## iClicker

# Chapter 8 Multidimensional Arrays 

# CS1: Java Programming Colorado State University 

Original slides by Daniel Liang Modified slides by Chris Wilcox

## Motivations

Thus far, you have used one-dimensional arrays to model linear collections of elements. You can use a two-dimensional array to represent a matrix or a table. For example, the following table that describes the distances between the cities can be represented using a two-dimensional array.

| Distance Table (in miles) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Chicago Boston New York Atlanta Miami Dallas Houston |  |  |  |  |  |  |


| Chicago | 0 | 983 | 787 | 714 | 1375 | 967 | 1087 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Boston | 983 | 0 | 214 | 1102 | 1763 | 1723 | 1842 |
| New York | 787 | 214 | 0 | 888 | 1549 | 1548 | 1627 |
| Atlanta | 714 | 1102 | 888 | 0 | 661 | 781 | 810 |
| Miami | 1375 | 1763 | 1549 | 661 | 0 | 1426 | 1187 |
| Dallas | 967 | 1723 | 1548 | 781 | 1426 | 0 | 239 |
| Houston | 1087 | 1842 | 1627 | 810 | 1187 | 239 | 0 |

## Other Representations?

## What are some other representations of multi-dimensional arrays?

## Motivations

```
double[][] distances = {
    {0, 983, 787, 714, 1375, 967, 1087},
    {983, 0, 214, 1102, 1763, 1723, 1842},
    {787, 214, 0, 888, 1549, 1548, 1627},
    {714, 1102, 888, 0, 661, 781, 810},
    {1375, 1763, 1549, 661, 0, 1426, 1187},
    {967, 1723, 1548, 781, 1426, 0, 239},
    {1087, 1842, 1627, 810, 1187, 239, 0},
};
```


## Declare/Create Two-dimensional Arrays

// Declare array ref var dataType[][] refVar;
// Create array and assign its reference to variable refVar $=$ new dataType[10][10];
// Combine declaration and creation in one statement dataType[][] refVar = new dataType[10][10];
// Alternative syntax dataType refVar[][] = new dataType[10][10];

# Declaring Variables of <br> Two-dimensional Arrays and Creating Two-dimensional Arrays 

```
int[][] matrix = new int[10][10];
    or
int matrix[][] = new int[10][10];
matrix[0][0] = 3;
for (int i = 0; i < matrix.length; i++)
    for (int j = 0; j < matrix[i].length; j++)
        matrix[i][j] = (int) (Math.random() * 1000)
```

double[][] x;

## Two-dimensional Array Illustration

| $[0][1][2][3][4]$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $[0]$ 0 0 0 0 0 <br> $[1]$ 0 0 0 0 0 <br> $[2]$ 0 0 0 0 0 <br> $[3]$ 0 0 0 0 0 <br> $[4]$ 0 0 0 0 0 |  |  |  |  |  |

matrix = new int[5][5];
(a)

| [0][1][2][3][4] |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| [0] | 0 | 0 | 0 | 0 | 0 |
| [1] | 0 | 0 | 0 | 0 | 0 |
| [2] | 0 | 7 | 0 | 0 | 0 |
| [3] | 0 | 0 | 0 | 0 | 0 |
| [4] | 0 | 0 | 0 | 0 | 0 |

matrix.length? 5
matrix[0].length? 5
(b)
[0][1][2]

| $[0]$ | 1 | 2 | 3 |
| :--- | :---: | :---: | :---: |
| $[1]$ | 4 | 5 | 6 |
| $[2]$ | 7 | 8 | 9 |
| $[3]$ | 10 | 11 | 12 |
|  |  |  |  |

int[][] array = \{
$\{1,2,3\}$,
$\{4,5,6\}$,
$\{7,8,9\}$,
$\{10,11,12\}$
\};
(c)
array.length? 4 array[0].length? 3

## Declaring, Creating, and Initializing Using Shorthand Notations

You can also use an array initializer to declare, create and initialize a two-dimensional array. For example,


## Lengths of Two-dimensional Arrays

$$
\operatorname{int[[][]~x~=~new~int[3][4];~}
$$



## Lengths of Two-dimensional Arrays, cont.

$$
\begin{aligned}
& \text { int[][] array }=\{ \\
& \{1,2,3\}, \\
& \{4,5,6\}, \\
& \{7,8,9\}, \\
& \{10,11,12\} \\
& \}
\end{aligned}
$$

array[4].length ArrayIndexOutOfBoundsException

## Ragged Arrays

Each row in a two-dimensional array is itself an array. So, the rows can have different lengths. Such an array is known as a ragged array. For example, int[][] matrix $=\{$
$\{1,2,3,4,5\}$,
$\{2,3,4,5\}$,
$\{3,4,5\}$,
$\{4,5\}$,
\{5\}
\};

## Ragged Arrays, cont.

int[][] triangleArray $=$ \{
$\{1,2,3,4,5\}$,
$\{2,3,4,5\}$,
$\{3,4,5\}$,
$\{4,5\}$,
\{5\}
\};


## Initializing arrays with input values

java.util.Scanner input = new Scanner(System.in);
System.out.println("Enter " + matrix.length + " rows and " + matrix[0].length + " columns: "); for (int row $=0$; row $<$ matrix.length; row ++ ) \{ for (int column $=0 ;$ column $<$ matrix[row].length; column++) $\{$ matrix[row][column] = input.nextInt();

## Initializing arrays with random values

```
for (int row = 0; row < matrix.length; row++) {
    for (int column = 0; column < matrix[row].length; column++) {
        matrix[row][column] = (int)(Math.random() * 100);
    }
}
```


## Printing arrays

```
for (int row = 0; row < matrix.length; row++) {
    for (int column = 0; column < matrix[row].length; column++) {
    System.out.print(matrix[row][column] + " ");
}
```

    System.out.println();
    \}

## Summing all elements

```
int total = 0;
for (int row = 0; row < matrix.length; row++) {
    for (int column = 0; column < matrix[row].length; column++) {
        total += matrix[row][column];
    }
}
```


## Summing elements by column

for (int column $=0 ;$ column $<$ matrix[0].length; column++) \{ int total $=0$;
for (int row $=0$; row $<$ matrix.length; row ++ ) total $+=$ matrix[row][column];
System.out.println("Sum for column " + column + " is " + total);

## Random shuffling

for (int $\mathrm{i}=0 ; \mathrm{i}<$ matrix.length; $\mathrm{i}++$ ) \{
for (int $\mathrm{j}=0 ; \mathrm{j}<\operatorname{matrix[i].length;~} \mathrm{j}++$ ) \{ int il $=(\mathrm{int})($ Math.random() $*$ matrix.length); int j1 $=(\mathrm{int})($ Math.random ()$*$ matrix[i].length $) ;$ // Swap matrix[i][j] with matrix[i1][j1] int temp $=$ matrix $[i][j] ;$ $\operatorname{matrix}[i][j]=\operatorname{matrix}[i 1][j 1]$; $\operatorname{matrix}[i 1][j 1]=$ temp;

# Passing Two-Dimensional Arrays to Methods 

## Problem: Grading Multiple-Choice Test

Students' answer
0123456789

Student 0
Student 1
Student 2
Student 3
Student 4
Student 5
Student 6
Student 7

Objective: write a program that grades multiple-choice test.

Key to the Questions:
$\begin{array}{llllllllll}0 & 2 & 3 & 5 & 6 & 8\end{array}$
Key D B D C C D A E A D

PassTwoDimensionalArray
Run

## Problem: Finding Two Points Nearest to Each Other



## Multidimensional Arrays

Occasionally, you will need to represent n-dimensional data structures. In Java, you can create n -dimensional arrays for any integer n .

The way to declare two-dimensional array variables and create two-dimensional arrays can be generalized to declare n-dimensional array variables and create n -dimensional arrays for n 3.

## Multidimensional Arrays

```
double[][][] scores = {
    {{7.5,20.5},{9.0,22.5},{15,33.5},{13,21.5},{15,2.5}},
    {{4.5,21.5},{9.0,22.5},{15, 34.5},{12,20.5},{14, 9.5}},
    {{6.5,30.5},{9.4,10.5},{11,33.5},{11, 23.5},{10, 2.5}},
    {{6.5,23.5},{9.4, 32.5},{13, 34.5},{11, 20.5},{16,7.5}},
    {{8.5,26.5},{9.4, 52.5},{13, 36.5},{13,24.5},{16, 2.5}},
    {{9.5,20.5},{9.4,42.5},{13,31.5},{12, 20.5},{16,6.5}}
};
```

Which student
Which exam
Multiple-choice or essay


## Misc Slides

## Problem: Calculating Total Scores

Objective: write a program that calculates the total score for students in a class. Suppose the scores are stored in a three-dimensional array named scores. The first index in scores refers to a student, the second refers to an exam, and the third refers to the part of the exam. Suppose there are 7 students, 5 exams, and each exam has two parts--the multiple-choice part and the programming part. So, scores[i][i][0] represents the score on the multiple-choice part for the i's student on the i's exam. Your program displays the total score for each student.

TotalScore Run

## Problem: Weather Information

Suppose a meteorology station records the temperature and humidity at each hour of every day and stores the data for the past ten days in a text file named weather.txt. Each line of the file consists of four numbers that indicate the day, hour, temperature, and humidity. Your task is to write a program that calculates the average daily temperature and humidity for the $\underline{10}$ days.

```
1 1 76.4 0.92
1 2 77.7 0.93
10 23 97.7 0.71
10 24 98.7 0.74
```

```
10 24 98.7 0.74
1277.7 0.93
10 23 97.7 0.71
1 1 76.4 0.92
```

(b)

Weather Run

## Problem: Guessing Birthday

Listing 4.3, GuessBirthday.java, gives a program that guesses a birthday. The program can be simplified by storing the numbers in five sets in a three-dimensional array, and it prompts the user for the answers using a loop.

## Objectives

- To give examples of representing data using two-dimensional arrays (§8.1).
- To declare variables for two-dimensional arrays, create arrays, and access array elements in a two-dimensional array using row and column indexes (§8.2).
- To program common operations for two-dimensional arrays (displaying arrays, summing all elements, finding the minimum and maximum elements, and random shuffling) (§8.3).
- To pass two-dimensional arrays to methods (§8.4).
- To write a program for grading multiple-choice questions using two-dimensional arrays (§8.5).
- To solve the closest-pair problem using two-dimensional arrays (\$8.6).
- To check a Sudoku solution using two-dimensional arrays (§8.7).
- To use multidimensional arrays (§8.8).


## What is Sudoku?

| 5 | 3 |  |  | 7 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 |  |  | 1 | 9 | 5 |  |  |  |
|  | 9 | 8 |  |  |  |  | 6 |  |
| 8 |  |  |  | 6 |  |  |  | 3 |
| 4 |  |  | 8 |  | 3 |  |  | 1 |
| 7 |  |  |  | 2 |  |  |  | 6 |
|  | 6 |  |  |  |  |  |  |  |
|  |  |  | 4 | 1 | 9 |  |  | 5 |
|  |  |  |  | 8 |  |  | 7 | 9 |

http://www.cs.armstrong.edu/liang /animation/web/Sudoku.html

## Every row contains the numbers 1 to 9

| 5 | 3 |  |  | 7 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 |  |  | 1 | 9 | 5 |  |  |  |
|  | 9 | 8 |  |  |  |  | 6 |  |
| 8 |  |  |  | 6 |  |  |  | 3 |
| 4 |  |  | 8 |  | 3 |  |  | 1 |
| 7 |  |  |  | 2 |  |  |  | 6 |
|  | 6 |  |  |  |  |  |  |  |
|  |  |  | 4 | 1 | 9 |  |  | 5 |
|  |  |  |  | 8 |  |  | 7 | 9 |


| 5 | 3 | 4 | 6 | 7 | 8 | 9 | 1 | 2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
|  | 1 | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
|  | 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
|  | 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
|  | 7 | 1 | 3 | 9 | 2 | 4 | 8 | 5 | 6 |
|  | 9 | 6 | 1 | 5 | 3 | 7 | 2 | 8 | 4 |
|  | 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
|  | 3 | 4 | 5 | 2 | 8 | 6 | 1 | 7 | 9 |

## Every column contains the numbers 1 to 9

| 5 | 3 |  |  | 7 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 |  |  | 1 | 9 | 5 |  |  |  |
|  | 9 | 8 |  |  |  |  | 6 |  |
| 8 |  |  |  | 6 |  |  |  | 3 |
| 4 |  |  | 8 |  | 3 |  |  | 1 |
| 7 |  |  |  | 2 |  |  |  | 6 |
|  | 6 |  |  |  |  |  |  |  |
|  |  |  | 4 | 1 | 9 |  |  | 5 |
|  |  |  |  | 8 |  |  | 7 | 9 |


| 5 | 3 | 4 | 6 | 7 | 8 | 9 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
| 1 | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 | 2 | 4 | 8 | 5 | 6 |
| 9 | 6 | 1 | 5 | 3 | 7 | 2 | 8 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 6 | 1 | 7 | 9 |

## Every $3 \times 3$ box contains the numbers 1 to 9

| 5 | 3 |  |  | 7 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 |  |  | 1 | 9 | 5 |  |  |  |
|  | 9 | 8 |  |  |  |  | 6 |  |
| 8 |  |  |  | 6 |  |  |  | 3 |
| 4 |  |  | 8 |  | 3 |  |  | 1 |
| 7 |  |  |  | 2 |  |  |  | 6 |
|  | 6 |  |  |  |  |  |  |  |
|  |  |  | 4 | 1 | 9 |  |  | 5 |
|  |  |  |  | 8 |  |  | 7 | 9 |


| 5 | 3 | 4 | 6 | 7 | 8 | 9 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
| 1 | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 | 2 | 4 | 8 | 5 | 6 |
| 9 | 6 | 1 | 5 | 3 | 7 | 2 | 8 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 6 | 1 | 7 | 9 |

## Checking Whether a Solution Is Correct

| 5 | 3 |  |  | 7 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 |  |  | 1 | 9 | 5 |  |  |  |
|  | 9 | 8 |  |  |  |  | 6 |  |
| 8 |  |  |  | 6 |  |  |  | 3 |
| 4 |  |  | 8 |  | 3 |  |  | 1 |
| 7 |  |  |  | 2 |  |  |  | 6 |
|  | 6 |  |  |  |  |  |  |  |
|  |  |  | 4 | 1 | 9 |  |  | 5 |
|  |  |  |  | 8 |  |  | 7 | 9 |


| 5 | 3 | 4 | 6 | 7 | 8 | 9 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
| 1 | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 | 2 | 4 | 8 | 5 | 6 |
| 9 | 6 | 1 | 5 | 3 | 7 | 2 | 8 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 6 | 1 | 7 | 9 |

## PassTwoDimensionalArray

## Processing Two-Dimensional Arrays

See the examples in the text.

1. (Initializing arrays with input values)
2. (Printing arrays)
3. (Summing all elements)
4. (Summing all elements by column)
5. (Which row has the largest sum)
6. (Finding the smallest index of the largest element)
7. (Random shuffling)
