(k) \rightarrow P(k+1)$ for this particular case.

c) Complete the inductive step.

2a) Find a formula for $\frac{1}{1*2} + \frac{1}{2*3} + \dots + \frac{1}{n*(n+1)}$ by examining the values of this expression for small values of n.

2b) Prove the formula you found by induction. Follow the format of question 1.