

CS 250: FOUNDATIONS OF COMPUTER SYSTEMS [BINARY REPRESENTATIONS & OPERATIONS]

Powering up with Binary

All you have is a 0 and 1
But the fun's just begun

Simpler math operations

Multiplications simple as additions

Representing numbers on both sides of zero
Using two's complement, our unsung hero

SHRIDEEP PALICKARA

Computer Science

Colorado State University

COMPUTER SCIENCE DEPARTMENT



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Frequently asked questions from the previous class survey

- Registers and caches?
- Let's say we have a binary number: 10100; why do we say we signify it as 0b10100 or 10100₂? Can't we tell it is binary by just looking at it?
 - Does the hardware use this 0b prefix or the base₂ subscript?
- More easy ways to calculate the binary value? Besides the one where all n bits are 1 (i.e., $2^n - 1$) or only one of the bits is 1
- What is a logic circuit?
- Will we get to the bit-iness of operating systems? E.g., some operating systems are 64-bits
- Is binary used anywhere? For programmers?
- When will you tell us which problem you will choose for the coding exam?
- If signals are used, how is it that a number can be detected?



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CS250 Submissions so far: As of 2:00 pm MT 1/27

Name	Status	Total Submissions	Last Submission Status	Last Submission Date
01 - Hello World	On	220	Green	1/27/2026, 1:21:37 PM
02 - Types, Operators	On	167	Green	1/27/2026, 1:08:03 PM
03 - IO, Random	On	126	Green	1/27/2026, 12:54:18 PM
04 - Strings	On	60	Green	1/27/2026, 10:20:21 AM
05 - Conditionals	On	40	Green	1/26/2026, 2:57:43 PM
06 - Arrays	On	13	Green	1/27/2026, 1:19:52 PM
07 - Loops	On	4	Green	1/25/2026, 9:24:45 PM
08 - Exceptions	On	6	Green	1/27/2026, 12:59:22 PM
09 - Methods	On	—	—	—
10 - Classes	On	—	—	—
Working with numbering systems, bitwise operations, and common binary operations	On	49	Green	1/27/2026, 11:24:39 AM



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Topics covered in this lecture

- Binary Representations
 - Properties of binary numbers
 - Operations on binary numbers
- Decimal to Binary
- Integers and word size implications
- Signed numbers



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Properties of binary numbers

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- Multiplying two n -bit binary values together may require *as many as* $2 \times n$ bits to hold the result
 - Biggest n -digit decimal number is $10^n - 1$ (e.g., for $n = 3$, it's 999). Worst case: $(10^n - 1)^2 < 10^{2n}$. For e.g.: $999 \times 999 = 998001 \rightarrow 6 \text{ digits} = 2 \times 3$
 - Binary version is the same story with base 2: max n -bit value is $2^n - 1$. And, $(2^n - 1)^2 < 2^{2n}$ so you may need up to $2n$ bits
- Adding or subtracting two n -bit binary values never requires more than $n + 1$ bits to hold the result



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Properties of binary numbers

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- Incrementing (adding 1 to) the largest unsigned binary value for a given number of bits always produces a value of 0
 - $0b11111111 = 0b00000000$ (the last carryover of 1 **overflows**)
- Decrementing (subtracting 1 from) 0 always produces the largest unsigned binary value for a given number of bits



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Number of unique combinations in a byte?

- Another way to think about this question is how many unique combinations of 0s and 1s can we make with our 8 bits?
- Let's first illustrate this with 4-bits



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16 unique combinations of 0s and 1s in a 4-bit number,
ranging in decimal value from 0 to 15

- We could determine the largest possible number that 4 bits can represent by setting all the bits to one, giving us **0b1111**
 - That is 15 in decimal
- If we add 1 to account for representing 0, then we come to our total of 16

Binary	Decimal
0000	0
0001	1
0010	2
0011	3
0100	4
0101	5
0110	6
0111	7
1000	8
1001	9
1010	10
1011	11
1100	12
1101	13
1110	14
1111	15



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Properties of binary numbers

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- In general, for n bits
 - The total number of unique combinations: 2^n
 - The largest possible number is $2^n - 1$



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Conversion from decimal to binary

- The binary number is constructed from **right to left**
- Step 1: Divide the decimal number by 2 and note down the remainder
- Step 2: Divide the obtained **quotient** by 2, and note remainder again
- Step 3: Repeat the above steps until you get **0** as the quotient
- **Stopping criteria**



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Example: Decimal number 23

- $23 \div 2 = 11$ (Remainder 1)
- $11 \div 2 = 5$ (Remainder 1)
- $5 \div 2 = 2$ (Remainder 1)
- $2 \div 2 = 1$ (Remainder 0)
- $1 \div 2 = 0$ (Remainder 1)

□ Binary Representation: **10111**

□ $2^4 + 2^2 + 2^1 + 2^0 = 16 + 4 + 2 + 1 = 23$

Top to Bottom
is
Right to Left
{LSB to MSB}



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Example: Decimal number 99

- $99 \div 2 = 49$ (Remainder 1)
- $49 \div 2 = 24$ (Remainder 1)
- $24 \div 2 = 12$ (Remainder 0)
- $12 \div 2 = 6$ (Remainder 0)
- $6 \div 2 = 3$ (Remainder 0)
- $3 \div 2 = 1$ (Remainder 1)
- $1 \div 2 = 0$ (Remainder 1)

Top to Bottom
is
Right to Left
{LSB to MSB}

□ Binary Representation: **1100011**

□ $2^6 + 2^5 + 2^1 + 2^0 = 64 + 32 + 2 + 1 = 99$



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PREFIXES FOR LARGE COLLECTIONS

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Prefixes

- To more easily communicate the size of data, we use **prefixes** like giga- and mega-
- The International System of Units (SI), also known as the **metric system**, defines a set of standard prefixes
- These prefixes are used to describe anything that can be quantified, *not just bits*



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Common SI Prefixes

Prefix name	Prefix symbol	Base-10 value	English word
Peta	P	10^{15}	quadrillion
Tera	T	10^{12}	trillion
Giga	G	10^9	billion
Mega	M	10^6	million
Kilo	K	10^3	thousand
centi	c	10^{-2}	hundredth
milli	m	10^{-3}	thousandth
micro	μ	10^{-6}	millionth
nano	n	10^{-9}	billionth
pico	p	10^{-12}	trillionth

These prefixes are used to describe anything that can be quantified, not just bits.



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When dealing with bytes, most software is actually working in base 2, not base 10

- If your computer tells you that a file is 1MB in size, it is actually 1,048,576 bytes!
 - That is approximately one million, but not quite

Prefix name	Prefix symbol	Value	Base 2
Peta	P	1,125,899,906,842,624	2^{50}
Tera	T	1,099,511,627,776	2^{40}
Giga	G	1,073,741,824	2^{30}
Mega	M	1,048,576	2^{20}
Kilo	K	1024	2^{10}



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A closer look at K ... myriad other places where it crops up!

- "K" can mean one kilometer
- A thousand monetary units
- 1024 bytes
- A strikeout in baseball
- A degree on the Kelvin temperature scale
- The nation of Korea (as in "K-pop")
- The chemical potassium
- A measure of the fineness of gold (karat)
- The drug ketamine
- Kindergarten (as in "K-12")
- The king in a chess move (as in "Kd2")
- The shape of a kind of economic recovery
- A protagonist in Franz Kafka's novels

This particular slide will not be on any Quiz or Exam!



"I've been feeling a lot of work related stress."



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Addition

- A pair of binary numbers can be added **bitwise from right to left**
 - Using the same decimal addition algorithm learned in elementary school
- First, we add the two rightmost bits, also called the least significant bits (LSB) of the two binary numbers
 - Next, add the resulting **carry** bit to the sum of the next pair of bits
- Continue this lockstep process **until** the two left most significant bits (MSB) are added



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Adding binary numbers: Rules

- $0 + 0 = 0$
- $0 + 1 = 1$
- $1 + 0 = 1$
- $1 + 1 = 0$ with **carry**
- $\text{Carry} + 0 + 0 = 1$
- $\text{Carry} + 0 + 1 = 0$ with carry
- $\text{Carry} + 1 + 0 = 0$ with carry
- $\text{Carry} + 1 + 1 = 1$ with carry



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Examples: Binary Addition

	0	0	0	1	
# 9		1	0	0	1
# 5		0	1	0	1
	0	1	1	1	0

No Overflow

CARRY

1	1	1	1	
	1	0	1	1
	0	1	1	1
1	0	0	1	0

Overflow

Addition of 9 and 5 = $8 + 4 + 2 = 14$

Addition of 11 and 7 = $10010_2 = 18$ (no truncation)
Addition of 11 and 7 = $0010_2 = 2$ (with truncation to 4-bits)



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Subtracting binary numbers: Rules

- $0 - 0 = 0$
- $0 - 1 = 1$ with a borrow
- $1 - 0 = 1$
- $1 - 1 = 0$



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Subtraction: An example

	0	b		
# 5	0	1	0	1
# 3	0	0	1	1
	0	0	1	0

Borrow



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Multiplication of binary numbers: Rules

- $0 \times 0 = 0$
- $0 \times 1 = 0$
- $1 \times 0 = 0$
- $1 \times 1 = 1$



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Multiplication: An example

		1	0	1	0	#10
		0	1	0	1	# 5
		1	0	1	0	1×1010
						0×1010
		1	0	1	0	1×1010
	1	1	0	0	1	0

Decimal representations:
 10×5

$$0b110010 = \\ 32 + 16 + 2 = 50$$



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Division: An example

- $3456 \div 12 = 288$
- How? Let's take a look at a long-division example



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Division in binary

- The basic algorithm is easier in binary because
 - At each step you don't have to guess how many times 12 goes into the remainder or multiply 12 by your guess to obtain the amount to subtract
 - At each step in the binary algorithm, **the divisor goes into the remainder exactly zero or one times**
- Let's take a look at: $0b11011 \div 0b11 = 0b1001$
 - $27 \div 3 = 9$



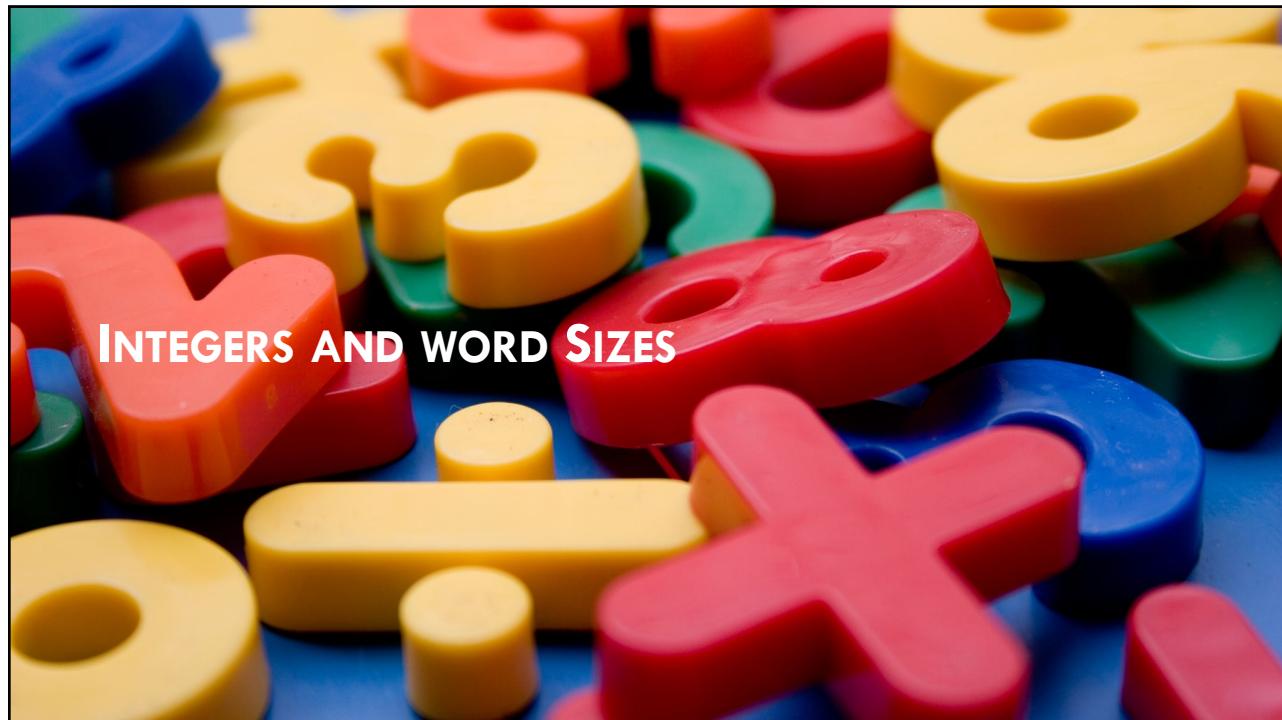
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Integer numbers are, of course, unbounded

- For any given number x :
 - There are integers that are less than x and integers that are greater than x
- Yet computers are *finite machines* that use a **fixed word size** for representing numbers
- **Word size** is a common hardware term used for specifying number of bits that computers use
 - For representing a **basic chunk of information**: in this case, integer values
 - Typically, 8-, 16-, 32-, or 64-bit registers are used for representing integers



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Word size implications

- The **fixed word size** implies that there is a **limit** on the number of values that these registers can represent
- For example, suppose we use 8-bit registers for representing integers
 - This representation can code $2^8 = 256$ different things
 - If we wish to represent only nonnegative integers?
 - We can assign 00000000 for representing 0,
 - 00000001 for representing 1,
 - 00000010 for representing 2, 00000011 for representing 3,
 - All the way up to assigning 11111111 for representing 255



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Word size implications

- In general, using n bits we can represent all the nonnegative integers ranging from 0 to $2^n - 1$
 - What about representing negative numbers using binary codes? Soon ...



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Representing numbers that are $>$ maximal, or $<$ minimal, values permitted by the fixed register size

- Every high-level language provides abstractions for handling numbers that are **as large or as small** as we can practically want
 - For e.g., `java.math.BigInteger` ($-2^{\text{Integer.MAX_VALUE}} \dots +2^{\text{Integer.MAX_VALUE}}$)
 - $\text{Integer.MAX_VALUE} = 2^{31} - 1 = 2,147,483,647$
- These abstractions are typically implemented by **lashing together** as many n -bit registers as necessary for representing the numbers
- Since executing arithmetic and logical operations on multi-word numbers is a **slow affair**
 - It is recommended to use this practice only when the application requires processing extremely large or extremely small numbers



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There's a sign on the wall, but she wants to be sure
'Cause you know sometimes words have two meanings
Stairway to Heaven, Jimmy Page / Robert Plant; Led Zeppelin

SIGNED NUMBERS



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Signed Numbers

- An n-bit binary system can code 2^n different things
- If we have to represent **signed** (+ and -) numbers in binary code, a solution is to split the available space into **two subsets**
 - One for representing nonnegative (+) numbers, and
 - The other for representing negative (-) numbers



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Desirable properties of signed number representations

- Ideally, the coding scheme should be chosen such that the introduction of signed numbers
 - Complicates the hardware implementation of arithmetic operations **as little as possible**
- This challenge has led to the development of several coding schemes for representing signed numbers in binary code



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The solution used today in almost all computers?

- **Two's complement** method, also known as *radix complement*
- Example:
 - Consider a binary system that uses a word size of n bits
 - The two's complement binary code that represents negative x is taken to be the code that represents $2^n - x$
 - Representation of $-x \rightarrow 2^n - x$



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Two's complement representation of 4-bit numbers

- Recall, in a n -bit number system
- $-x \rightarrow 2^n - x$
- For example, in a 4-bit binary system:
 - -7 is represented using the binary code associated with $2^4 - 7 = 9$
 - Which happens to be 1001

4-bit binary	Base-10	Derivation
0000	0	
0001	1	
0010	2	
0011	3	
0100	4	
0101	5	
0110	6	
0111	7	
1000	-8	$2^4 - 8 = 16 - 8 = 8$
1001	-7	$2^4 - 7 = 16 - 7 = 9$
1010	-6	$2^4 - 6 = 16 - 6 = 10$
1011	-5	$2^4 - 5 = 16 - 5 = 11$
1100	-4	$2^4 - 4 = 16 - 4 = 12$
1101	-3	$2^4 - 3 = 16 - 3 = 13$
1110	-2	$2^4 - 2 = 16 - 2 = 14$
1111	-1	$2^4 - 1 = 16 - 1 = 15$



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Let's take a closer look at $+7$ and -7

- $+7 = 0111$
- $-7 = 1001$
- $+7 - 7 = 0000$ (ignoring the overflow bit)



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An n -bit binary system with two's complement representation has attractive properties

- The system codes 2^n signed numbers, ranging from -2^{n-1} to $(2^{n-1} - 1)$
- The code of any **nonnegative** number begins with a **0**
- The code of any **negative** number begins with a **1**
- To obtain the binary code of $-x$ from the binary code of x ?
 - **Flip all the bits of x and add 1 to the result**

0000	0	
0001	1	
0010	2	
0011	3	
0100	4	
0101	5	
0110	6	
0111	7	
1000	-8	(16-8)
1001	-7	(16-7)
1010	-6	(16-6)
1011	-5	(16-5)
1100	-4	(16-4)
1101	-3	(16-3)
1110	-2	(16-2)
1111	-1	(16-1)



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Two's complement: binary code of $-x$ from the binary code of x ?

- Flip all the bits of x and add 1 to the result

4-bit binary	Base-10	Flip the bits	Add 1	Base-10
0001	1	1110	1111	-1
0010	2	1101	1110	-2
0011	3	1100	1101	-3
0100	4	1011	1100	-4
0101	5	1010	1011	-5
0110	6	1001	1010	-6
0111	7	1000	1001	-7
1000	8	0111	1000	-8

0000	0	
0001	1	
0010	2	
0011	3	
0100	4	
0101	5	
0110	6	
0111	7	
1000	-8	(16-8)
1001	-7	(16-7)
1010	-6	(16-6)
1011	-5	(16-5)
1100	-4	(16-4)
1101	-3	(16-3)
1110	-2	(16-2)
1111	-1	(16-1)



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Another attractive feature of two's complement

- Subtraction is handled as a special case of addition
- To illustrate, consider 5–7 in our 4-bit binary number system
 - This $5 + (-7)$
 - $0101 + 1001$
 - $= 1110$
 - Which is -2



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Implications of the two's complement method? [1/2]

- The two's complement method enables adding and subtracting signed numbers
 - Using nothing more than the hardware required for adding positive numbers!
- Every arithmetic operation, from multiplication to division to square root, can be implemented reductively using binary addition



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Implications of the two's complement method? [2/2]

- A huge range of computer capabilities rides on top of binary addition
- The two's complement method *obviates the need for special hardware* for adding and subtracting signed numbers
- The two's complement method is one of the most **remarkable and unsung** heroes of applied computer science



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ONE'S COMPLEMENT

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Another useful concept to know ... one's complement

- A *not so successful* attempt to represent signed numbers
- Get to negative numbers by taking positive numbers and flipping all the bits (i.e., 1 becomes 0 and 0 becomes 1)



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One's complement

- Flipping each bit of 0111 (+7) yields 1000 (-7)
- Has **two** different representations for zero

Sign	2^2	2^1	2^0	Decimal
0	1	1	1	+7
0	1	1	0	+6
0	1	0	1	+5
0	1	0	0	+4
0	0	1	1	+3
0	0	1	0	+2
0	0	0	1	+1
0	0	0	0	+0
1	1	1	0	-1
1	1	0	1	-2
1	1	0	0	-3
1	0	1	1	-4
1	0	1	0	-5
1	0	0	1	-6
1	0	0	0	-7



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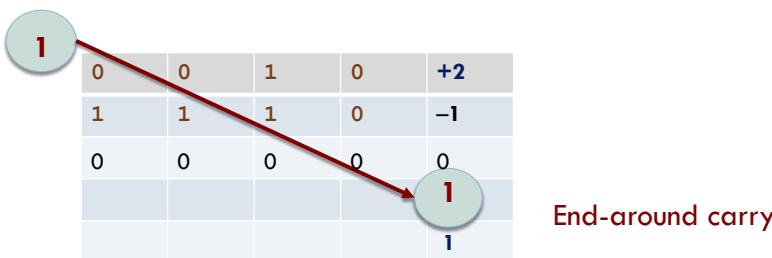
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One's complement: Addition is a little more complicated



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The contents of this slide-set are based on the following references

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- Jonathan E. Steinhart. *The Secret Life of Programs: Understand Computers -- Craft Better Code*. ISBN-10 / ISBN-13 : 1593279701 / 978-1593279707. No Starch Press. [Chapter 1]
- Randall Hyde. *Write Great Code, Volume 1*, 2nd Edition: Understanding the Machine 2nd Edition. ASIN: B07VSC1K8Z. No Starch Press. 2020. [Chapter 2]
- Matthew Justice. *How Computers Really Work: A Hands-On Guide to the Inner Workings of the Machine*. ISBN-10/ISBN-13 : 1718500661 / 978-1718500662. No Starch Press. 2020. [Chapter 1]



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