

The Canny Edge Detector and the Hough Transform

CS 510

Lecture #12

February 27, 2019

Colorado State University



Before Canny - Sobel Edges



Source

Dx Image

Dy Image

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Sobel Edges: A Local Decision

- Magnitude = $(dx^2 + dy^2)^{1/2}$
- Orientation = $\tan^{-1} dy/dx$
- dy/dx responses are signed
- Edge Masks: sum of weights is zero
- Edges tend to be “thick”

Symbolic Edge Detection

- Although Sobel edges are optimal estimators for the slope of a planar facet, as symbols they:
 - Are continuous; edge yes/no based on threshold
 - May be “thick”; need to be localized
 - Are isolated; need to be grouped into longer lines
- If they correspond to scene structure (e.g. discontinuities), we want a model of how scene structures map to images.

Seminal Work – Canny Edges



The screenshot shows the Wikipedia page for the 'Canny edge detector'. The browser address bar displays 'en.wikipedia.org'. The page layout includes a left sidebar with navigation links, a main content area with the article title and text, and a right sidebar with feature detection images and links.

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Canny edge detector

From Wikipedia, the free encyclopedia

The **Canny edge detector** is an [edge detection](#) operator that uses a multi-stage [algorithm](#) to detect a wide range of edges in images. It was developed by [John F. Canny](#) in 1986. Canny also produced a *computational theory of edge detection* explaining why the technique works.

Contents [\[hide\]](#)

- 1 Development of the Canny algorithm
- 2 Process of Canny edge detection algorithm
 - 2.1 Gaussian Filter
 - 2.2 Finding the Intensity Gradient of the Image
 - 2.3 Non-maximum Suppression
 - 2.4 Double Threshold
 - 2.5 Edge Tracking by Hysteresis
- 3 Improvement on Canny Edge Detection

Feature detection



Output of a typical corner detection algorithm

Edge detection

[Canny](#) · [Canny–Deriche](#) · [Differential](#) · [Sobel](#) · [Prewitt](#) · [Roberts cross](#)

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Canny Edge Detection (Step 1)

- In order to maximize the likelihood of finding step-edges,
 1. Smooth image with a Gaussian filter
 - Size is determined by noise model
 2. Compute image gradients over the same size mask
- The bigger the mask, the better detection is but the worse localization is...

Canny Edge Detection (step 2)

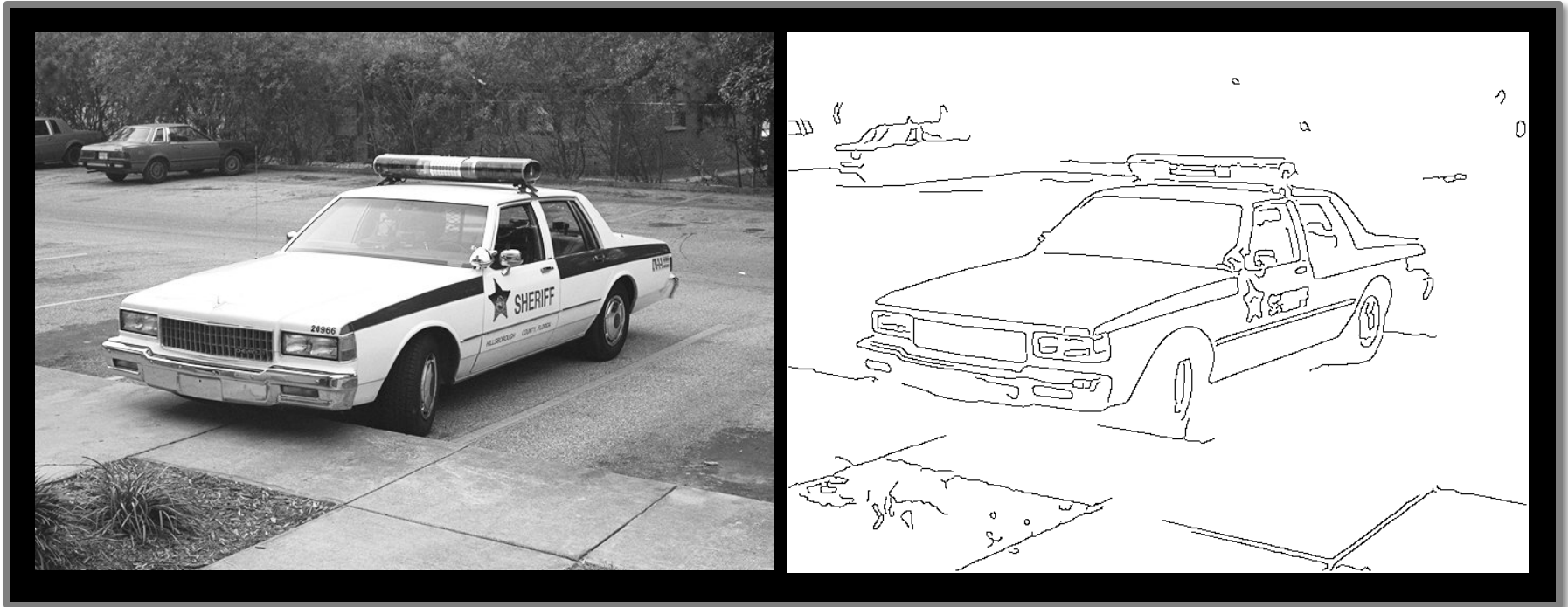
- Non-maximal suppression
 - So far, edges are still “thick”
 - For every edge pixel:
 - 1) Calculate direction of edge (gradient)
 - 2) Check neighbors in edge direction

If either neighbor is “stronger”, set edge to zero.

Canny Edge Detection (Step 3): Hysteresis Thresholding

- Continuous values still need thresholding
- Algorithm takes two thresholds: high & low
 - Any pixel with edge strength above the high threshold is an edge
 - Any pixel above the low threshold and next to an edge is an edge
- Iteratively label edges
 - they “grow out” from high points.
 - This is called hysteresis.

Canny Example

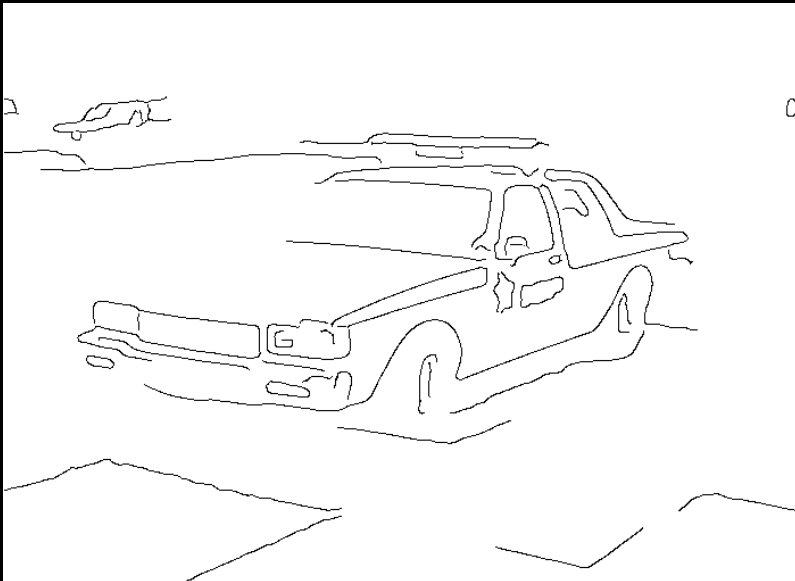


Source image

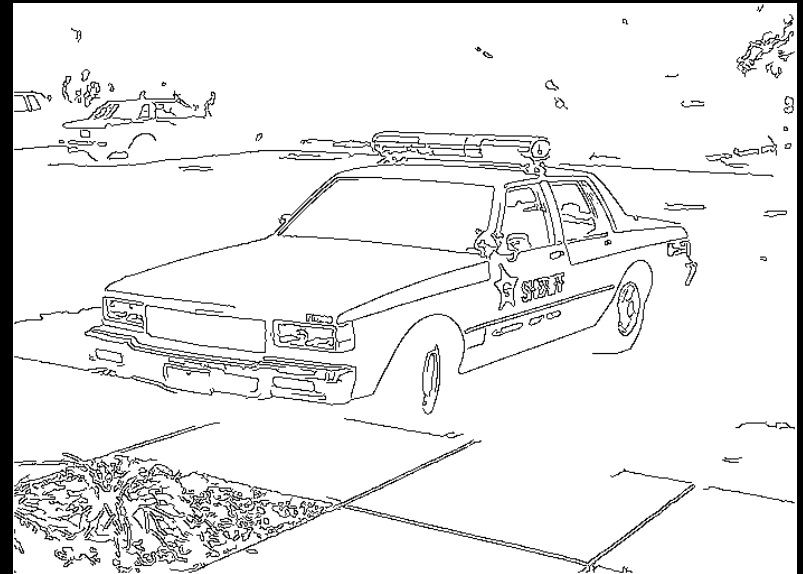
Canny: $\sigma = 2.0$,
low = 0.40, high = 0.90

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Canny Example (cont.)



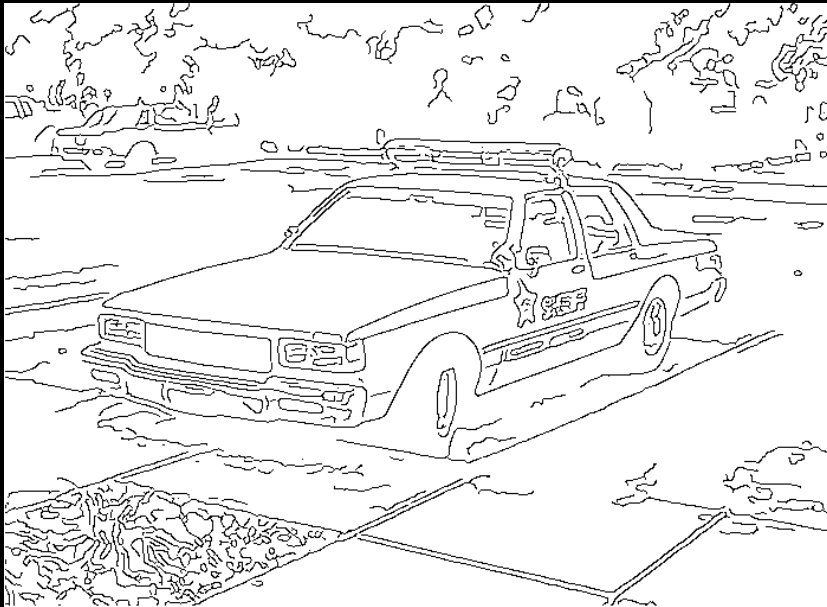
Sigma = 3.0
low = 0.4, high = 0.9



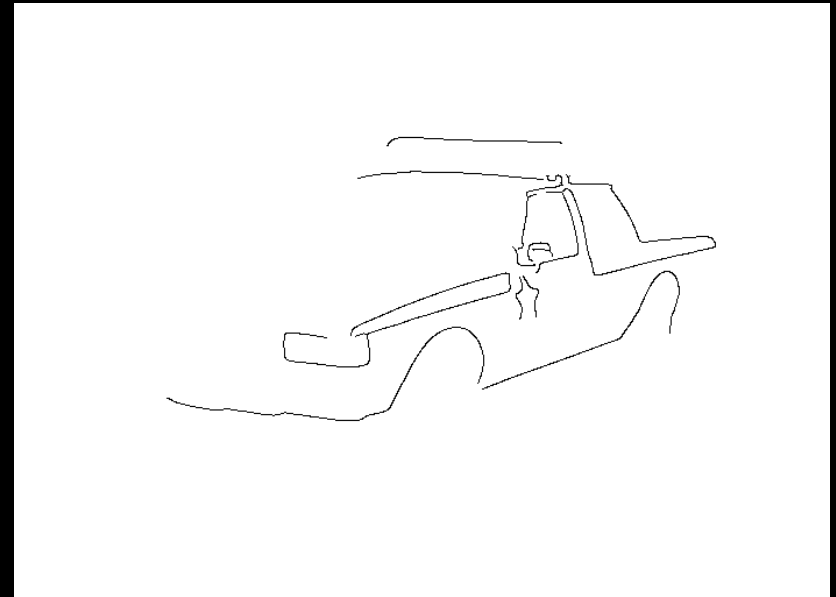
Sigma = 1.0
low = 0.4, high = 0.9

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Canny Example (III)



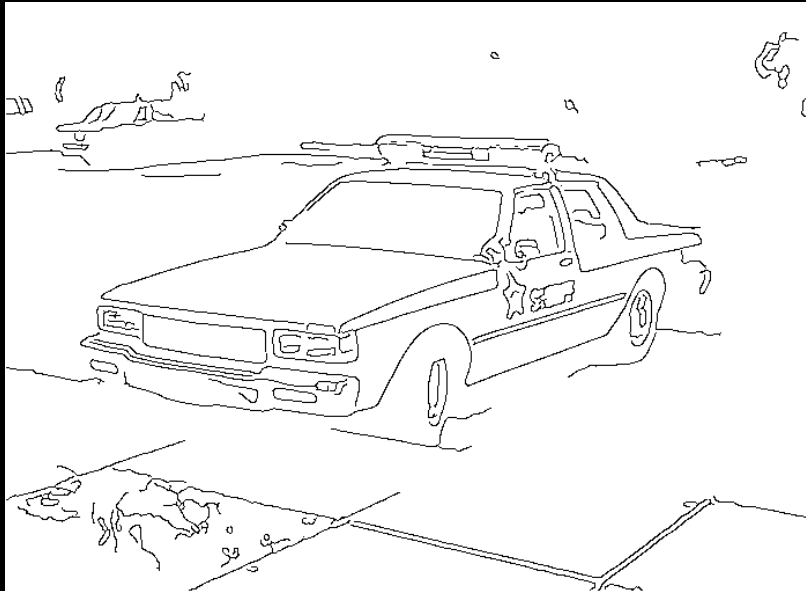
Sigma = 2.0
low = 0.4, high = 0.6



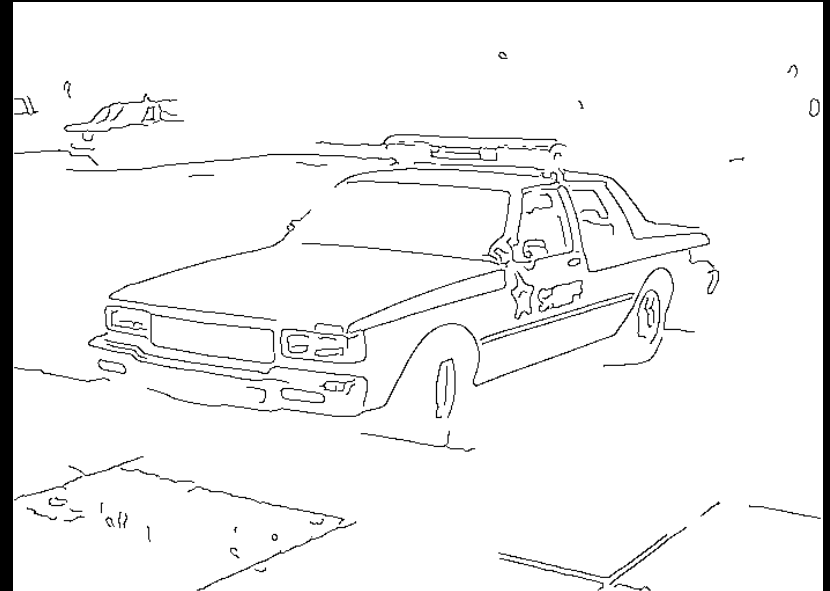
Sigma = 2.0
low = 0.4, high = 0.99

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Canny Example (IV)



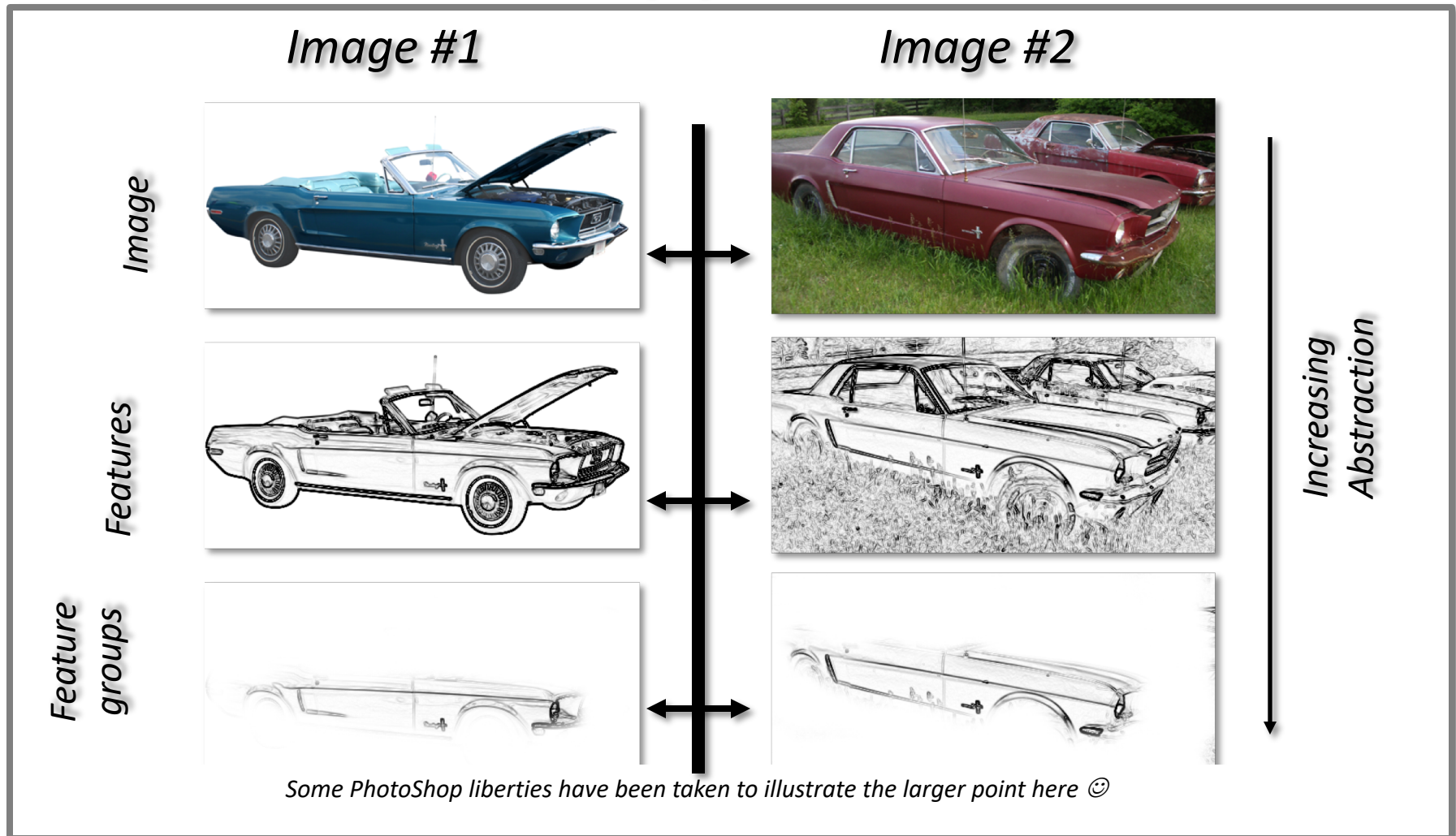
Sigma = 2.0
low = 0.2, high = 0.9



Sigma = 2.0
low = 0.6, high = 0.9

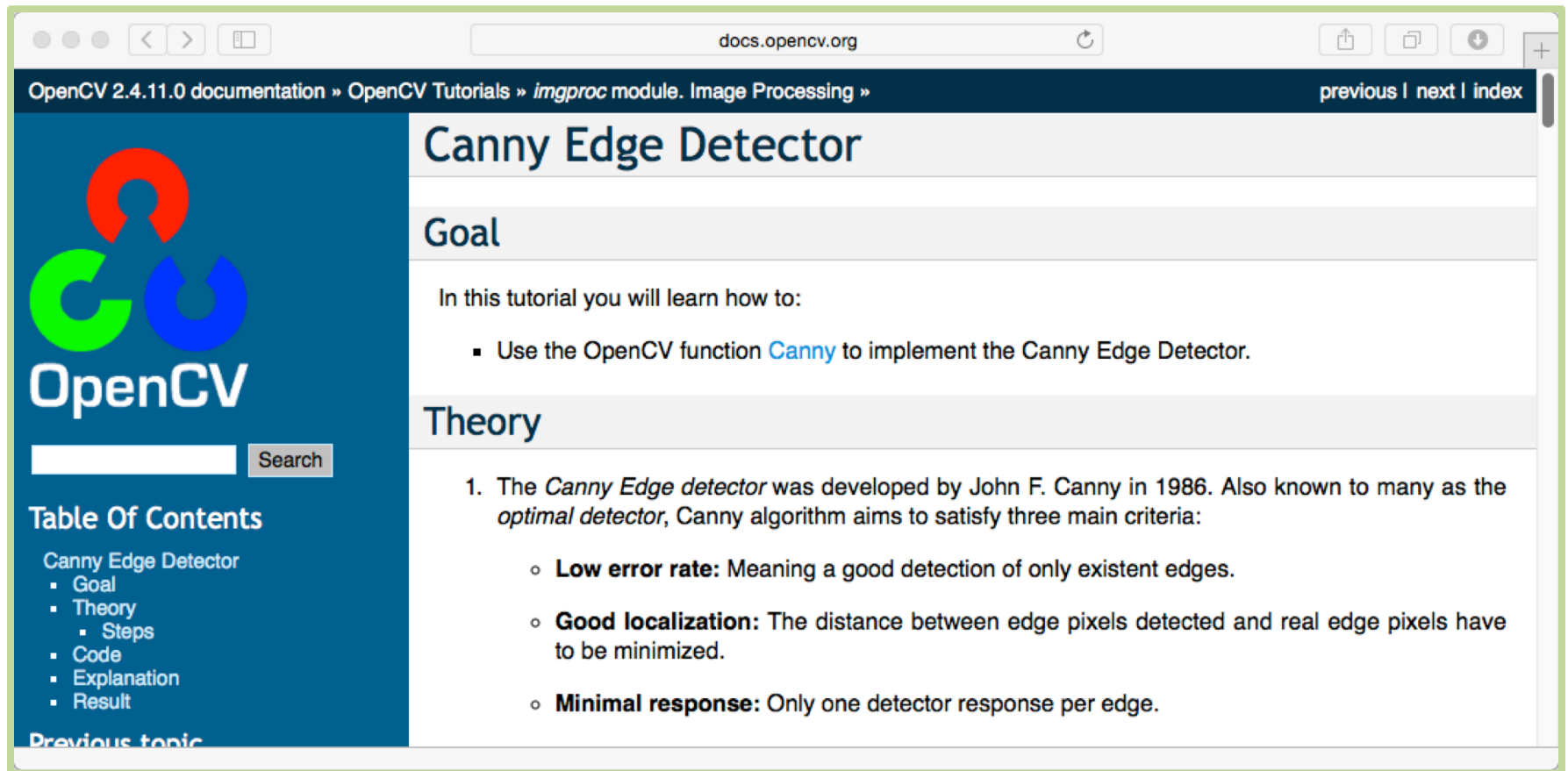
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Motivation – Apprx. Invariance



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Canny in OpenCV



The screenshot shows a web browser window with the URL `docs.opencv.org`. The page title is "OpenCV 2.4.11.0 documentation » OpenCV Tutorials » *imgproc* module. Image Processing »". The main heading is "Canny Edge Detector". Below it is a "Goal" section with the text "In this tutorial you will learn how to:" followed by a bullet point: "Use the OpenCV function `Canny` to implement the Canny Edge Detector." The "Theory" section follows, starting with "1. The *Canny Edge detector* was developed by John F. Canny in 1986. Also known to many as the *optimal detector*, Canny algorithm aims to satisfy three main criteria:" followed by three bullet points: "Low error rate: Meaning a good detection of only existent edges.", "Good localization: The distance between edge pixels detected and real edge pixels have to be minimized.", and "Minimal response: Only one detector response per edge." On the left side of the page, there is a sidebar with the OpenCV logo, a search bar, and a "Table Of Contents" section listing: "Canny Edge Detector", "Goal", "Theory", "Steps", "Code", "Explanation", and "Result".

OpenCV 2.4.11.0 documentation » OpenCV Tutorials » *imgproc* module. Image Processing »

Canny Edge Detector

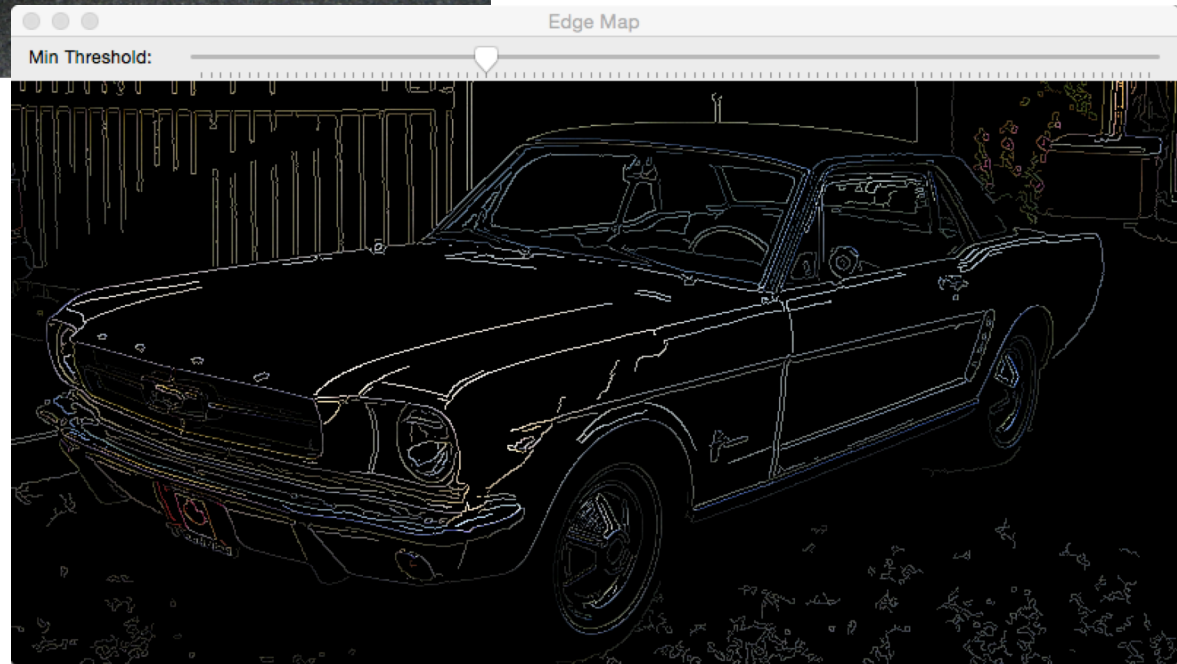
Goal

In this tutorial you will learn how to:

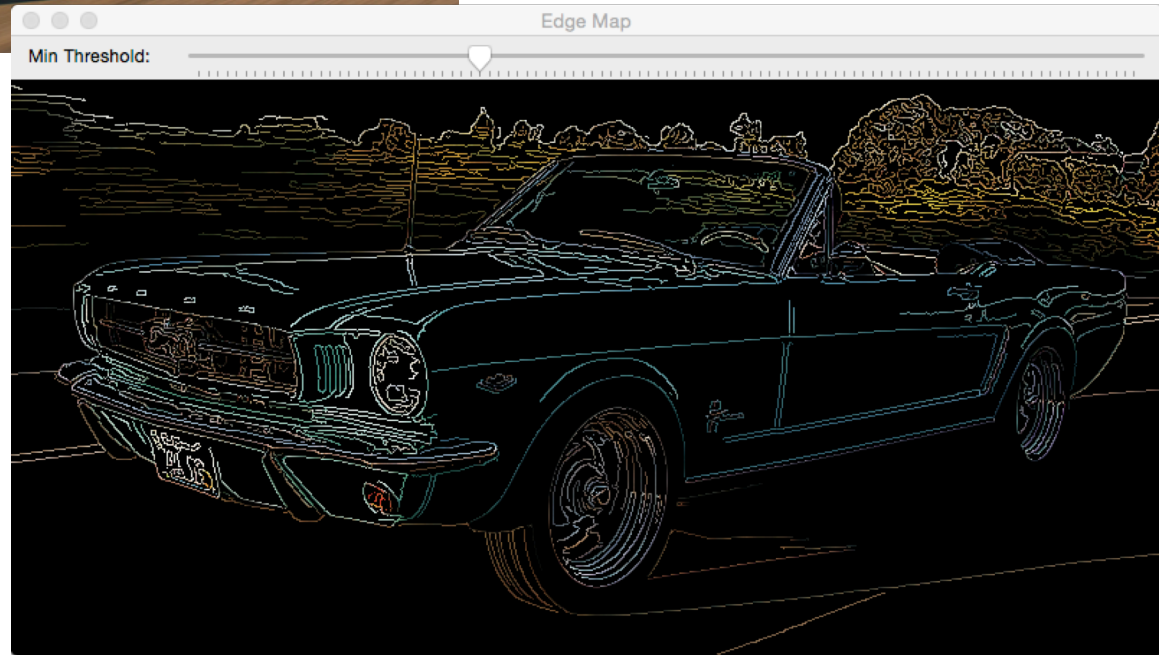
- Use the OpenCV function `Canny` to implement the Canny Edge Detector.

Theory

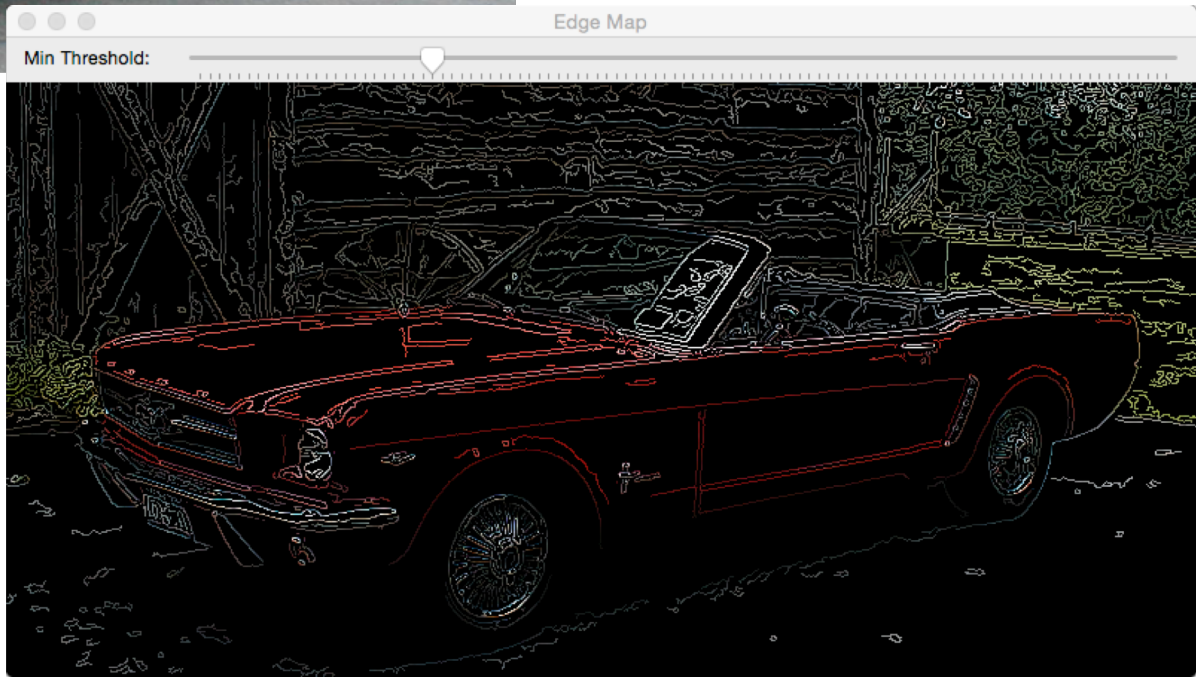
- The *Canny Edge detector* was developed by John F. Canny in 1986. Also known to many as the *optimal detector*, Canny algorithm aims to satisfy three main criteria:
 - Low error rate:** Meaning a good detection of only existent edges.
 - Good localization:** The distance between edge pixels detected and real edge pixels have to be minimized.
 - Minimal response:** Only one detector response per edge.



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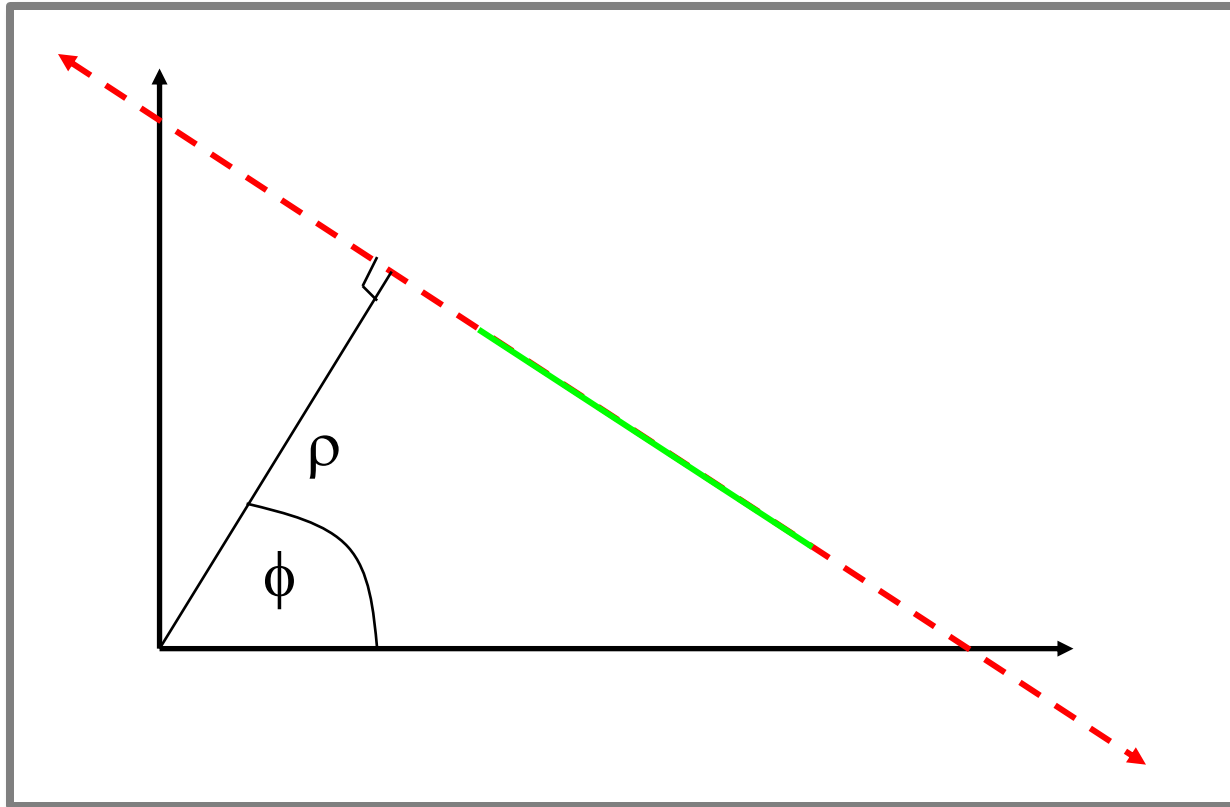
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Hough Transform: Grouping

- The idea of the Hough transform is that a change in representation converts a point grouping problem into a peak detection problem.
- Standard line representations:
 - $y = mx + b$ -- *compact, but no vertical lines*
 - $(x_0, y_0) + t(x_1, y_1)$ -- *your raytracer used this form, but it is highly redundant (4 free parameters)*
 - $ax + by + c = 0$ -- *Bresenham's uses this form. Still redundant (3 free parameters)*
- How else might you represent a line?

Hough Grouping (cont.)

- Represent infinite lines as (ϕ, ρ) :

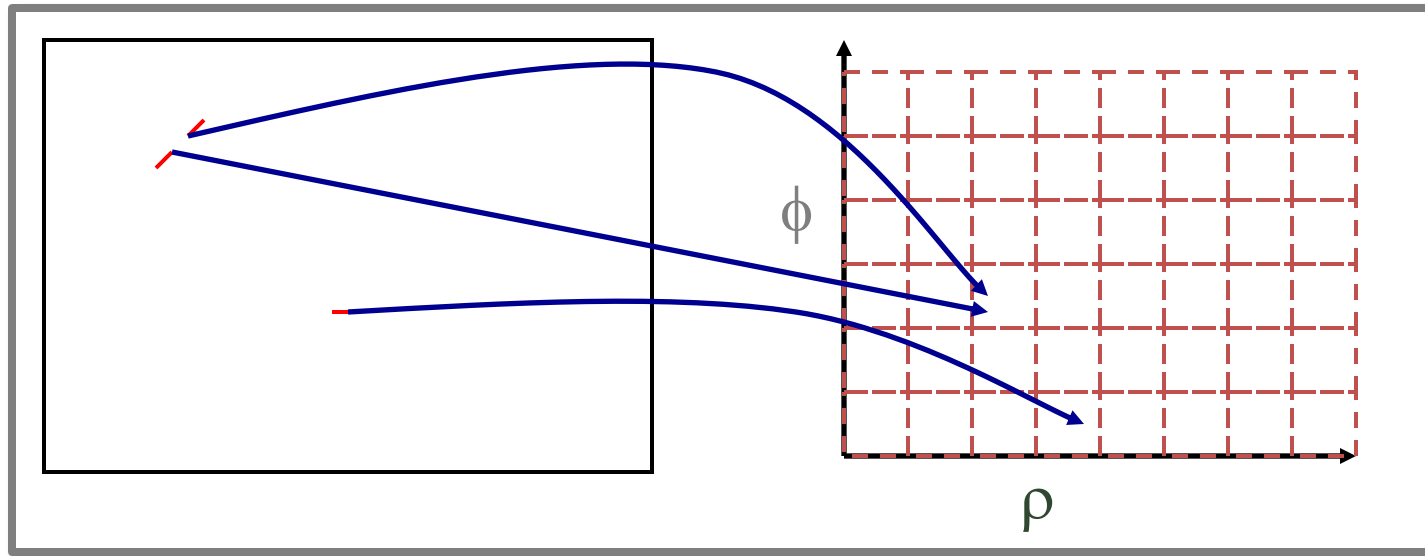


Hough Grouping (III)

- Why? This representation is:
 - Small: only two free parameters (like $y=mx+b$)
 - Finite in all parameters : $0 \leq \rho < \sqrt{\text{row}^2 + \text{col}^2}$, $0 \leq \phi < 2\pi$
 - Unique: only one representation per line
- General Idea:
 - Hough space (ϕ, ρ) represents all possible lines
 - Next step - use discrete Hough space
 - Let every point “vote for” any line it might belong to.

Hough Grouping: Directed Edges

- Every edge has a location and position, so it can be part of only one (infinitely extended) line.



- Co-linear edges map to one bucket in Hough space.

Hough Grouping: Edges

- Reduces line grouping to peak detection
 - Each edge votes for a bucket (line)
 - # of votes equates to support
 - The # of participating edges.
 - Position of bucket provides the ϕ , ρ parameters
- Problem: if “true” line parameters are on the boundary of a bucket, supporting data may be split
- Solution: smooth the histogram (Hough image) before selecting peaks.

Basic Hough – Infinite Lines

- The Hough Transform in pure form ...
- Does not return end-points
- Instead, it returns a rho and theta pairs.

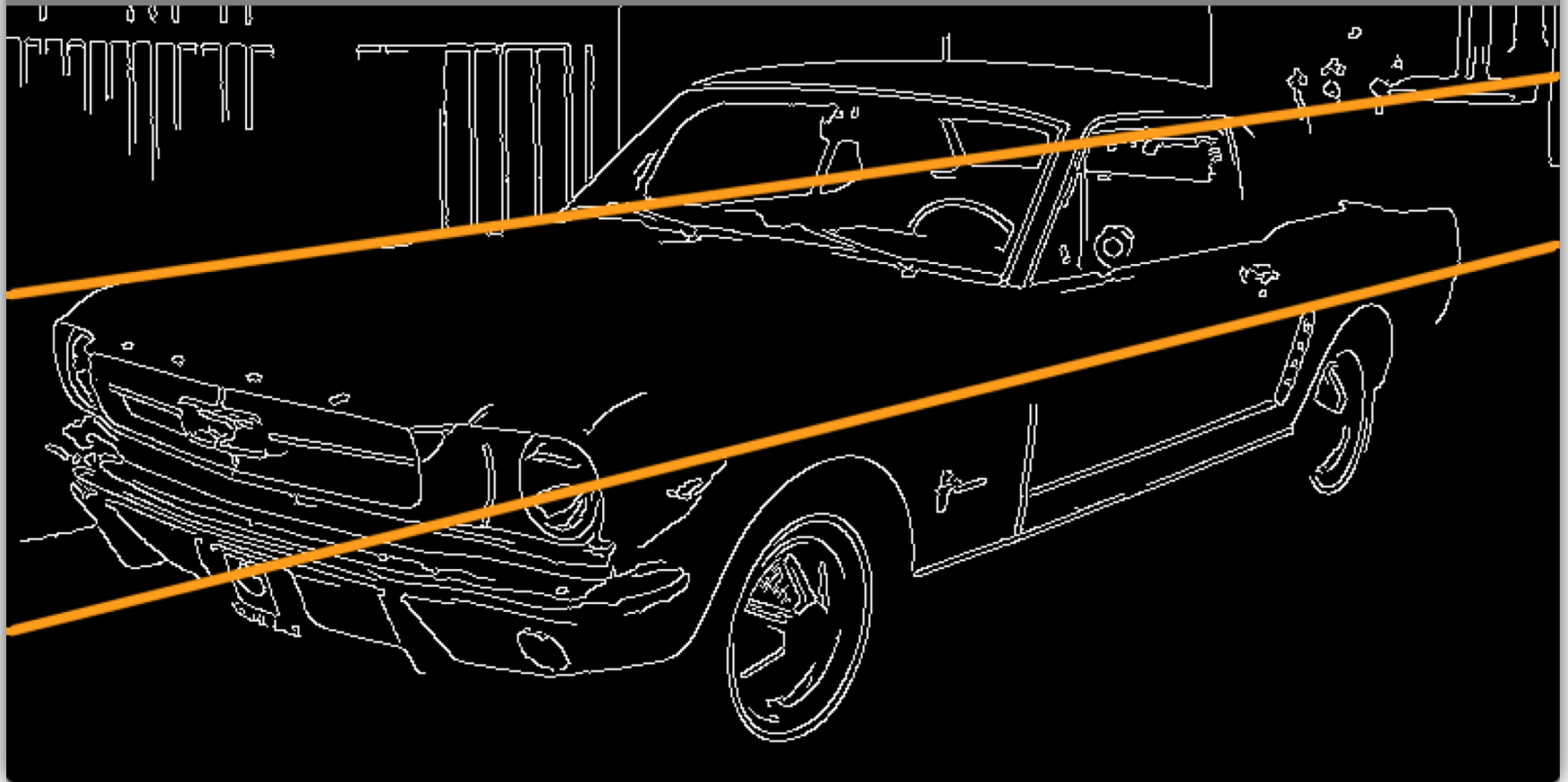
```
44     for (size_t i = 0; i < lines.size(); i++) {  
45         float rho = lines[i][0], theta = lines[i][1];  
46         Point pt1, pt2;  
47         double a = cos(theta), b = sin(theta);  
48         double x0 = a * rho, y0 = b * rho;  
49         pt1.x = cvRound(x0 + 1000 * (-b));  
50         pt1.y = cvRound(y0 + 1000 * (a));  
51         pt2.x = cvRound(x0 - 1000 * (-b));  
52         pt2.y = cvRound(y0 - 1000 * (a));
```

Open CV Hough Lines

Edge Threshold:

Vote Threshold:

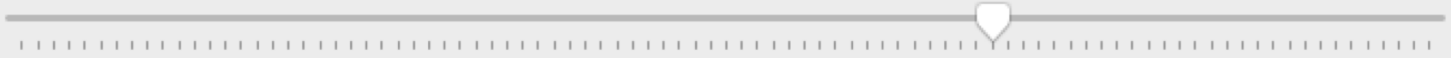
Min Edge Threshold: 71, Min Votes: 194



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Open CV Hough Lines

Edge Threshold:



Vote Threshold:



Min Edge Threshold: 72, Min Votes: 194



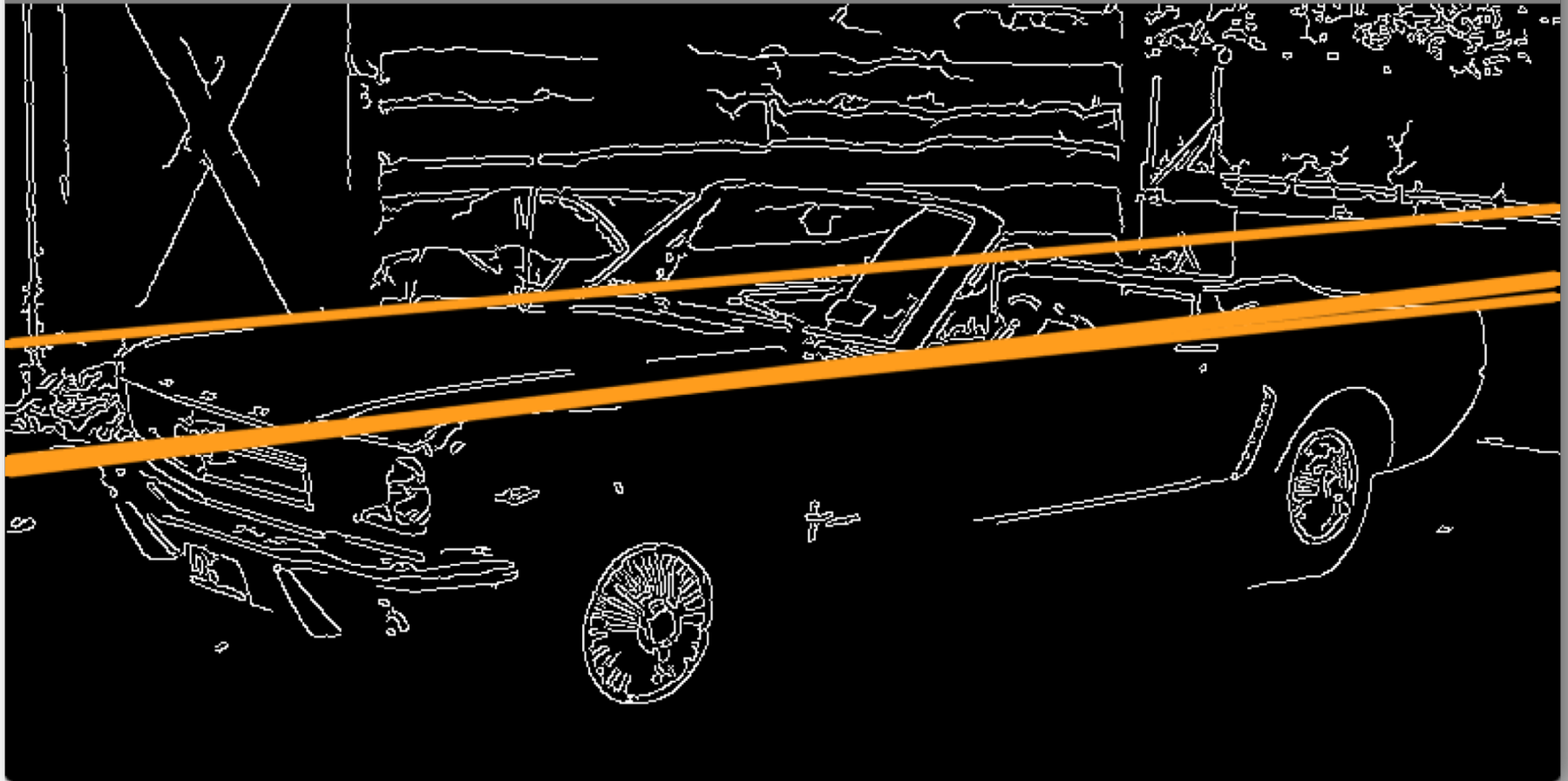
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Open CV Hough Lines

Edge Threshold:

Vote Threshold:

Min Edge Threshold: 71, Min Votes: 194



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Hough Fitting

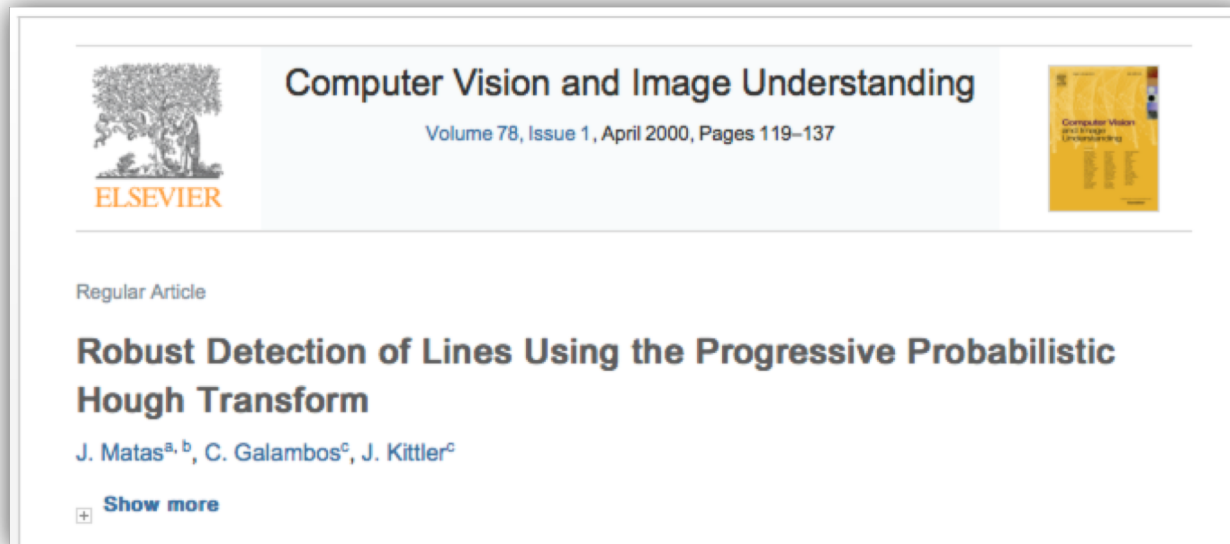
- After finding the peaks in the Hough Transform - still two potential problems:
 - Resolution limited by bucket size.
 - Infinite lines, not line segments
- Both of these problems can be fixed,
 - If you kept a linked list of edges (not just #)
 - Of course, this is more expensive...

Hough Fitting (II)

- Sort your edges
 - rotate edge points according to ρ
 - sort them by (rotated) x coordinate
- Look for gaps
 - have the user provide a “max gap” threshold
 - if two edges (in the sorted list) are more than max gap apart, break the line into segments
 - if there are enough edges in a given segment, fit a straight line to the points

Open CV Hough Version 2

- Second Hough algorithm in OpenCV
- Returns segments – based on work below

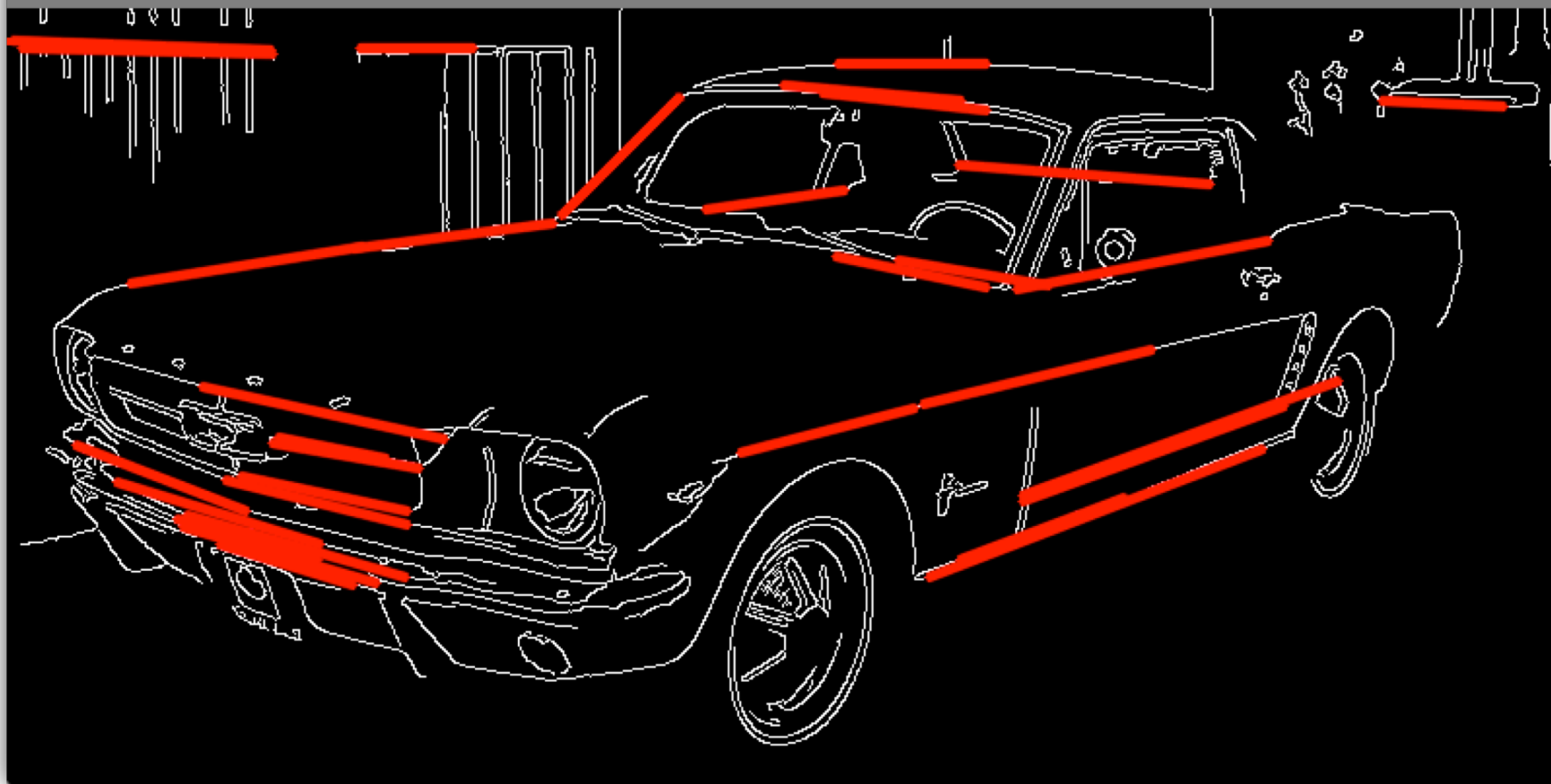


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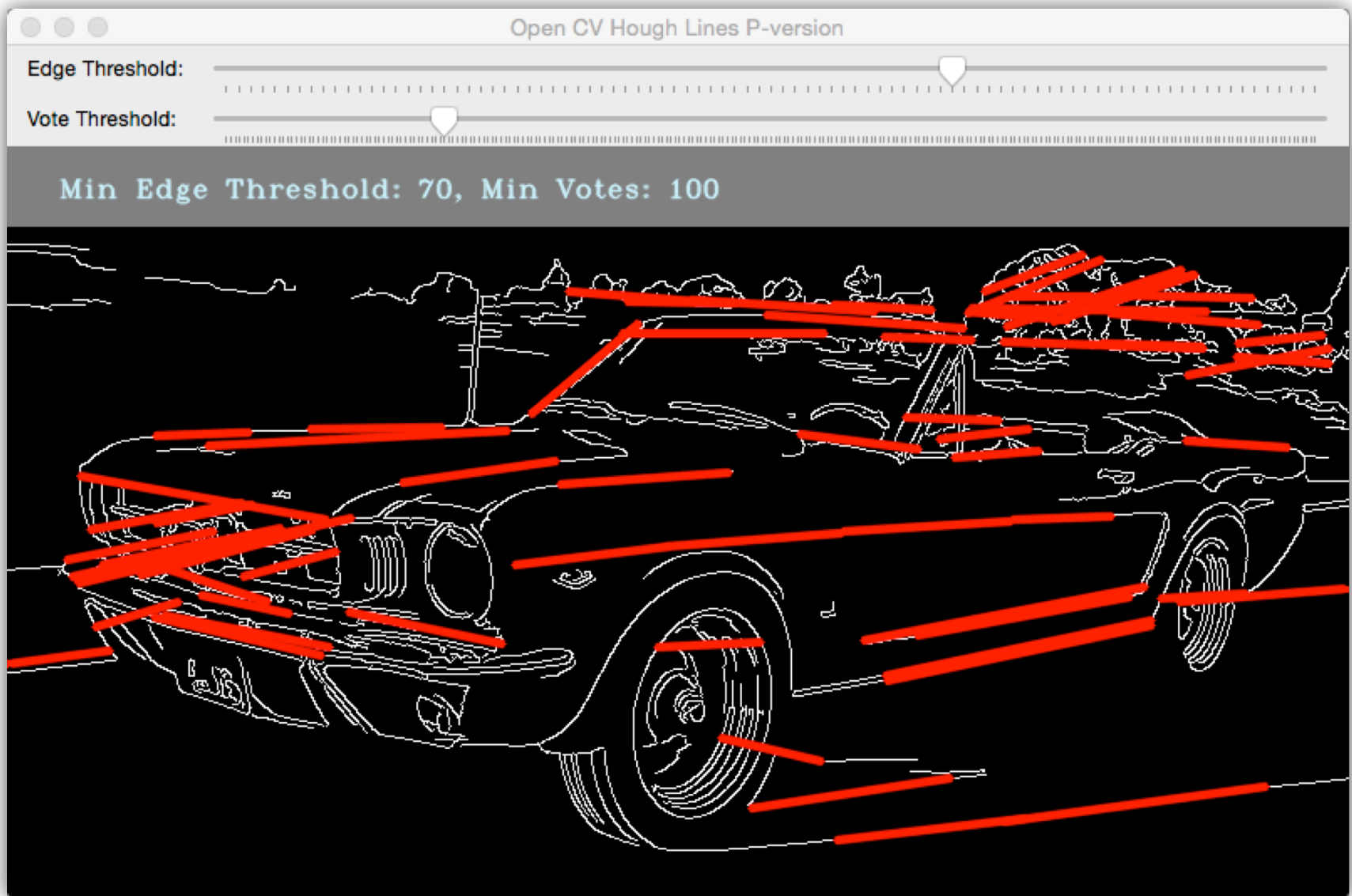
Edge Threshold:

Vote Threshold:

Min Edge Threshold: 70, Min Votes: 100



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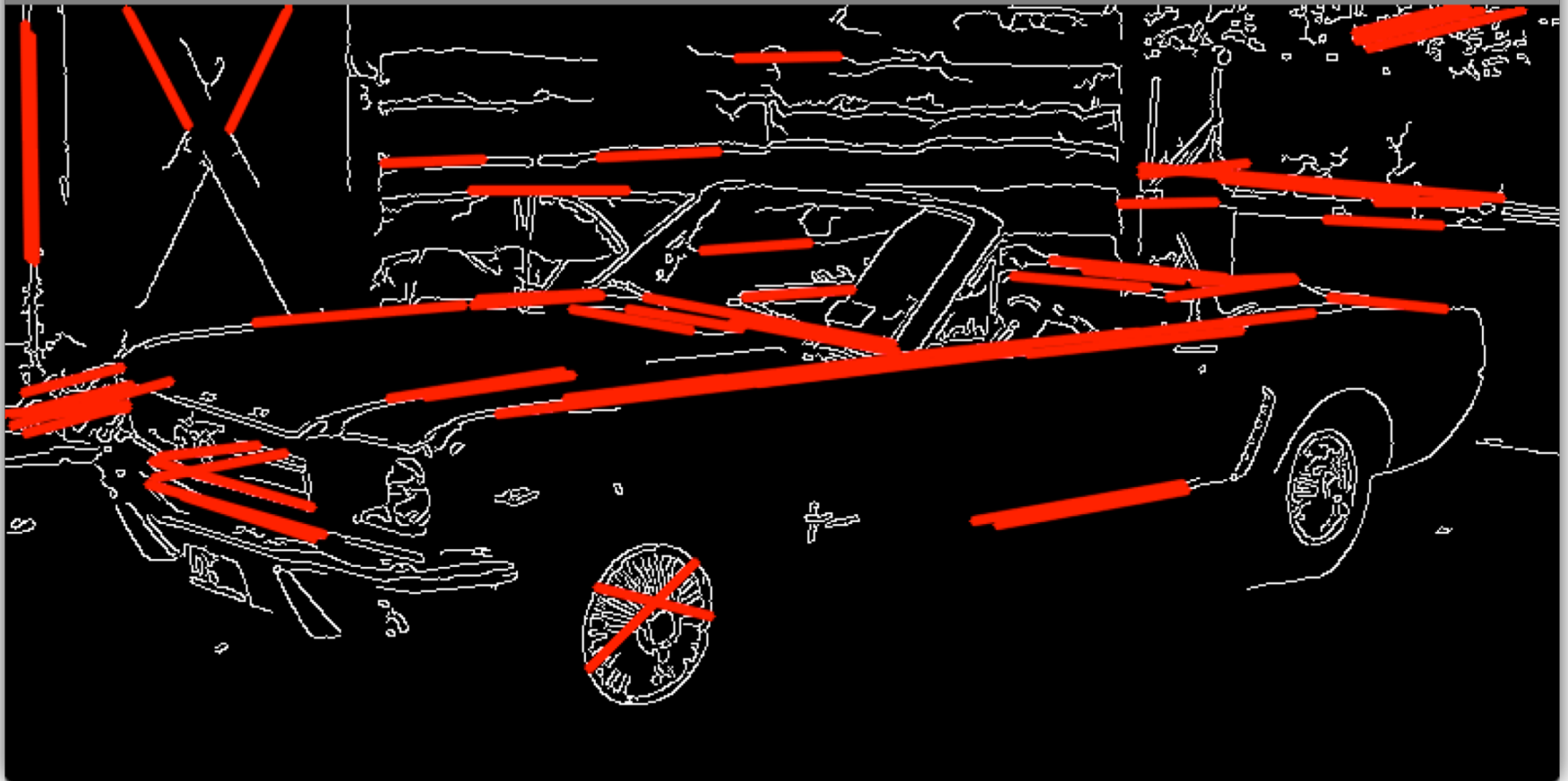


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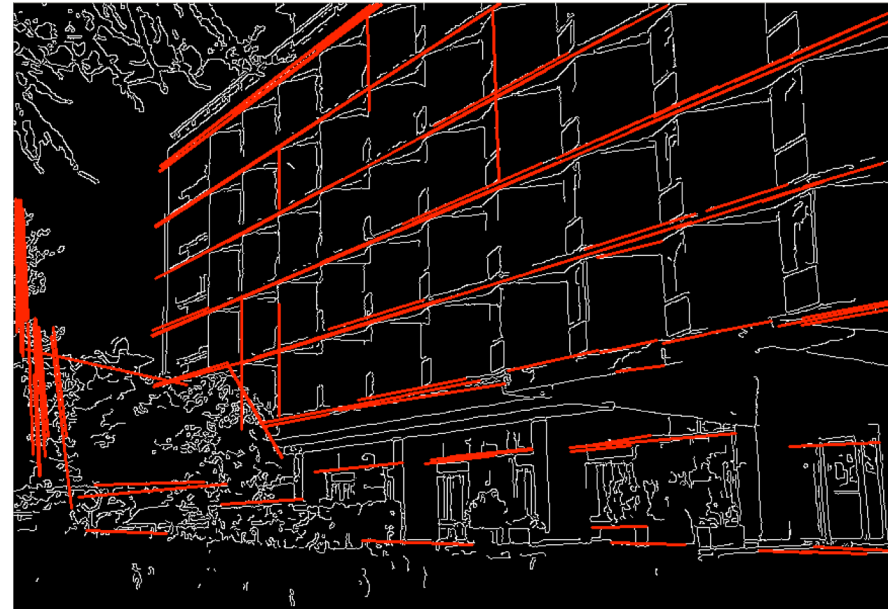
Edge Threshold:

Vote Threshold:

Min Edge Threshold: 70, Min Votes: 100



Building Example



http://docs.opencv.org/modules/imgproc/doc/feature_detection.html

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