FAQ

• What is the meaning of life? [One answer video]
• What are resources? Drives, memory blocks, locks for critical sections, etc.
• Why modern OSs do not actively prevent deadlocks?
  – If a process does not progress for a few seconds, the system may generate a message. “.. not responding”
  – May be used by embedded/rear-time OSs,
  – data-bases, locked files may be checked for deadlocks
  – Some version of [Windows] and [Linux] may have capability to check for deadlocks involving locks for critical sections.
  – Use of mechanism by which locks are always acquired in a defined order
Methods for Handling Deadlocks

• Ensure that the system will *never* enter a deadlock state:
  – Deadlock prevention
    • ensuring that at least one of the 4 conditions cannot hold
  – Deadlock avoidance
    • Dynamically examines the resource-allocation state to ensure that there can never be a circular-wait condition

• Allow the system to enter a deadlock state
  – Detect and then recover. Hope is that it happens rarely.

• Ignore the problem and pretend that deadlocks never occur in the system; used by most operating systems, including UNIX.
Deadlock Prevention

For a deadlock to occur, each of the four necessary conditions must hold. By ensuring that at least one of these conditions cannot hold, we can prevent the occurrence of a deadlock.

**Mutual exclusion:** only one process at a time can use a resource

**Hold and wait:** a process holding at least one resource is waiting to acquire additional resources held by other processes

**No preemption:** a resource can be released only voluntarily by the process holding it, after that process has completed its task

**Circular wait:** there exists a set \( \{P_0, P_1, ..., P_n\} \) of waiting processes that are circularly waiting.
Deadlock Avoidance

Requires that the system has some additional *a priori* information available

- each process declares the *maximum number* of resources of each type that it may need
- *Resource-allocation state* is defined by the number of available and allocated resources, and the maximum demands of the processes
- The deadlock-avoidance algorithm dynamically examines the resource-allocation state to ensure that there can never be a circular-wait condition
  - Ensures all allocations result in a safe state
Safe Sequence

System must decide if immediate allocation leaves the system in a safe state

System is in **safe state** if there exists a sequence \(<P_1, P_2, \ldots, P_n>\) of ALL the processes such that

- for each \(P_i\), the resources that \(P_i\) can still request can be satisfied by
  - currently available resources +
  - resources held by all the \(P_j\), with \(j < i\)
  - That is
    - If \(P_i\) resource needs are not immediately available, then \(P_i\) can wait until all \(P_j\) have finished and released resources
    - When \(P_i\) terminates, \(P_{i+1}\) can obtain its needed resources, and so on
- If no such sequence exists: system state is **unsafe**
Example A: Assume **12 Units** in the system

<table>
<thead>
<tr>
<th></th>
<th>Max need (initially declared)</th>
<th>Current holding at time T0</th>
</tr>
</thead>
<tbody>
<tr>
<td>P0</td>
<td>10</td>
<td>5</td>
</tr>
<tr>
<td>P1</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>P2</td>
<td>9</td>
<td>2</td>
</tr>
</tbody>
</table>

At T0:
9 units allocated
12-9 = **3 units available**

A unit could be a drive, a block of memory etc.

• **Is the system in a safe state at time T0?**
  – Try sequence <P1, P0, P2>
  – P1 can be given 2 units
  – When P1 releases its resources; there are 5 units available
  – P0 uses 5 and subsequently releases them (10 available now)
  – P2 can then proceed.

• **Thus <P1, P0, P2> is a safe sequence, and at T0 system was in a safe state**
Avoidance Algorithms

- **Single instance** of a resource type
  - Use a resource-allocation graph scheme

- **Multiple instances** of a resource type
  - Use the banker’s algorithm (Dijkstra)
Resource-Allocation Graph Scheme

- **Claim edge** $P_i \rightarrow R_j$ indicated that process $P_i$ may request resource $R_j$; represented by a dashed line. This is new.

- Claim edge converts to request edge when a process requests a resource

- Request edge converted to an assignment edge when the resource is allocated to the process

- When a resource is released by a process, assignment edge reconverts to a claim edge

- Requirement: Resources must be claimed *a priori* in the system
Suppose $P_2$ requests $R_2$. Can $R_2$ be allocated to $P_2$? Although $R_2$ is currently free, we cannot allocate it to $P_2$, since this action will create a cycle getting system in an unsafe state. If $P_1$ requests $R_2$, and $P_2$ requests $R_1$, then a deadlock will occur.
Banker’s Algorithm: examining a request

- Multiple instances of resources.
- Each process must a priori claim maximum use.
- When a process requests a resource,
  - it may have to wait until the resource becomes available (resource request algorithm)
  - Request should not be granted if the resulting system state is unsafe (safety algorithm)
- When a process gets all its resources it must return them in a finite amount of time.
- Modeled after a banker in a small-town making loans.
Let $n =$ number of processes, and $m =$ number of resources types.

- **Available:** Vector of length $m$. If available $[j] = k$, there are $k$ instances of resource type $R_j$ available

**Processes vs resources:**

- **Max:** $n \times m$ matrix. If $Max[i,j] = k$, then process $P_i$ may request at most $k$ instances of resource type $R_j$

- **Allocation:** $n \times m$ matrix. If $Allocation[i,j] = k$ then $P_i$ is currently allocated $k$ instances of $R_j$

- **Need:** $n \times m$ matrix. If $Need[i,j] = k$, then $P_i$ may need $k$ more instances of $R_j$ to complete its task

\[ \text{Need} [i,j] = \text{Max}[i,j] – \text{Allocation} [i,j] \]
1. Let $Work$ and $Finish$ be vectors of length $m$ and $n$, respectively. Initialize:
   - $Work = \text{Initially Available resources}$
   - $Finish[i] = \text{initially false}$ for $i = 0, 1, \ldots, n-1$ (processes done)

2. Find a process $i$ such that both:
   - (a) $Finish[i] = false$
   - (b) $\text{Need}_i \leq Work$
   If no such $i$ exists, go to step 4

3. $Work = Work +\text{Allocation}_i$
   $Finish[i] = true$
   go to step 2

4. If $Finish[i] == true$ for all $i$, then the system is in a safe state
Resource-Request Algorithm for Process $P_i$

**Notation:** $Request_i = \text{request vector for process } P_i$.
If $Request_i[j] = k$ then process $P_i$ wants $k$ instances of resource type $R_j$.

**Algorithm:** Should the allocation request be granted?

1. If $Request_i \leq Need_i$ go to step 2. Otherwise, raise error condition, since process has exceeded its maximum claim.
2. If $Request_i \leq Available$, go to step 3. Otherwise $P_i$ must wait, since resources are not available.
3. **Is allocation safe?:** Pretend to allocate requested resources to $P_i$ by modifying the state as follows:
   
   - $Available = Available - Request_i$
   - $Allocation_i = Allocation_i + Request_i$
   - $Need_i = Need_i - Request_i$

   - If safe $\Rightarrow$ the resources are allocated to $P_i$
   - If unsafe $\Rightarrow P_i$ must wait, and the old resource-allocation state is preserved.
Example 1A: Banker’s Algorithm

- 5 processes $P_0$ through $P_4$;
- 3 resource types: $A$ (10 instances), $B$ (5 instances), and $C$ (7 instances);
- **Is it a safe state?**

<table>
<thead>
<tr>
<th>Process</th>
<th>Max</th>
<th>Allocation</th>
<th>Need</th>
</tr>
</thead>
<tbody>
<tr>
<td>type</td>
<td>A</td>
<td>B</td>
<td>C</td>
</tr>
<tr>
<td>Currently available</td>
<td>3</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>P0</td>
<td>7</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>P1</td>
<td>3</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>P2</td>
<td>9</td>
<td>0</td>
<td>2</td>
</tr>
<tr>
<td>P3</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>P4</td>
<td>4</td>
<td>3</td>
<td>3</td>
</tr>
</tbody>
</table>

The Need matrix is redundant.
Example 1A: Banker’s Algorithm

- Is it a safe state?
- Yes, since the sequence < P1, P3, P4, P2, P0> satisfies safety criteria

<table>
<thead>
<tr>
<th>Process</th>
<th>Max</th>
<th>Allocation</th>
<th>Need</th>
</tr>
</thead>
<tbody>
<tr>
<td>type</td>
<td>A</td>
<td>B</td>
<td>C</td>
</tr>
<tr>
<td>available</td>
<td>3</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>P0</td>
<td>7</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>P1</td>
<td>3</td>
<td>2</td>
<td>2</td>
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</tr>
<tr>
<td>P3</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>P4</td>
<td>4</td>
<td>3</td>
<td>3</td>
</tr>
</tbody>
</table>

P1 run to completion. Available becomes \([3 \ 3 \ 2]+[2 \ 0 \ 0] = [5 \ 3 \ 2]\)
P3 run to completion. Available becomes \([5 \ 3 \ 2]+[2 \ 1 \ 1] = [7 \ 4 \ 3]\)
P4 run to completion. Available becomes \([7 \ 4 \ 3]+[0 \ 0 \ 2] = [7 \ 4 \ 5]\)
P2 run to completion. Available becomes \([7 \ 4 \ 5]+[3 \ 0 \ 2] = [10 \ 4 \ 7]\)
P0 run to completion. Available becomes \([10 \ 4 \ 7]+[0 \ 1 \ 0] = [10 \ 5 \ 7]\)

Hence state above is safe.
Ex 1B: Assume now $P_1$ Requests (1,0,2)

- Check that $\text{Request}_i \leq \text{Need}_i$ and $\text{Request}_i \leq \text{Available}$. $(1,0,2) \leq (3,3,2) \rightarrow \text{true}.$
- Check for safety after pretend allocation. $P_1$ allocation would be $\begin{pmatrix} 2 & 0 & 0 \end{pmatrix} + \begin{pmatrix} 1 & 0 & 2 \end{pmatrix} = \begin{pmatrix} 3 & 0 & 2 \end{pmatrix}$

<table>
<thead>
<tr>
<th>Process</th>
<th>Max</th>
<th>Pretend Allocation</th>
<th>Need</th>
</tr>
</thead>
<tbody>
<tr>
<td>type</td>
<td>A</td>
<td>B</td>
<td>C</td>
</tr>
<tr>
<td>Available</td>
<td></td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>P0</td>
<td>7</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>P1</td>
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<td>2</td>
<td>2</td>
</tr>
<tr>
<td>P2</td>
<td>9</td>
<td>0</td>
<td>2</td>
</tr>
<tr>
<td>P3</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>P4</td>
<td>4</td>
<td>3</td>
<td>3</td>
</tr>
</tbody>
</table>

Sequence $< P_1, P_3, P_4, P_0, P_2 >$ satisfies safety requirement.

Hence state above is safe, thus the allocation would be safe.
Ex 1C,1D: Additional Requests ..

- Given State is (same as previous slide)

<table>
<thead>
<tr>
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<th>Max</th>
<th>Allocation</th>
<th>Need</th>
</tr>
</thead>
<tbody>
<tr>
<td>type</td>
<td>A</td>
<td>B</td>
<td>C</td>
</tr>
<tr>
<td>available</td>
<td></td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>P0</td>
<td>7</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>P1</td>
<td>3</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>P2</td>
<td>9</td>
<td>0</td>
<td>2</td>
</tr>
<tr>
<td>P3</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>P4</td>
<td>4</td>
<td>3</td>
<td>3</td>
</tr>
</tbody>
</table>

P4 request for (3,3,0): cannot be granted - resources are not available.
P0 request for (0,2,0): cannot be granted since the resulting state is unsafe.
Bankers Algorithm: Practical Issues

• Processes may not know in advance about their maximum resource needs
• Number of processes is not fixed
  – Varies dynamically
• Resources thought to be available can disappear
• Few systems use this algorithm
Deadlock Detection

- Allow system to enter deadlock state. If that happens, detect the deadlock and do something about it.

- Detection algorithm
  - Single instance of each resource:
    - wait-for graph
  - Multiple instances:
    - detection algorithm (based on Banker’s algorithm)

- Recovery scheme
• Maintain **wait-for graph** (based on resource allocation graph)
  – Nodes are processes
  – \( P_i \rightarrow P_j \) if \( P_i \) is waiting for \( P_j \)

  – **Deadlock if cycles**

• Periodically invoke an algorithm that searches for a cycle in the graph. If there is a cycle, there exists a deadlock

• An algorithm to detect a cycle in a graph requires an order of \( n^2 \) operations, where \( n \) is the number of vertices in the graph
Resource-Allocation Graph and Wait-for Graph

Has cycles. Deadlock.

(a) Resource-Allocation Graph

(b) Corresponding wait-for graph

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Banker’s algorithm: Can requests by all process be satisfied?

- **Available**: A vector of length $m$ indicates the number of available (currently free) resources of each type
- **Allocation**: An $n \times m$ matrix defines the number of resources of each type currently allocated to each process
- **Request**: An $n \times m$ matrix indicates the current request of each process. If $\text{Request}_{ij} = k$, then process $P_i$ is requesting $k$ more instances of resource type $R_j$. 
Detection Algorithm

1. Let \textbf{Work} and \textbf{Finish} be vectors of length \( m \) and \( n \), respectively. Initialize:
   (a) \textbf{Work} = initially available
   (b) For \( i = 1,2, ..., n \), if \text{Allocation}_i \neq 0, \text{ then Finish}[i] = false; otherwise, Finish[i] = true

2. Find an index \( i \) such that both:
   (a) Finish[i] == false
   (b) Request_i \leq Work
   If no such \( i \) exists, go to step 4

3. \textbf{Work} = \textbf{Work} + \text{Allocation}_i, Finish[i] = true
   go to step 2 (find next process)

4. If \text{Finish}[i] == false, for some \( i, \ 1 \leq i \leq n \), then the system is in deadlock state. Moreover, if \text{Finish}[i] == false, then \( P_i \) is deadlocked

Algorithm requires an order of \( O(m \times n^2) \) operations to detect whether the system is in deadlocked state
Example of Detection Algorithm

- Five processes $P_0$ through $P_4$; three resource types A (7 instances), B (2 instances), and C (6 instances)
- Sequence $<P_0, P_2, P_3, P_1, P_4>$ will result in $Finish[i] = true$ for all $i$. No deadlock

<table>
<thead>
<tr>
<th>Process</th>
<th>Allocation</th>
<th>Request</th>
</tr>
</thead>
<tbody>
<tr>
<td>type</td>
<td>A B C</td>
<td>A B C</td>
</tr>
<tr>
<td>available</td>
<td>0 0 0</td>
<td>A B C</td>
</tr>
<tr>
<td>P0</td>
<td>0 1 0</td>
<td>0 0 0</td>
</tr>
<tr>
<td>P1</td>
<td>2 0 0</td>
<td>2 0 2</td>
</tr>
<tr>
<td>P2</td>
<td>3 0 3</td>
<td>0 0 0</td>
</tr>
<tr>
<td>P3</td>
<td>2 1 1</td>
<td>1 0 0</td>
</tr>
<tr>
<td>P4</td>
<td>0 0 2</td>
<td>0 0 2</td>
</tr>
</tbody>
</table>

After work

<table>
<thead>
<tr>
<th>After</th>
<th>work</th>
</tr>
</thead>
<tbody>
<tr>
<td>ini</td>
<td>0 0 0</td>
</tr>
<tr>
<td>P0</td>
<td>0 1 0</td>
</tr>
<tr>
<td>P2</td>
<td>3 1 3</td>
</tr>
<tr>
<td>P3</td>
<td>5 2 4</td>
</tr>
<tr>
<td>P1</td>
<td>7 2 4</td>
</tr>
<tr>
<td>P4</td>
<td>7 2 6</td>
</tr>
</tbody>
</table>
Example of Detection Algorithm (cont)

- \( P_2 \) requests an additional instance of type \( C \)

<table>
<thead>
<tr>
<th>Process</th>
<th>Allocation</th>
<th>Request</th>
</tr>
</thead>
<tbody>
<tr>
<td>type</td>
<td>A  B  C</td>
<td>A  B  C</td>
</tr>
<tr>
<td>available</td>
<td>0 0 0</td>
<td></td>
</tr>
<tr>
<td>P0</td>
<td>0 1 0</td>
<td>0 0 0</td>
</tr>
<tr>
<td>P1</td>
<td>2 0 0</td>
<td>2 0 2</td>
</tr>
<tr>
<td>P2</td>
<td>3 0 3</td>
<td>0 0 1</td>
</tr>
<tr>
<td>P3</td>
<td>2 1 1</td>
<td>1 0 0</td>
</tr>
<tr>
<td>P4</td>
<td>0 0 2</td>
<td>0 0 2</td>
</tr>
</tbody>
</table>

State of system?
- Can reclaim resources held by process \( P_0 \), but insufficient resources to fulfill other processes’ requests
- Deadlock exists, consisting of processes \( P_1, P_2, P_3, \) and \( P_4 \)
- When, and how often, to invoke depends on:
  - How often a deadlock is likely to occur
  - How many processes will need to be rolled back
    - one for each disjoint cycle

- If detection algorithm is invoked arbitrarily, there may be many cycles in the resource graph and so we would not be able to tell which of the many deadlocked processes “caused” the deadlock.
Recovery from Deadlock: Process Termination

Choices

• Abort all deadlocked processes

• Abort one process at a time until the deadlock cycle is eliminated

In which order should we choose to abort?

1. Priority of the process
2. How long process has computed, and how much longer to completion
3. Resources the process has used
4. Resources process needs to complete
5. How many processes will need to be terminated
6. Is process interactive or batch?
Recovery from Deadlock: Resource Preemption

- **Selecting a victim** – minimize cost

- **Rollback** – return to some safe state, restart process for that state

- **Starvation** – same process may always be picked as victim, include number of rollbacks in cost factor
Deadlock recovery through rollbacks

- **Checkpoint** process periodically
  - Contains memory image and resource state

- Deadlock detection tells us *which* resources are needed

- Process owning a needed resource
  - **Rolled back** to before it acquired needed resource
    - Work done since rolled back checkpoint discarded
  - **Assign** resource to deadlocked process
Livelocks

In a livelock two processes need each other’s resource

- Both run and make no progress, but neither process blocks
- Use CPU quantum over and over without making progress

Ex: If fork fails because process table is full

- Wait for some time and try again
- But there could be a collection of processes each trying to do the same thing
- Avoided by ensuring that only one process (chosen randomly or by priority) takes action

Two people meet in a narrow corridor, and each tries to be polite by moving aside to let the other pass. But they end up swaying from side to side without making any progress because they both repeatedly move the same way at the same time.
Welcome to CS370 Second Half

• Topics: Memory, Storage, File System, Virtualization
• Class rules: See Syllabus
  – Class, Canvas, Teams
  – participation
  – Final
    • Sec 001, local 801: in class.
    • Sec 801 non-local: on-line.
    • SDC: Sec 001, Sec 801: must be taken at SDC
  – Project, deadlines, Plagiarism
Some OS History Lessons 1: UNIX

- History in Unix-like OSs
Some OS History Lessons 2: Windows

• 1974: CP/M Intel 8080, Gary Kildall, Digital Research
  – 8-bit, min 16 kB RAM, floppy
• 1980: 86-DOS, Intel 8086, Tim Paterson, Seattle Computer Products
  – Inspired by CP/M?
• 1981: PC DOS, Bill Gates, Microsoft
  – 86-DOS licensed for $25,000, hired Paterson
• 1985: Windows, Bill Gates, Microsoft
  – GUI inspired by MAC? Xerox PARC Star?

Gary Kildall net worth $1.9 Million at death
Tim Paterson Net Worth: $250,000
Main Memory

Slides based on
• Text by Silberschatz, Galvin, Gagne
• Various sources
Main Memory

Slides based on
- Text by Silberschatz, Galvin, Gagne
- Various sources
Chapter 8: Main Memory

Objectives:

• Organizing memory for multiprogramming environment
  • Partitioned vs separate address spaces
• Memory-management techniques
  • Virtual vs physical addresses
  • Chunks
    • segmentation
    • Paging: page tables, caching (“TLBs”)
• Examples: the Intel (old/new) and ARM architectures
What we want

- Memory capacities have been increasing
  - But programs are getting bigger faster
  - Parkinson’s Law*: Programs expand to fill the memory available to hold

- What we would like
  - Memory that is
    - infinitely large, infinitely fast
    - Non-volatile
    - Inexpensive too

- Unfortunately, no such memory exists as of now

*work expands so as to fill the time available for its completion. 1955
Background

- Program must be brought (from disk) into memory and run as a process
- Main memory and registers are only storage CPU can access directly
- Memory unit only sees a stream of
  - addresses + read requests, or
  - address + data and write requests
- n-bit address: address space of size $2^n$ bytes.
  - Ex: 32 bits: addresses 0 to $(2^{32} - 1)$ bytes
  - Addressable unit is always 1 byte.
- Access times:
  - Register access in one CPU clock (or less)
  - Main memory can take many cycles, causing a **stall**
  - **Cache** sits between main memory and CPU registers making main memory appear much faster
- **Protection** of memory required to ensure correct operation

$2^{10} = 1,024 \approx K$

$2^{20} = 1,048,576 \approx M$

$2^{30} \approx G$
Main memory and registers are only storage CPU can access directly access.

Register access in one CPU clock (or less).
Main memory can take many cycles, causing a stall.

Cache sits between main memory and CPU registers making main memory appear much faster.

Ch 11, 13, 14, 16: Disk, file system

Cache: CS470
Memory Technology

The History of Memory

In 1940 I invented a bit of memory.

1953: I invented a byte of memory.

1966: 1k

1978: 32k

2011: Look, 100 terabytes

2038: What memory?
Protection: Making sure each process has separate memory spaces

• OS must be protected from accesses by user processes
• User processes must be protected from one another
  – Determine range of legal addresses for each process
  – Ensure that process can access only those

• Approaches:
  – Partitioning address space (early system)
  – Separate address spaces (modern practice)
Partitioning: Base and Limit Registers

- Base and Limit for a process
  - **Base**: Smallest legal physical address
  - **Limit**: Size of the range of physical address
- A pair of **base** and **limit registers** define the logical address space for a process
- CPU must check every memory access generated in user mode to be sure it is between base and limit for that user
- Base: **Smallest** legal physical address
- Limit: Size of the **range** of physical address
- Eg: Base = 300040 and limit = 120900
- Legal: 300040 to \((300040 + 120900 -1) = 420939\)

Addresses: decimal, hex/binary
Hardware Address Protection

Legal addresses: **Base address** to **Base address + limit -1**
Multistep Processing of a User Program
Address Binding Questions

• Programs on disk, ready to be brought into memory to execute form an input queue
  – Without support, must be loaded into address 0000
• Inconvenient to have first user process physical address always at 0000
  – How can it not be?
• Addresses represented in different ways at different stages of a program’s life
  – Source code addresses are symbolic
  – Compiled code addresses bind to relocatable addresses
    • i.e., “14 bytes from beginning of this module”
  – Linker or loader will bind relocatable addresses to absolute addresses
    • i.e., 74014
  – Each binding maps one address space to another
• Address binding of instructions and data to memory addresses can happen at three different stages
  – **Compile time**: If memory location known a priori, **absolute code** can be generated; must recompile code if starting location changes
  – **Load time**: Must generate **relocatable code** if memory location is not known at compile time
  – **Execution time**: Binding delayed until run time if the process can be moved during its execution from one memory segment to another
    • Need hardware support for address maps (e.g., base and limit registers)
Separate Address Spaces

• Each process has its own private address space.
  – **Logical address space** is the set of all logical addresses used by a process.

• However, the physical memory has just one address space.
  – **Physical address space** is the set of all physical addresses

• Need to map one to the other.
Logical vs. Physical Address Space

- The concept of a logical address space that is bound to a separate **physical address space** is central to proper memory management
  - *Logical address* – generated by the CPU; also referred to as **virtual address**
  - *Physical address* – address seen by the memory unit
- **Logical address space** is the set of all logical addresses generated by a program
- **Physical address space** is the set of all physical addresses