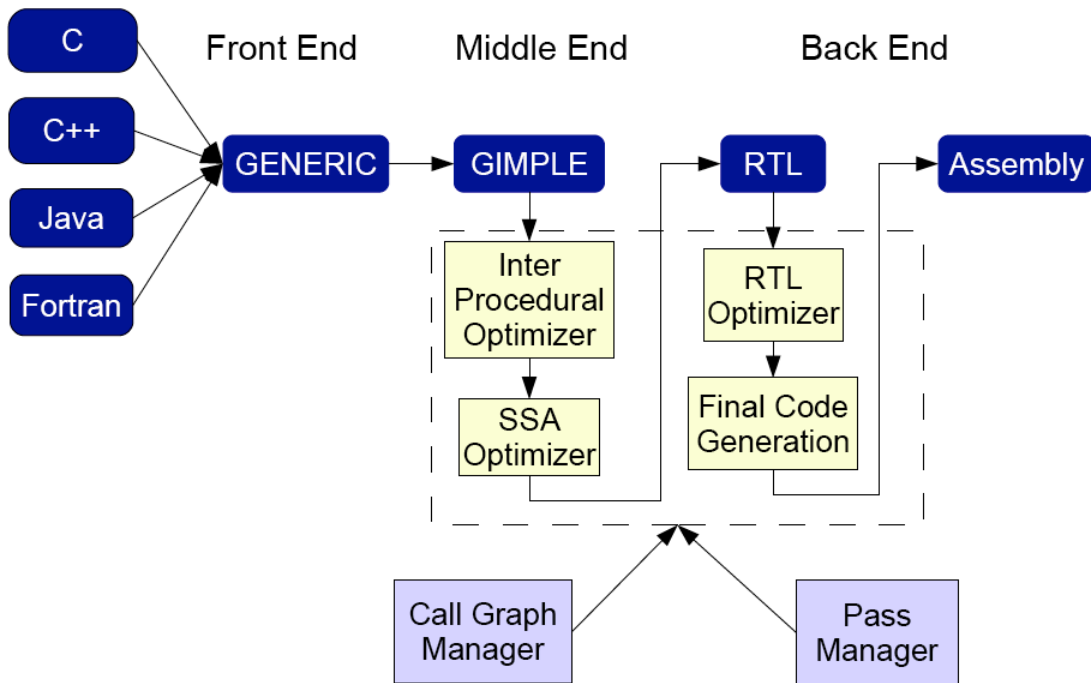


GCC Compiler Overview



CS553 Lecture

From **GCC - An Architectural Overview**, D. Novillo, September 2006.

1

GCC Overview cont...

SSA Optimizers

- vectorization
- loop optimizations
- scalar optimizations: CCP, DCE, DSE, FRE, PRE, VRP, SRA
- field-sensitive, points-to alias analysis

RTL Optimizers

- RTL has infinite registers
- register allocation
- scheduling, SW pipelining, CSE, ...

From **GCC - An Architectural Overview**, D. Novillo, September 2006.

CS553 Lecture

Static Single Assignment Form

2

LLVM Compiler Infrastructure

Source: "LLVM: A Compilation Framework for Lifelong Program Analysis & Transformation" by Lattner and Adve

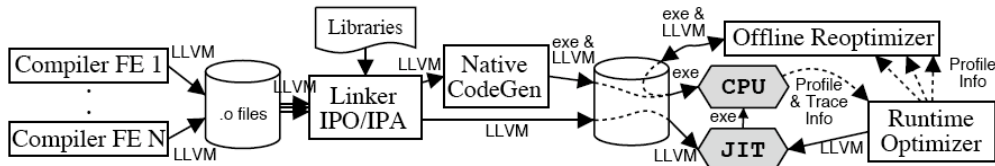


Figure 4: LLVM system architecture diagram

Goals

- lifelong analysis and optimization
- modular compiler components

IR is low level, control-flow graph and SSA

- language-independent types: any-bit ints, float, double, pointers, arrays, structures, functions
- interprocedural analysis and transformation

Status

- Apple is paying main developer (Chris Lattner) to continue development
- built OpenGL JIT compiler with it in two weeks

Static Single Assignment Form

Last Time

- Induction variable detection and elimination and strength reduction

Today

- Program representations
- Static single assignment (SSA) form
 - Program representation for sparse data-flow
- Conversion to and from SSA

Next Time

- Applications of SSA

Data Dependence

Definition

- Data dependences are constraints on the order in which statements may be executed

We say statement s_2 depends on s_1

- **Flow (true) dependence:** s_1 writes memory that s_2 later reads (RAW)
- **Anti-dependence:** s_1 reads memory that s_2 later writes (WAR)
- **Output dependences:** s_1 writes memory that s_2 later writes (WAW)
- **Input dependences:** s_1 reads memory that s_2 later reads (RAR)

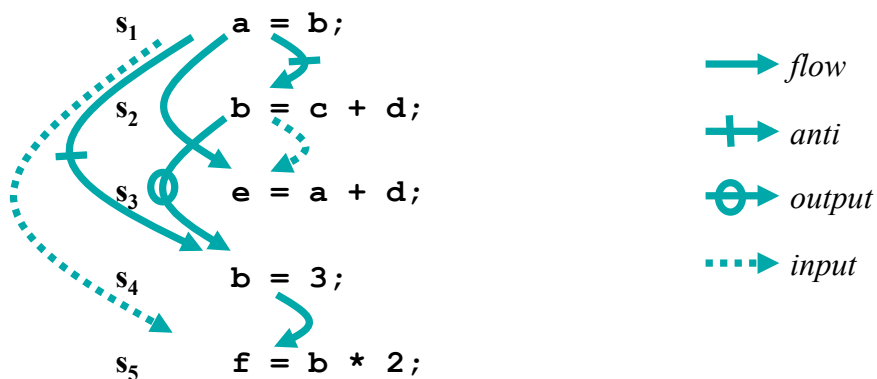
True dependences

- Flow dependences represent actual flow of data

False dependences

- Anti- and output dependences reflect reuse of memory, not actual data flow; can often be eliminated

Example



Representing Data Dependences

Implicitly

- Using variable defs and uses
- Pros: simple
- Cons: hides data dependence (analyses must find this info)

Def-use chains (du chains)

- Link each def to its uses
- Pros: explicit; therefore fast
- Cons: must be computed and updated, space consuming

Alternate representations

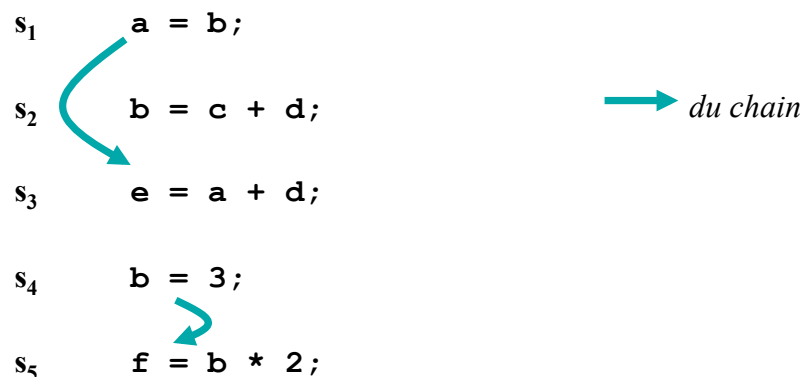
- *e.g.*, Static single assignment form (SSA), Program Dependence Graph (PDG), dependence flow graphs (DFG), value dependence graphs (VDG),

DU Chains

Definition

- du chains link each def to its uses

Example



Static Single Assignment (SSA) Form

Idea


- Each variable has only one static definition
- Makes it easier to reason about values instead of variables
- Similar to the notion of functional programming

Transformation to SSA

- Rename each definition
- Rename all uses reached by that assignment

Example

```
    v := ...
... := ... v ...
    v := ...
... := ... v ...
```



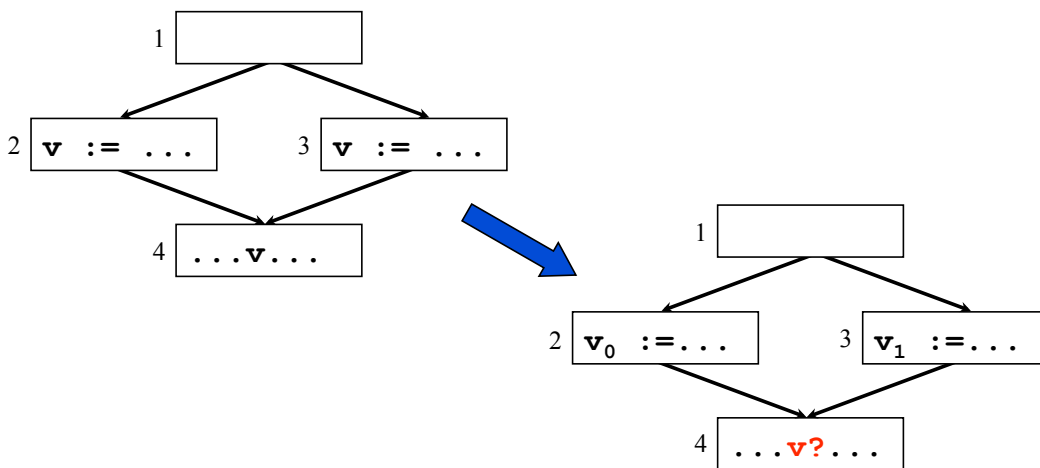
```
    v0 := ...
... := ... v0 ...
    v1 := ...
... := ... v1 ...
```

What do we do when there's control flow?

SSA and Control Flow

Problem

- A use may be reached by several definitions

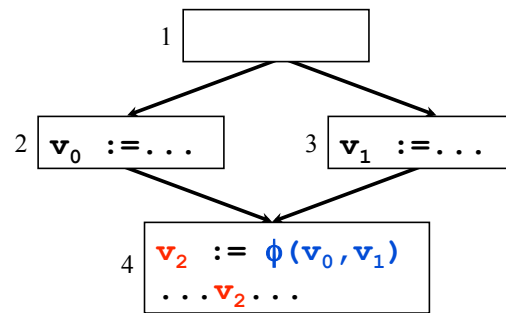


SSA and Control Flow (cont)

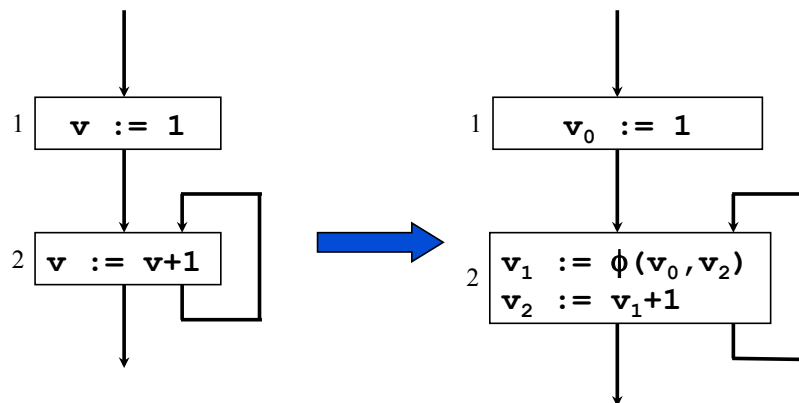
Merging Definitions

- ϕ -functions merge multiple reaching definitions

Example



Another Example



SSA vs. ud/du Chains

SSA form is more constrained

Advantages of SSA

- More compact
- Some analyses become simpler when each use has only one def
- Value merging is explicit
- Easier to update and manipulate?

Furthermore

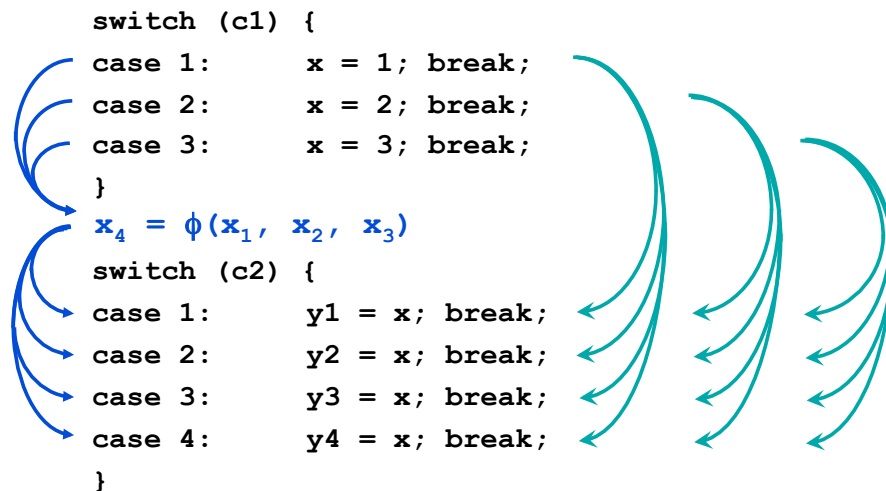
- Eliminates false dependences (simplifying context)

```
for (i=0; i<n; i++)
    A[i] = i;
for (i=0; i<n; i++)
    print(foo(i));
```

Unrelated uses of **i** are given
different variable names

SSA vs. ud/du Chains (cont)

Worst case du-chains?



m defs and n uses leads to $m \times n$ du chains

Transformation to SSA Form

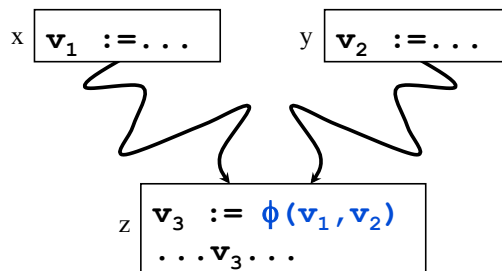
Two steps

- Insert ϕ -functions
- Rename variables

Where Do We Place ϕ -Functions?

Basic Rule

- If two distinct (non-null) paths $x \rightarrow z$ and $y \rightarrow z$ converge at node z , and nodes x and y contain definitions of variable v , then a ϕ -function for v is inserted at z



Approaches to Placing ϕ -Functions

Minimal

- As few as possible subject to the basic rule

Briggs-Minimal

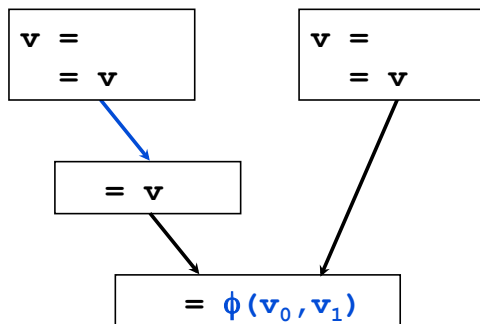
- Same as minimal, except v must be live across some edge of the CFG

Pruned

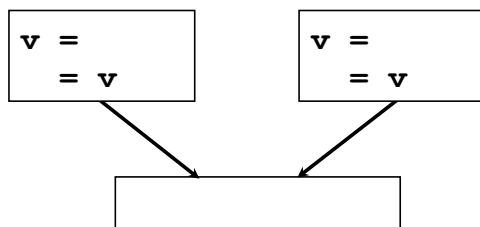
- Same as minimal, except dead ϕ -functions are not inserted

What's the difference between Briggs Minimal and Pruned SSA?

Briggs Minimal vs. Pruned



Briggs Minimal will add a ϕ function because v is live across the blue edge, but Pruned SSA will not because the ϕ function is dead



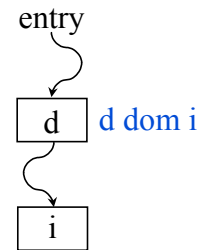
Neither Briggs Minimal nor Pruned SSA will place a ϕ function in this case because v is not live across any CFG edge

Why would we ever use Briggs Minimal instead of Pruned SSA?

Machinery for Placing ϕ -Functions

Recall Dominators

- d **dom** i if all paths from entry to node i include d
- d **sdom** i if d **dom** i and $d \neq i$



Dominance Frontiers

- The **dominance frontier** of a node d is the set of nodes that are “just barely” not dominated by d ; i.e., the set of nodes n , such that
 - d dominates a predecessor p of n , and
 - d does **not** strictly dominate n
- $DF(d) = \{n \mid \exists p \in \text{pred}(n), d \text{ dom } p \text{ and } d \not\text{sdom } n\}$

Notational Convenience

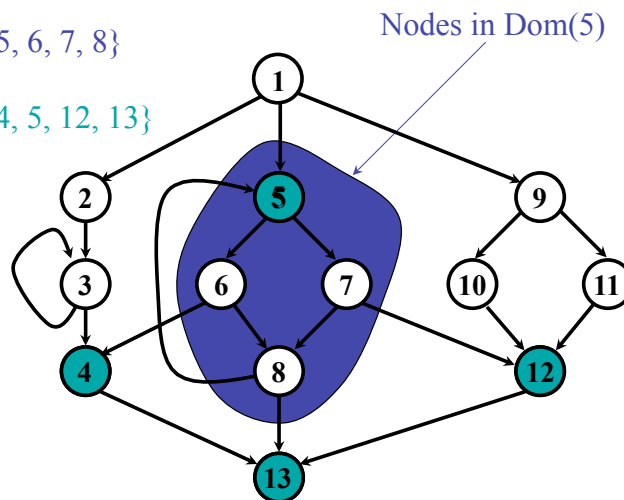
- $DF(S) = \bigcup_{n \in S} DF(n)$

Dominance Frontier Example

$$DF(d) = \{n \mid \exists p \in \text{pred}(n), d \text{ dom } p \text{ and } d \not\text{sdom } n\}$$

$$\text{Dom}(5) = \{5, 6, 7, 8\}$$

$$DF(5) = \{4, 5, 12, 13\}$$



What’s significant about the Dominance Frontier?

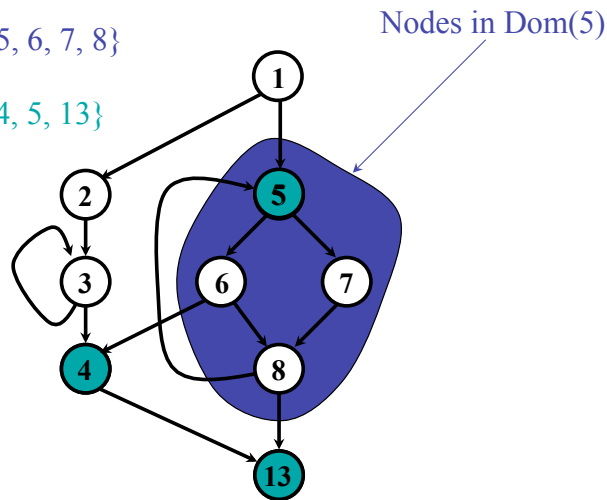
In SSA form, definitions must dominate uses

Dominance Frontier Example II

$$DF(d) = \{n \mid \exists p \in \text{pred}(n), d \text{ dom } p \text{ and } d \not\text{dom } n\}$$

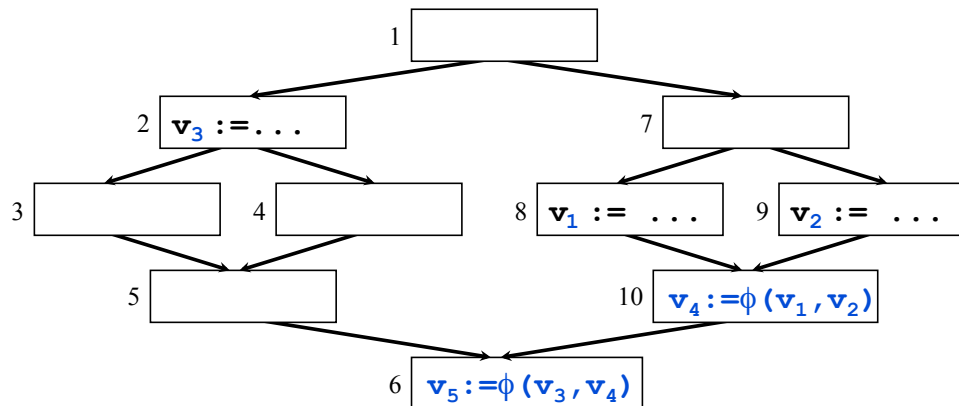
$$\text{Dom}(5) = \{5, 6, 7, 8\}$$

$$DF(5) = \{4, 5, 13\}$$



In this graph, node 4 is the first point of convergence between the entry and node 5, so do we need a ϕ -function at node 13?

SSA Exercise



$$DF(8) = \{10\}$$

$$DF(9) = \{10\}$$

$$DF(2) = \{6\}$$

$$DF(\{8,9\}) = \{10\}$$

$$DF(10) = \{6\}$$

$$DF(\{2,8,9,6,10\}) = \{6,10\}$$

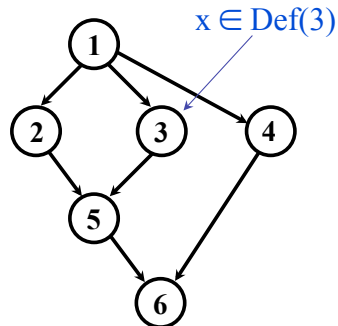
$$DF(d) = \{n \mid \exists p \in \text{pred}(n), d \text{ dom } p \text{ and } d \not\text{dom } n\}$$

See <http://www.hipersoft.rice.edu/grads/publications/dom14.pdf> for a more thorough description of DF.

Dominance Frontiers Revisited

Suppose that node 3 defines variable x

$$DF(3) = \{5\}$$



Do we need to insert a ϕ -function for x anywhere else?

Yes. At node 6. Why?

Dominance Frontiers and SSA

Let

- $DF_1(S) = DF(S)$
- $DF_{i+1}(S) = DF(S \cup DF_i(S))$

Iterated Dominance Frontier

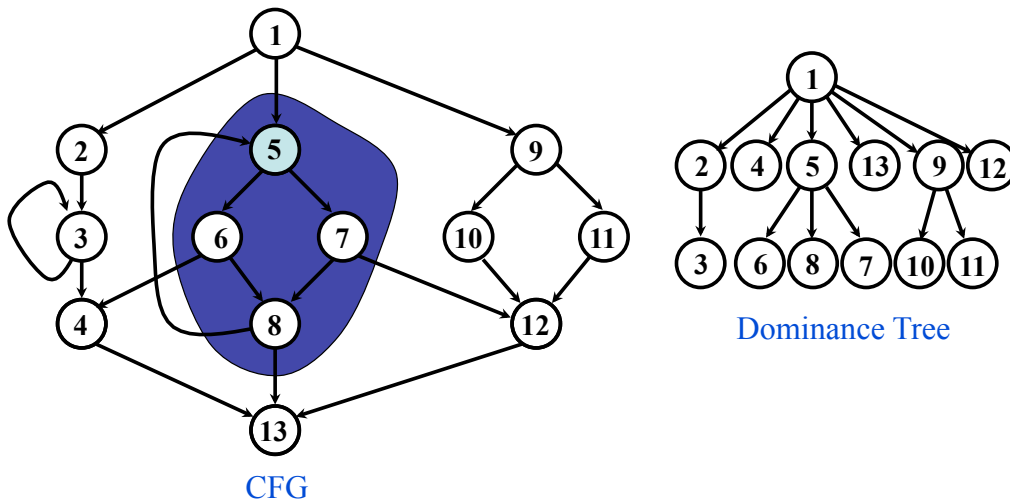
- $DF_\infty(S)$

Theorem

- If S is the set of CFG nodes that define variable v , then $DF_\infty(S)$ is the set of nodes that require ϕ -functions for v

Dominance Tree Example

The dominance tree shows the dominance relation



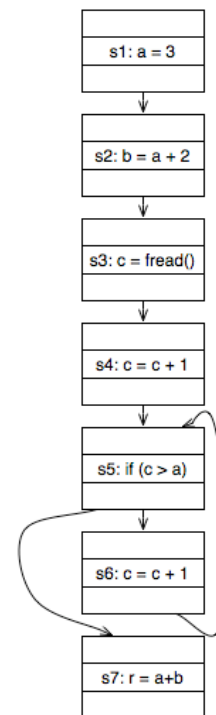
Inserting Phi Nodes

Calculate the dominator tree

- a lot of research has gone into calculating this quickly

Computing dominance frontier from dominator tree

- $DF_{local}[n]$ = successors of n (in CFG) that are not strictly dominated by n
- $DF_{up}[n]$ = nodes in the dominance frontier of n that are not strictly dominated by n 's immediate dominator
- $DF[n] = DF_{local}[n] \cup \bigcup_{c \in children[n]} DF_{up}[c]$



Algorithm for Inserting ϕ -Functions

```
for each variable v
  WorkList  $\leftarrow \emptyset$ 
  EverOnWorkList  $\leftarrow \emptyset$ 
  AlreadyHasPhiFunc  $\leftarrow \emptyset$ 
  for each node n containing an assignment to v   Put all defs of v on the worklist
    WorkList  $\leftarrow$  WorkList  $\cup$  {n}
  EverOnWorkList  $\leftarrow$  WorkList
  while WorkList  $\neq \emptyset$ 
    Remove some node n for WorkList
    for each d  $\in$  DF(n)
      if d  $\notin$  AlreadyHasPhiFunc                 Insert at most one  $\phi$  function per node
        Insert a  $\phi$ -function for v at d
        AlreadyHasPhiFunc  $\leftarrow$  AlreadyHasPhiFunc  $\cup$  {d}
      if d  $\notin$  EverOnWorkList                   Process each node at most once
        WorkList  $\leftarrow$  WorkList  $\cup$  {d}
        EverOnWorkList  $\leftarrow$  EverOnWorkList  $\cup$  {d}
```

CS553 Lecture

Static Single Assignment Form

29

Transformation to SSA Form

Two steps

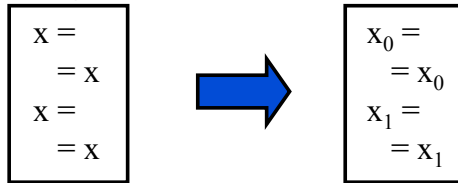
- Insert ϕ -functions
- Rename variables

Variable Renaming

Basic idea

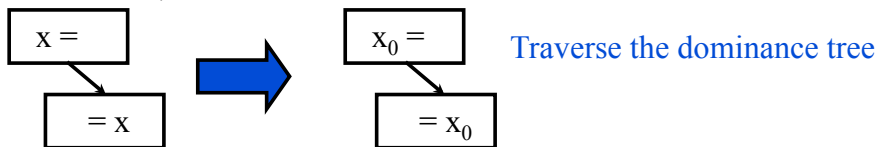
- When we see a variable on the LHS, create a new name for it
- When we see a variable on the RHS, use appropriate subscript

Easy for straightline code



Use a stack when there's control flow

- For each use of x , find the definition of x that dominates it



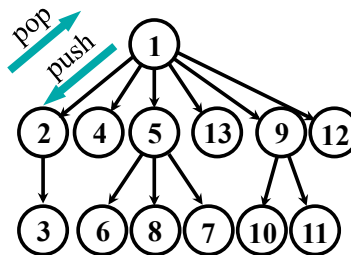
Variable Renaming (cont)

Data Structures

- $\text{Stacks}[v] \forall v$
Holds the subscript of most recent definition of variable v , initially empty
- $\text{Counters}[v] \forall v$
Holds the current number of assignments to variable v ; initially 0

Auxiliary Routine

```
procedure GenName(variable v)
  i := Counters[v]
  push i onto Stacks[v]
  Counters[v] := i + 1
```



Use the Dominance Tree to remember the most recent definition of each variable

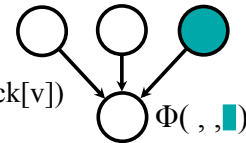
Variable Renaming Algorithm

procedure Rename(block b)
 if b previously visited return

Call Rename(entry-node)

for each statement s in b (in order)
for each variable $v \in \text{RHS}(s)$ (except for ϕ -functions)
 replace v by v_i , where $i = \text{Top}(\text{Stack}[v])$
for each variable $v \in \text{LHS}(s)$
 GenName(v) and replace v with v_i , where $i = \text{Top}(\text{Stack}[v])$

for each $s \in \text{succ}(b)$ (in CFG)
 j \leftarrow position in s's ϕ -function corresponding to block b
for each ϕ -function p in s
 replace the j^{th} operand of RHS(p) by v_i , where $i = \text{Top}(\text{Stack}[v])$



for each $s \in \text{child}(b)$ (in DT)
 Rename(s)

for each ϕ -function or statement t in b
for each $v_i \in \text{LHS}(t)$
 Pop(Stack[v])

Recurse using Depth First Search

Unwind stack when done with this node

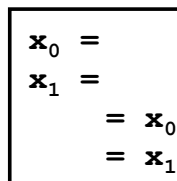
Transformation from SSA Form

Proposal

- Restore original variable names (*i.e.*, drop subscripts)
- Delete all ϕ -functions

Complications (the proposal doesn't work!)

- What if versions get out of order?
 (simultaneously live ranges)



Alternative

- Perform dead code elimination (to prune ϕ -functions)
- Replace ϕ -functions with copies in predecessors
- Rely on register allocation coalescing to remove unnecessary copies

Concepts

Data dependences

- Three kinds of data dependences
- du-chains

Alternate representations

SSA form

Conversion to SSA form

- ϕ -function placement
- variable renaming

Next Time

Assignments

- Read Alpern and Zadeck paper on value numbering

Lecture

- Using SSA to apply optimizations