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Chapter 17 Recursion

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What is Recursion?

- ◆ A **recursive function** is one that solves its task by **calling itself** on smaller pieces of data.
 - Similar to recurrence function in mathematics.
 - Like iteration -- can be used interchangeably; sometimes recursion results in a simpler solution.

Example: Running sum ($\sum_{i=1}^n i$)

<p>Mathematical Definition: $RunningSum(1) = 1$ $RunningSum(n) = n + RunningSum(n-1)$</p>	<p>Recursive Function:</p> <pre>int RunningSum(int n) { if (n == 1) return 1; else return n + RunningSum(n-1); }</pre>
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Executing RunningSum

```
res = RunningSum(4);
```

return value = 10 RunningSum(4)
 return 4 + RunningSum(3);
 return value = 6 RunningSum(3)
 return 3 + RunningSum(2);
 return value = 3 RunningSum(2)
 return 2 + RunningSum(1);
 return value = 1 RunningSum(1)
 return 1;

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High-Level Example: Binary Search

- ◆ Given a sorted set of exams, in alphabetical order, find the exam for a particular student.
 1. Look at the exam **halfway** through the pile.
 2. If it matches the name, we're done; if it does not match, then...
 - 3a. If the name is greater (alphabetically), then **search the upper half** of the stack.
 - 3b. If the name is less than the halfway point, then **search the lower half** of the stack.

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Binary Search: Pseudocode

- Pseudocode is a way to describe algorithms without completely coding them in C.

```

FindExam(studentName, start, end) {
    halfwayPoint = (end + start)/2;
    if (end < start)
        ExamNotFound(); /* exam not in stack */
    else if (studentName == NameOfExam(halfwayPoint))
        ExamFound(halfwayPoint); /* found exam! */
    else if (studentName < NameOfExam(halfwayPoint))
        /* search lower half */
        FindExam(studentName, start, halfwayPoint-1)
    else
        /* search upper half */
        FindExam(studentName, halfwayPoint + 1, end);
}
    
```

Detailed Example: Fibonacci Numbers

- Mathematical Definition:

$$f(n) = f(n - 1) + f(n - 2)$$

$$f(1) = 1$$

$$f(0) = 1$$
- In other words, the n-th Fibonacci number is the sum of the previous two Fibonacci numbers.

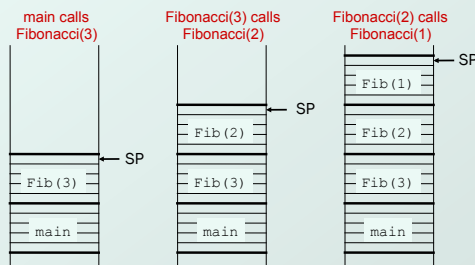
Fibonacci: C Code

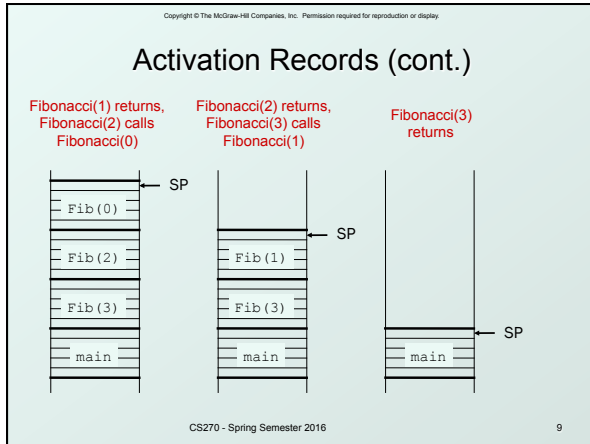
```

int Fibonacci(int n)
{
    if ((n == 0) || (n == 1))
        return 1;
    else
        return Fibonacci(n-1) + Fibonacci(n-2);
}
    
```

Activation Records

- Whenever Fibonacci is invoked, a new activation record is pushed onto the stack.





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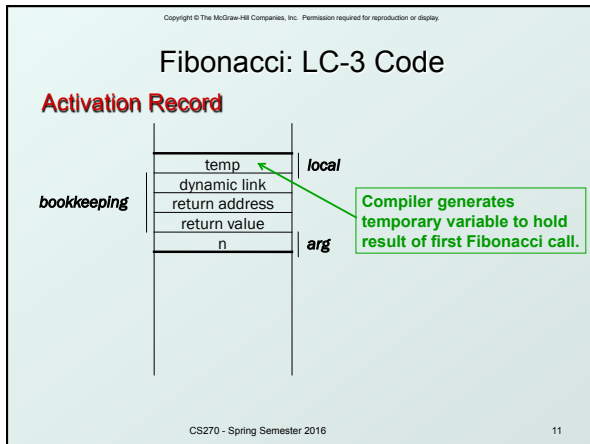
Tracing the Function Calls

- If we are debugging this program, we might want to trace all the calls of Fibonacci.
 - Note: A trace will also contain the arguments passed into the function.
- For Fibonacci(3), a trace looks like:


```

Fibonacci (3)
Fibonacci (2)
Fibonacci (1)
Fibonacci (0)
Fibonacci (1)
      
```
- What would trace of Fibonacci(4) look like?

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A Final C Example: Printing an Integer

- Recursively converts an unsigned integer as a string of ASCII characters.
 - If integer < 10, convert to char and print.
 - else, call self on first (n-1) digits and then print last digit.

```

void IntToAscii(int num) {
    int prefix, currDigit;
    if (num < 10)
        putchar(num + '0'); /* print number */
    else {
        prefix = num / 10; /* previous digits */
        digit = num % 10; /* current digit */
        IntToAscii(prefix); /* recursive call */
        putchar(digit + '0'); /* print digit */
    }
}
      
```

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Trace of IntToAscii

- Calling IntToAscii with parameter 12345:

```
IntToAscii (12345)
  IntToAscii (1234)
    IntToAscii (123)
      IntToAscii (12)
        IntToAscii (1)
          putchar ('1')
        putchar ('2')
      putchar ('3')
    putchar ('4')
  putchar ('5')
```