

CSX55: DISTRIBUTED SYSTEMS [ARCHITECTURES/TOPOLOGY]

Decentralized topologies

Nodes without a weave
Like wings without flight

Connect them near and far
And watch it soar
Imbuing each with a nifty quirk
Assets that make them tick

This you probably knew,
Your networks tell a lot about you

Shrideep Pallickara
Computer Science
Colorado State University

COMPUTER SCIENCE DEPARTMENT



COLORADO STATE UNIVERSITY

1

Frequently asked questions from the previous class survey

- How is F calculated in Amdahl's law?
- Out-of-band data?
- Switch: stability and flexibility
- Isn't TCP handoff a flavor of IP spoofing? Aren't there protections against this?
- Thread-per-object architecture
- MIPv6



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.2

2

Topics covered in this lecture

- Decentralized architectures
- Topologies
 - Regular graphs
 - Random graphs
 - Small world graphs
 - Power law networks

Ryan Stern and Shrideep Pallickara. On the Role of Topology in Autonomously Coping with Failures in Content Dissemination Systems. Proceedings of the ACM Cloud and Autonomic Computing Conference. Miami, USA. 2013.



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.3

3



4

Decentralized architectures

- Server may be split up into logically equivalent parts
 - ▣ Each part operates on its share of the dataset
 - ▣ Balance the load
- Interaction between processes is **symmetric**
 - ▣ Each **peer** acts as a client and a server



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.5

5

Structured Peer to Peer Architectures: Distributed hash tables

- **Data items** are assigned an identifier from a large random space
 - 128-bit UUIDs or 160-bit SHA-1 digests
- **Nodes** are also assigned a number from the **same** identifier space



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.6

6

Crux of the DHT problem

- Implement an efficient, **deterministic** scheme to *map data item to node*
- When you look up a data item?
 - Network address of node holding the data is returned



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.7

7

Unstructured P2P networks that rely on random graphs

- Maintain connections to randomly chosen live nodes
- To locate a data item
 - **Flood** the network



COLORADO STATE UNIVERSITY

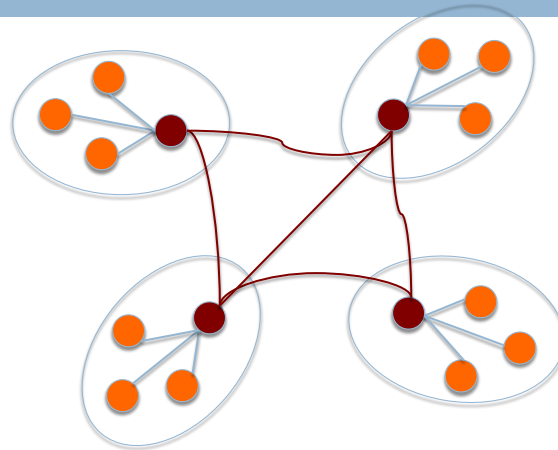
Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.8

8

Hierarchical organization of nodes



Super peer ●
Regular peer ●



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.9

9

Superpeer networks

- The client-superpeer relationship is **fixed**
 - When a peer joins, it *attaches* itself to the superpeer and stays attached till it leaves
- Superpeers are expected to be *long-lived* processes with *high-availability*
- Selecting nodes that are eligible to be superpeers?
 - Closely related to the leader **election** problem



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.10

10



11

Stanley Milgram's experiment on social networks

- In 1967 he mailed 160 letters
- People were randomly chosen from Omaha, Nebraska
- Objective was to pass their letter
 - ▣ TARGET: Stock broker in Boston, MA
 - ▣ CONSTRAINT: Use *intermediary* known to them on a **first-name** basis



12

Results: It's a small, small world

- 42 letters made it through
 - Median was just 5.5. intermediaries
 - US Population in 1967: 200 million
 - 2024: 341 million
- First demonstration of what is known as the **small world** effect



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.13

13

Intuitively it seems that the pathlengths should have been much higher

- People's social circle is cliquish or **clustered**
- People you know, know each other



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.14

14

The key is the distribution of links within social networks

- Some acquaintances are relatively isolated
- Some have wide ranging connections
 - ▣ Play a critical role in bringing network **closer** together
- Milgram experiment
 - ▣ $\frac{1}{4}$ of the successful chains passed through a local storekeeper



The Hollywood Network:

- Here we organize all actors in a graph
- If they have co-starred with someone in a movie
 - ▣ They have a direct link to them (1 hop)
- Some actors have more links than others because they have acted in so many movies
 - ▣ E.g., Kevin Bacon



The Hollywood Network: 6 degrees of Kevin Bacon

- John Carradine: 4000 links
- Robert Mitchum: 2905 links
- But acting in the most movies does not always translate into shortest hops to a random node in the network
- Rankings:
 - Rod Steiger: 2.53
 - Donald Pleasence: 2.54
 - Martin Sheen, Christopher Lee, Robert Mitchum, Charlton Heston
 - Kevin Bacon? 2.79 pathlength and ranked 876th



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.17

17

Turns out even a small number of bridges can dramatically reduce pathlengths

Duncan Watts and Steven Strogatz (1998), "*Collective Dynamics of 'Small-World' Networks*," Nature 393, p 440.



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.18

18

Regular Graphs

- Ring of n vertices
- Each of the nodes are connected to its **nearest k** neighbors



COLORADO STATE UNIVERSITY

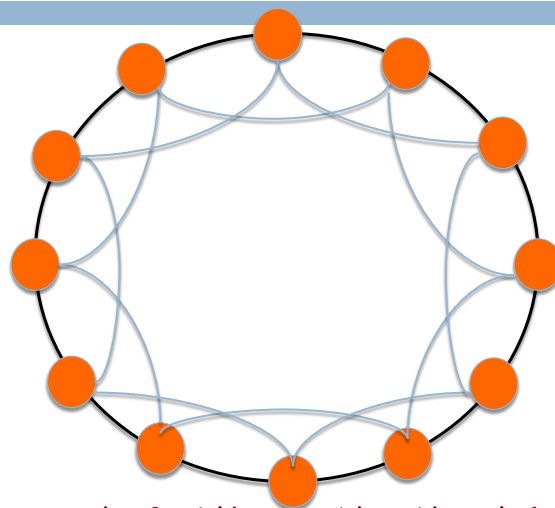
Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.19

19

Example regular graph with $k = 4$



Each node is connected to 2 neighbors on either side; so $k=4$



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.20

20

Pathlength in a graph

- Average number of **hops** to reach any node in the system
 - For **each pair** of vertices, compute shortest path
 - Take the average over all pairs
- Gives a sense of **how far apart** points are in the network



Clustering coefficients are a measure of the level of clustering

- For k neighbors of a vertex, the number of possible connections between them is

$$C_2^k = \frac{k(k-1)}{2}$$

- **Clustering coefficient** of a vertex
 - Proportion ($0 \sim 1$) of possible links actually present in graph



Pathlength in Regular graphs

- Approximately $n/2k$
- If $n=4096$ and $k=8$
- Pathlength = $n/2k = 256$
 - ▣ Very large!



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

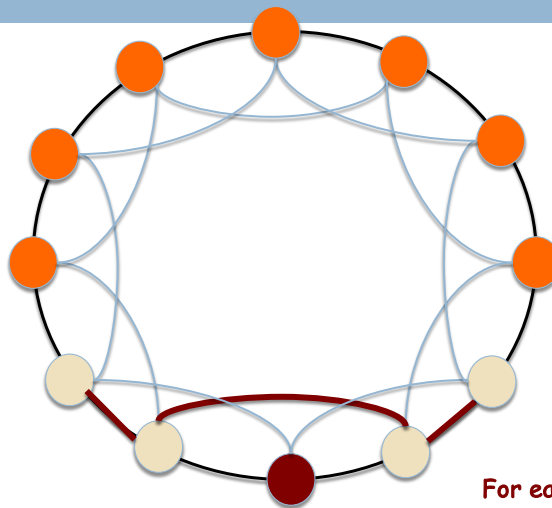
ARCHITECTURES & TOPOLOGY

L11.23

23

Clustering Coefficient: Regular graph $k=4$

$$\text{Clustering coefficient} = \frac{3(k-2)}{4(k-1)}$$



For each vertex = $3/6$



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.24

24

Random Graphs

- Opposite of regular graphs
- Vertices are connected to each other at **random**



COLORADO STATE UNIVERSITY

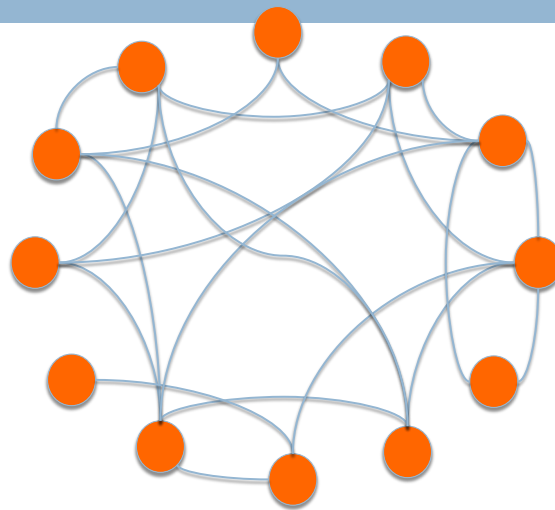
Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.25

25

Random Graphs



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.26

26

Pathlength and clustering coefficients in Random Graphs

- Pathlength is approximately $\log n / \log k$
- Clustering coefficient is approximately: k/n

- So, with $n=4096$ and $k = 8$
 - Average pathlength = $\log 4096 / \log 8 = 4$
 - Much better than regular graphs
- Clustering coefficient = $8/4096 = 0.002$
 - Much lower than regular graphs



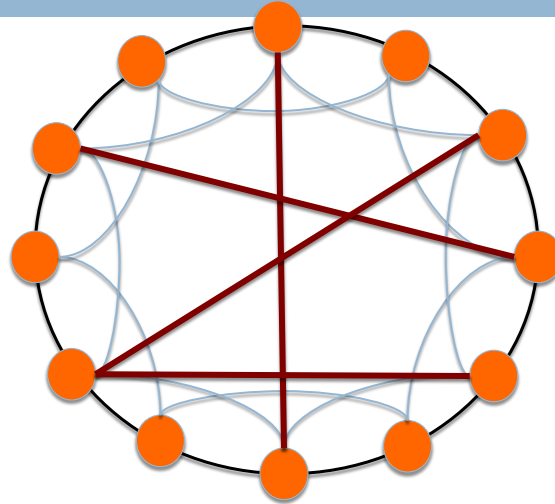
Comparing regular and random graphs

- Regular graph
 - **High clustering**
 - High pathlength

- Random graph
 - Low clustering
 - **Low pathlength**



Small world graphs: Add a few random links to the regular graph



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.29

29

Small world graphs

- High local clustering
- Short global pathlengths

- Implications:
 - ▣ Small amount of rewiring needed to promote the transition
 - ▣ Transition is barely noticeable at the local level



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.30

30

As restless as we are
We feel the pull
In the land of a thousand guilts
And poured cement
Lamented and assured
To the lights and towns below
Faster than the speed of sound
Faster than we thought we'd go
Beneath the sound of hope

1979, Benji Madden; Joel Madden; Matt Squire, The Smashing Pumpkins



SCALE FREE NETWORKS

COMPUTER SCIENCE DEPARTMENT

COLORADO STATE UNIVERSITY

31

Power law is a special relationship between two quantities

- The number or frequency of the object
 - Varies as a **power**
- Of some attribute (size) of the object
- Earthquakes
 - The frequency of earthquakes varies as a power of the size of the earthquake

COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.32

32

Power law and Random Networks: Real World examples

- Random networks
 - Eisenhower National Highway System
 - Nodes=Cities, Links=Highways connecting them
 - Most cities served by roughly the same number of highways
- Scale-free networks
 - Airport system
 - Large number of small airports served by a few major **hubs**



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.33

33

Distribution of links in random networks

- Follows a **bell curve**
- Most nodes have the same number of links



COLORADO STATE UNIVERSITY

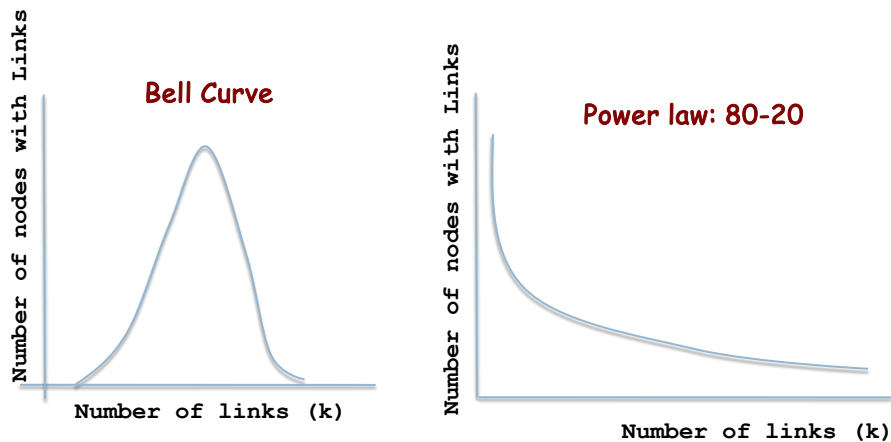
Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.34

34

Comparison of the distribution of links in random and scale-free networks



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.35

35

Growth of scale-free networks

- Addition of nodes
- **Preferential attachment**
 - Nodes prefer to attach to well-connected nodes
- **RESULT:** Highly connected nodes emerge



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.36

36

Power law distributions have no peak

- Continuously decreasing curve
- Many small events coexist with a few very large ones

- Imaginary planet:
 - ▣ Most people will be really short
 - ▣ Among 6 billion people, 1 person would be 8000 ft



Bell Curves vs Power Laws

- Bell Curves
 - ▣ Occur very often in nature
 - ▣ Exponentially decaying tail
 - Responsible for **absence** of hubs

- Power Laws
 - ▣ Emerge during phase transitions
 - Move from chaos to order: Self organization
 - ▣ Decay far more slowly
 - Allows for hubs



Why power law networks are called scale-free [1/2]

- In a random network vast majority of nodes have same number of links
 - Nodes deviating from average are rare
 - There is a characteristic **scale** in its connectivity
 - Embodied by the average node
 - Fixed by the peak of the degree distribution



Why power law networks are called scale-free [2/2]

- In a power law network
 - Absence of peak
- No such thing as a characteristic node
 - Continuous hierarchy of nodes spanning from rare hubs to numerous tiny nodes
- No intrinsic scale in power law networks
 - **Scale-free** networks



Achilles' heel in the power law network

- Power law networks are robust to random failures
- Vulnerable to a targeted attack on hubs
- Removal of hubs
 - ▣ Disintegrates these networks
 - ▣ Breaks them up into tiny non-communicating islands



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.41

41

Coexistence of robustness and vulnerability plays a role in complex systems

- Sea otters in California went nearly extinct because of excessive hunting for its pelts
- In 1911 federal regulators banned hunting them
 - ▣ Otters made a dramatic comeback



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.42

42

The case of the otter recovery

[1/2]

- Because otters feed on *urchins*, increase in their numbers leads to a decrease in the number of urchins
- With fewer urchins around, the number of *kelps* went up dramatically
- Increased the supply of food for fish
 - ▣ Protected the coast from erosion



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.43

43

The case of the otter recovery

[2/2]

- Protection of one species (a hub) altered economy and ecology of the coastline
- Finfish now dominate coastal fisheries
 - ▣ Once dedicated to shellfish



COLORADO STATE UNIVERSITY

Professor: SHRIDEEP PALLICKARA
COMPUTER SCIENCE DEPARTMENT

ARCHITECTURES & TOPOLOGY

L11.44

44

The contents of this slide set are based on the following references

- *Peer-to-Peer: Harnessing the Power of Disruptive Technologies*. Edited by Andy Oram. O'Reilly Publishing. ISBN: 0-596-00110-X.
[Chapter 14 – Performance by Theodore Hong]
- *Linked: How Everything is Connected to Everything Else and What it Means for Business, Science, and Everyday Life*. Albert-László Barabási. Plume. ISBN: 0452284392/978-0452284395.
[Chapters 4,5,6, and 7]

