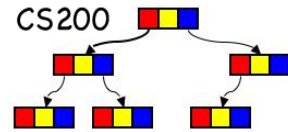


# CS200: Stacks

- Prichard Ch. 7

# Linear, **time**-ordered structures

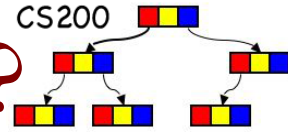


- Two data structures that reflect a **temporal** relationship
  - order of removal based on order of insertion
- We will consider:
  - “first come, first serve”
    - first in first out - FIFO (queue)
  - “take from the top of the pile”
    - last in first out - LIFO (stack)

Stacks or queues?

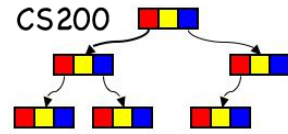


# What can we do with coin dispenser?

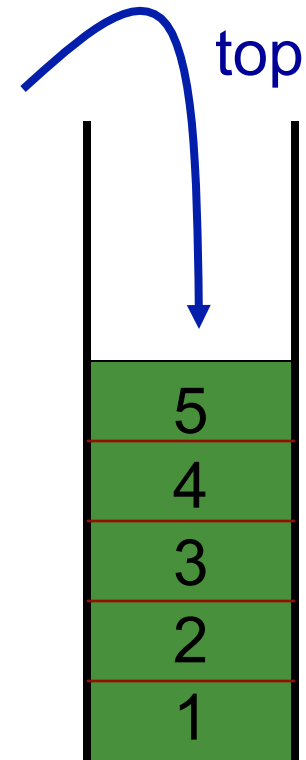


- “**push**” a coin into the dispenser.
- “**pop**” a coin from the dispenser.
- “**peek**” at the coin on top, but don’t pop it.
- “**isEmpty**” check whether this dispenser is empty or not.

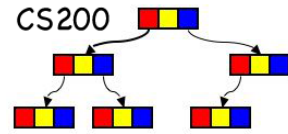
# Stacks



- Last In First Out (LIFO) structure
  - A stack of dishes in a café
  - A stack of quarters in a coin dispenser
- Add/Remove done from **same end**: the top

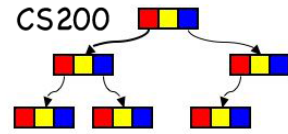


# Possible Stack Operations



- **isEmpty()**: determine whether stack is empty
- **push()**: add a new item to the stack
- **pop()**: remove the item added most recently
- **peek()**: retrieve, but don't remove, the item added most recently
  
- What would we call a collection of these ops?

# Checking for balanced braces



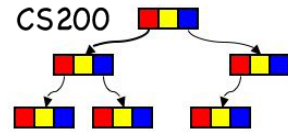
- How can we use a stack to determine whether the braces in a string are **balanced**?

abc { defg { ijk } { l { mn } } op } qr

abc { def } } { ghij { kl } m

**Can you define balanced?**

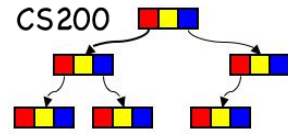
# Pseudocode



```
while ( not at the end of the string){
    if (the next character is a "{"){
        aStack.push("{")
    }
    else if (the character is a "}") {
        if(aStack.isEmpty()) ERROR!!!
        else aStack.pop()
    }
}
if(!aStack.isEmpty()) ERROR!!!
```



# question



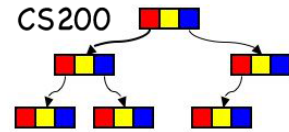
- Could you use a single int to do the same job?
- How?

Try it on

`abc { defg { ijk } { l { mn } } op } qr { st { uvw } xyz }`

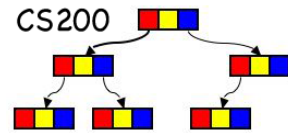
`abc { def } } { ghij { kl } m`

# Expressions



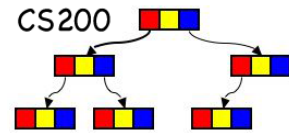
- Types of Algebraic Expressions
  - Prefix
  - Postfix
  - Infix
- Prefix and postfix are easier to parse. No ambiguity. Infix requires extra rules: **precedence** and **associativity**. **What are these?**
- Postfix: operator applies to the operands that immediately precede it.
- Examples:
  1.  $- 5 * 4 3$
  2.  $5 - 4 * 3$
  3.  $5 4 3 * -$





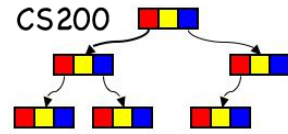
What type of expression is “5 4 3 – \*”?

- A. Prefix
- B. Infix
- C. Postfix
- D. None of the above (i.e., illegal)



What is the infix form of “5 4 3 – \*”?

# Evaluating a Postfix Expression



while there are input tokens left

    read the next token

    if the token is a value

        push it onto the stack.

    else

        //the token is a operator taking n arguments

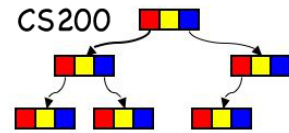
        pop the top n values from the stack and perform the operation

        push the result on the stack

If there is only one value in the stack return it as the result

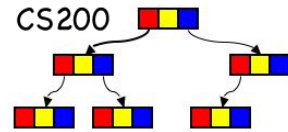
else

    throw an exception

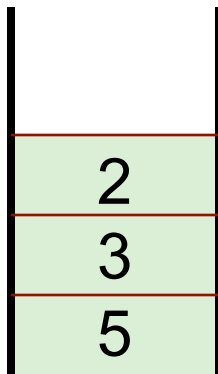


Draw Stacks to evaluate “5 4 3 – \*”?

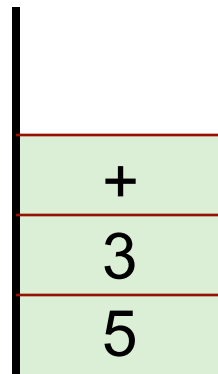
# Quick check



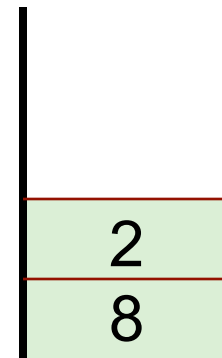
- If the input string is “5 3 + 2 \*”, which of the following could be what the stack looks like when trying to parse it?



A

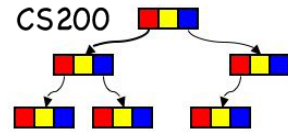


B



C

# Stack Interface



`push(StackItemType newItem)`

- adds a new item to the top of the stack

`StackItemType pop()` throws `StackException`

- deletes the item at the top of the stack and returns it
- Exception when deletion fails

`StackItemType peek()` throws `StackException`

- returns the top item from the stack, but does not remove it
- Exception when retrieval fails

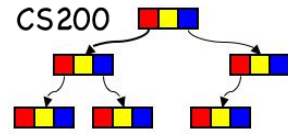
`boolean isEmpty()`

- returns true if stack empty, false otherwise

**Preconditions? Postconditions?**

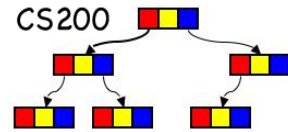


# Comparison of Implementations



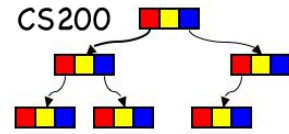
- Options for Implementation:
  - **Array** based implementation
  - **Array List** based implementation
  - **Linked List** based implementation
- What are the advantages and disadvantages of each implementation?
- Let's look at a Linked List based implementation
- In P1 you program an Array List based implementation

# Stacks and Recursion

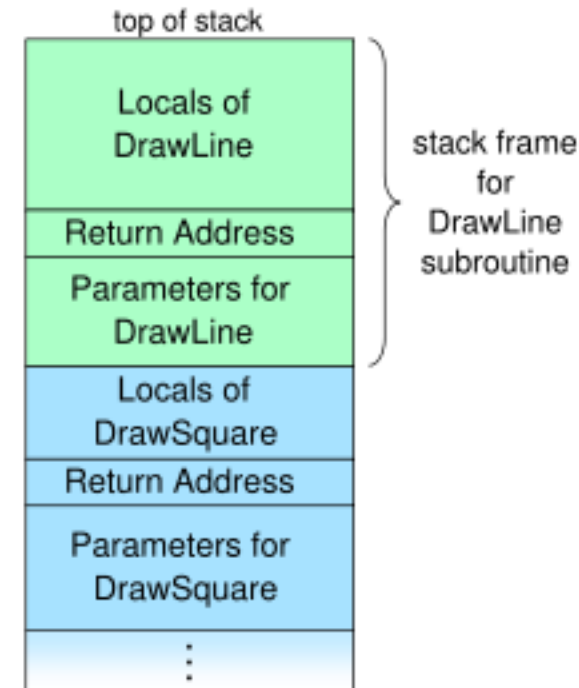


- Most implementations of recursion maintain a stack of activation records, called  
**the Run Time Stack**
- Activation records, or Stack Frames, contain parameters, local variables and return information of the method called
- The most recently executed activation record is stored at the top of the stack. So a call pushes a new activation record on the RT stack

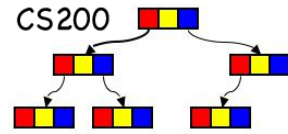
# Applications - the run-time stack



- Nested method calls tracked on **call stack** (aka run-time stack)
  - First method that returns is the last one invoked
- Element of call stack - **activation record or stack frame**
  - parameters
  - local variables
  - return address: pointer to next instruction to be executed in calling method

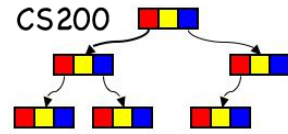


# Factorial example



```
int factorial(n){  
    // pre  $n \geq 0$   
    // post return  $n!$   
    if( $n == 0$ ) {  $r = 1$ ; return  $r$ ; }  
    else {  $r = n * factorial(n - 1)$ ; return  $r$ ; }  
}
```

# RTS factorial(3): wind phase



only active frame: **top of the run time stack**

**n=3, r=?**

**n=2, r=?**

n=3, r=?

**n=1, r=?**

n=2, r=?

n=3, r=?

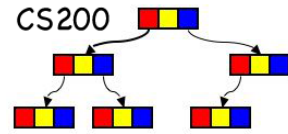
**n=0, r=1**

n=1, r=?

n=2, r=?

n=3, r=?

# RTS factorial(3): unwind phase



n=1, r=1

n=2, r=?

n=3, r=?

n=2, r=2

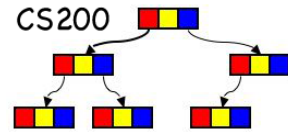
n=3, r=?

n=3, r=6

return 6

# More complex example:

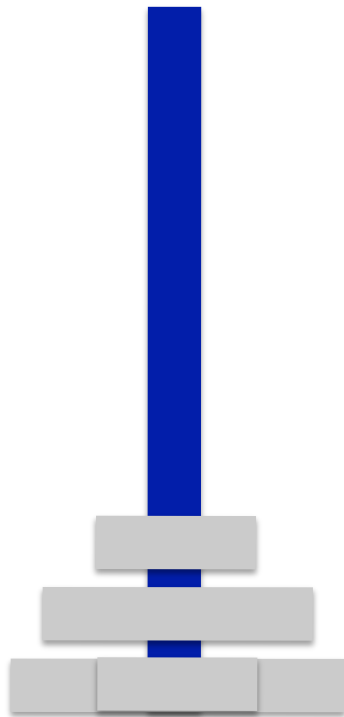
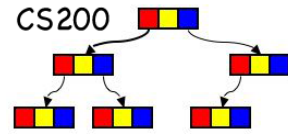
## The Towers of Hanoi



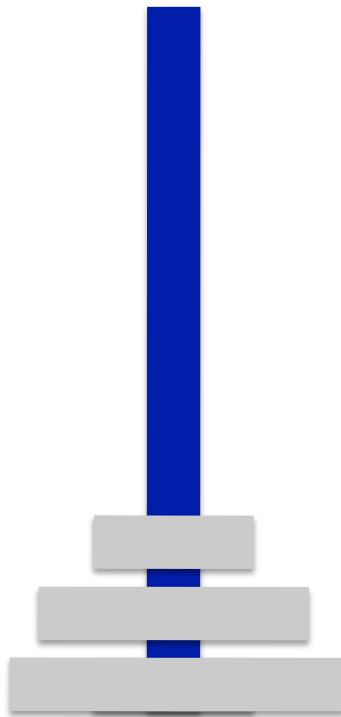
- **Move pile of disks from source to destination**
- **Only one** disk may be moved at a time.
- No disk may be placed on top of a smaller disk.



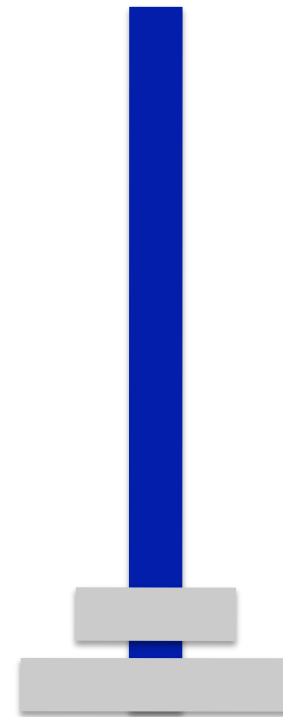
# Moves in the Towers of Hanoi



Source



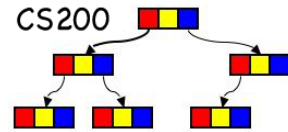
Destination



Spare



# Recursive Solution



// pegs are numbers, via is computed

// f: from: source peg, t: to: destination peg, v: via: intermediate peg

// state corresponds to return address, v is computed

```
public void hanoi(int n, int f, int t){
```

```
    if (n>0) {
```

```
        // state 0
```

```
        int v = 6 - f - t;
```

```
        hanoi(n-1,f, v);
```

```
        // state 1
```

```
        System.out.println("move disk " + n + " from " + f + " to " + t);
```

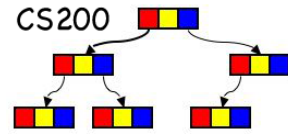
```
        hanoi(n-1,v,t);
```

```
        // state 2
```

```
    }
```

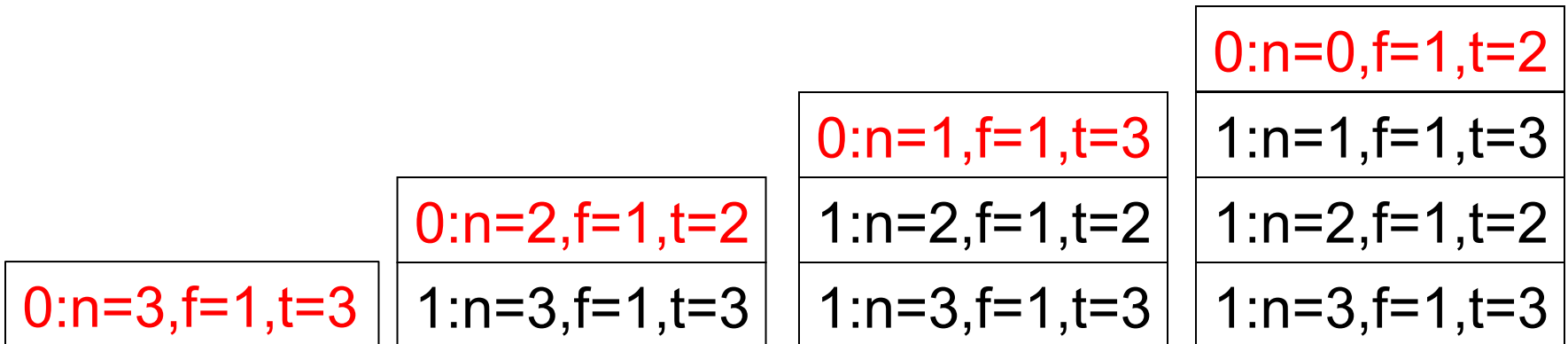
```
}
```

# Run time stack for hanoi(3,1,3)

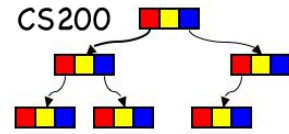


```
if (n>0) {  
    // state 0  
    int v = 6 - f - t;  
    hanoi(n-1,f, v);  
    // state 1  
    System.out.println("move disk " + n +  
        " from" + f + " to" + t);  
    hanoi(n-1,v,t);  
    // state 2  
}
```

only active frame:  
top of the run time stack



# Run time stack for hanoi(3,1,3)



```

if (n>0) {
  // state 0
  int v = 6 - f - t;
  hanoi(n-1,f, v);
  // state 1
  System.out.println("move disk " + n +
                    " from" + f + " to" + t);
  hanoi(n-1,v,t);
  // state 2
}

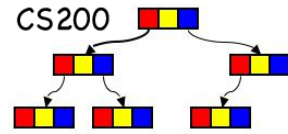
```

System.out:

“move disk 1 from 1 to 3”  
 “move disk 2 from 1 to 2”  
 etcetera

|               |               |               |               |
|---------------|---------------|---------------|---------------|
|               | 0:n=0,f=2,t=3 |               |               |
| 1:n=1,f=1,t=3 | 2:n=1,f=1,t=3 | 2:n=1,f=1,t=3 |               |
| 1:n=2,f=1,t=2 | 1:n=2,f=1,t=2 | 1:n=2,f=1,t=2 | 1:n=2,f=1,t=2 |
| 1:n=3,f=1,t=3 | 1:n=3,f=1,t=3 | 1:n=3,f=1,t=3 | 1:n=3,f=1,t=3 |

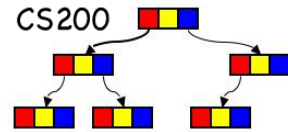
# Hanoi with explicit run time stack



- In Programming Assignment 1 you will create a Hanoi program with an explicit run time stack *rts*.
- The main loop of the program is:

```
while(rts not empty){  
  pop frame  
  check frame state  
  perform appropriate actions, including pushing frames  
}
```

# While loop:



Hanoi using an explicit Run Time Stack *rts*

Assume initially there is one Frame  $[state, n, from, to]$  on *rts*

Keep popping frames until *rts* is empty

When popping a frame:

if  $n == 0$  do nothing (discard frame)

else if frame in state 0:

    // do first call  $hanoi(n-1, from, via)$ :

        pushing  $[1, n, from, to]$  and push  $[0, n-1, from, via]$

else if in state 1:

    print disk  $n$  move

    //do second call  $hanoi(0, n-1, via, to)$

    push  $[2, n, from, to]$  and push  $[0, n-1, via, to]$

else (in state 2):

    do nothing