

# Lecture05a: Particle Filters

CS540 2/13/18

## Announcements

### On-campus students:

Make sure I am wearing the microphone

### Off-campus students

Keep up. Expectations are the same as for on-campus students

### All students:

How are the projects coming?

Dejan has his doubts...

Thursday will be project presentations

Send me Powerpoint or pdf files by Wednesday night

## Simple Genetic Algorithm

1. Create initial population  $P$  with  $N$  elements  $x^i$
2. For  $l = 1$  to  $N$  do
  1. Calculate  $f(x^i)$
3. While (not termination criterion)
  1. Create  $M$  with  $N$  individuals selected from  $P$  (resampling based on  $f$ )
  2. Index = 1
  3. Repeat
    1. If  $\text{random}(0,1) \leq p$  recombine  $x^i$  and  $x^{i+1}$  and add to  $P'$
    2. Else copy  $x^i$  and  $x^{i+1}$  to  $P'$
    3. Index += 2
  4. Until index >  $N$
  5. For  $i = 1$  to  $N$ 
    - for  $j = 1$  to  $|x^i|$ 
      - if  $\text{random}(0,1) \leq p$  then mutate( $x^i$ ) in  $P'$
  6. Calculate  $f(x^i)$  for  $P'$
  7.  $P = P'$

## GAs are great for static problems

### Problems like

- Satisfiability
- Traveling Salesman
- *Static* path planning

### But what if the problem changes over time?

- What if the evaluation function is a function of state & time?
- So the optimal answer at time  $t$  is no longer optimal at  $t+1$ ?

OK, but doesn't really happen... does it?

## Tracking



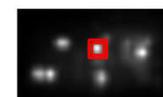
### Task:

Track children on playground

Measure their activity

Part of childhood obesity & playground equipment effectiveness study

## Motion Data



### Motion Data:

1. Model background
2. Label every pixel by probability of being foreground
3. Fitness function
  - (a) target pixels should be foreground
  - (b) target should be surrounded by background

## Tracking and GAs

There is a tight connection between *Genetic Algorithms* and *Particle Filters* and *Kalman Filters*

Let's look into it...

## Tracking as a Dynamic System

Targets move over time

- Partially observable state:  $\begin{bmatrix} x \\ y \\ \Delta x \\ \Delta y \\ w \\ h \end{bmatrix}$
- Motion model predicts next state based on  $(x, y, \Delta x, \Delta y)$
- Fitness based on  $(x, y, w, h)$

Observations

- Noisy
- Subject to occlusions & FOV

Multiple Targets

## Modify GAs for Tracking (step 1)

- Create initial population P with N elements  $x^i$
- For  $l = 1$  to N do
  - Calculate  $f(x^i, t)$
- While (not termination criterion)
  - Create M with N individuals selected from P (resampling based on f)
  - Index = 1
  - Repeat
    - If  $\text{random}(0,1) \leq p$  recombine  $x^i$  and  $x^{i+1}$  and add to P'
    - Else copy  $x^i$  and  $x^{i+1}$  to P'
  - Index += 2
  - Until index > N
  - For  $i = 1$  to N
    - for  $j = 1$  to  $|x^i|$ 
      - if  $\text{random}(0,1) \leq p$  then mutate( $x^i_j$ ) in P'
  - Calculate  $f(x^i, t)$  for P'
  - P = P'

Note: t is time,  
not iteration

## Modify GAs for Tracking (step 2)

- Create initial population P with N elements  $x^i$
- For  $l = 1$  to N do
  - Calculate  $f(x^i, t)$
- While (not termination criterion)
  - Create M with N individuals selected from P (resampling based on f)
  - Index = 1
  - Repeat
    - If  $\text{random}(0,1) \leq p$  recombine  $x^i$  and  $x^{i+1}$  and add to P'
    - Else copy  $x^i$  and  $x^{i+1}$  to P'
  - Index += 2
  - Until index > N
  - For  $i = 1$  to N
    - for  $j = 1$  to  $|x^i|$ 
      - if  $\text{random}(0,1) \leq p$  then mutate( $x^i_j$ ) in P'
  - Calculate  $f(x^i, t)$  for P'
  - P = P'

Particle Filters  
are GAs with  
selection &  
mutation, but  
not crossover.

## Modify GAs for Tracking (step 3)

- Create initial population P with N elements  $x^i$
- For  $l = 1$  to N do
  - Calculate  $f(x^i, t)$
- While (not termination criterion)
  - Create M with N individuals by
    - Selecting samples at time t according to their fitness
    - Forward predicting the sample to time t+1
  - For  $i = 1$  to N
    - for  $j = 1$  to  $|x^i|$ 
      - if  $\text{random}(0,1) \leq p$  then mutate( $x^i_j$ ) in P'
  - Calculate  $f(x^i, t)$  for P'
  - P = P'

Particle Filters  
are GAs with  
dynamic models  
for prediction.

## Extensions

It is possible to add a little local search

- Fit each track by optimizing the fitness function in a small search window on each step
  - Search in  $x, y, w$  &  $h$
  - Reset to local optimum
- Tends to increase redundancy, hurt diversity
- Increases cost (time)

It is possible to adapt the model

- Reset  $\Delta x$  and  $\Delta y$  to average motion over last N time steps

## Notes

### Particle Filters rely on redundancy

- Likelihood of a track propagating from  $t$  to  $t+1$  is
  - Based on fitness
  - Based on number of similar tracks (tracking same object)
- Otherwise noise or temporary occlusion could end track

### At termination

- Select tracks based on probability over time
  - Not final value of fitness function
- Still need to threshold tracks
  - Since there is no *single* answer

But we haven't really talked about forward prediction or probabilities. From Particle filters to Kalman Filters!