

Name: _____

Date: _____

CS270 Recitation 2 **“Number Crunching”**

This recitation will help you prepare for the Homework Assignment 1.
The teaching assistant will go through examples of these problems, then you will do them.
Answers can be checked on the websites shown at the bottom of the assignment.

Goals

To understand data representation in a computer, including boolean, integer, floating point, and character values, and the associated logical and arithmetic operations.

Question 1 (10 points): What is the minimum number of bits required to represent the 365 days in a year? If you have exactly the minimum number of bits, how many bit patterns are unused?

Minimum number of bits: **9, since $2^9 = 512$**

Number of unused bit patterns: **147, since $512 - 365 = 147$**

Question 2 (10 points): What are the 12-bit binary and hexadecimal representations of the decimal value 1234?

Binary: **0b010011010010 = $1024 + 128 + 64 + 16 + 2 = 1234$**

Hexadecimal: **0x04d2**

Question 3 (10 points): What is the range of unsigned integers that can be stored using 6 bits? What is the range for signed integers represented in 1's and 2's complement, with the same number of bits?

Range of unsigned integers: **0 to 63**

Range of signed integers: **-31 to 31** (1's complement)

Range of signed integers: **-32 to 31** (2's complement)

Question 4 (10 points): Show the 2's complement addition of -32 plus 12, with both numbers in binary using 8 bits. Hint: make sure that the resulting binary number corresponds to the correct answer.

0b11100000 (-32) + 0b00001100 (12) = 0b11101100 (-20)

Question 5 (10 points): Show the 2's complement subtraction of 10 minus 8, with both numbers in binary using 8 bits. Hint: make sure that the resulting binary number corresponds to the correct answer.

0b00001010 (10) + 0b11111000 (-8) = 0b00000010 (2)

Question 6 (10 points): Show the results of the following bitwise operations (using the same number of bits as shown in each problem):

$$\text{NOT}(0b10101100) = \mathbf{0b01010011}$$

$$0b10000010 \text{ OR } 0b01110110 = \mathbf{0b11110110}$$

$$0b10000111 \text{ AND } 0b10111010 = \mathbf{0b10000010}$$

$$0b10001000 \text{ XOR } 0b01011111 = \mathbf{0b11010111}$$

$$\text{NOT}(0b11011110 \text{ XOR } 0b01100000) = \mathbf{0b01000001}$$

Question 7 (10 points): Show the results of the following bitwise operations:

$$\sim(0x3456 \& 0xDCBA) = 0x\mathbf{EBED}$$

$$(0xFF00 \wedge 0x2244) | 0x1357 = 0x\mathbf{DF57}$$

Question 8 (10 points): Find the decimal floating-point numbers from the following values (assuming IEEE 32-bit floating-point representation):

$$0x41420000 = \mathbf{12.125f}$$

$$0 \ 10000001 \ 101000000000000000000000 = \mathbf{6.50f}$$

Question 9 (10 points): Find the binary and hexadecimal numbers for the following floating-point values (assuming IEEE 32-bit floating-point representation):

$$3.375f = \mathbf{0x40580000}$$
 (hexadecimal)

$$12.25f = \mathbf{0b \ 0 \ 1000010 \ 100010000000000000000000}$$
 (binary)

Question 10 (10 points): Translate the following strings from characters into ASCII hexadecimal values and vice versa:

$$\text{"cs270"} = \mathbf{0x63 \ 0x73 \ 0x32 \ 0x37 \ 0x30}$$

$$0x42696E617279 = \text{"Binary"}$$

Website for ASCII conversion: www.branah.com/ascii-converter

Website for IEEE floating-point conversion: www.h-schmidt.net/FloatConverter

Website for two's complement math: www.planetcalc.com/747