Security Vulnerabilities: Risks

from Discovery to





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Outline

- Vulnerabilities and the society
- Risk as Likelihood x Impact product
- Conditional components of Likelihood
 Internal and External
- Vulnerability discovery in lifecycle
- CVSS as a risk measure
- Vulnerability markets
- Measuring impact

Magnitude of Security Risks



2019 Year End Data Breach QuickView Report

Exposed Records by Country

Ranking	# of Breaches	Country	Total Exposed	Records Average Records per Breach	Median Number of Records	Percentage of Exposed Records
1	27	China	3,822,021,911	141,556,367	11,748,417	52.01%
2	2330	UnitedStates	2,317,065,126	994,449	1,458	31.53%
3	16	Netherlands	711,794,171	44,487,136	4,021	9.69%
4	78	India	301,422,538	3,864,392	216	4.10%
5	11	SouthAfrica	67,023,831	6,093,076	6,700,000	0.91%
6	3	Philippines	55,245,020	13,811,255	-	0.75%
7	6	Argentina	28,741,292	4,790,215	2,516	0.39%
8	12	Republic Of Korea	17,372,292	1,447,691	1,000,000	0.24%
9	11	Israel	14,001,285	1,272,844	131	0.19%
10	1	Bermuda	13,400,000	13,400,000	-	0.18%

Data Breach QuickView Report: 2017 Data Breach Trends – Year In Review

Cost of security Incidents

Business Size	BusinessSize in \$	Million \$/incident
Small	<100 M	0.41
Medium	100 M to 1 B	1.3
Large	>1 B	5.9
National Economy		? (<u>Gingrich IP \$360B</u>) '16
National Security		? (<u>Stuxnet type attack</u> \$1T) '15
National Democracy		? (Clinton campaign: 1.2B, DNC) '16

Source: Global State of Information Security Survey 2015 (and others)

Cost of security Incidents



Cost of a data breach by country or region

Figure 10:

Average total cost of a data breach by industry Measured in US\$ millions



What's the Cost of a Data Breach in 2019? Chris Brook July 30, 2019

Objectives and Challenges

Coming up with

- a standard and comprehensive terminology
- and then develop models for risk components

Challenges

- There exist numerous measures of risk, most of them partial measures based on limited perspectives (network accessibility, attack surface, CVSS etc)
- Different measures of "cost"
- Data does not come from controlled experiments
 - Real life data
 - Limited data from diverse sources collected without mutual coordination
 - Need to reconcile apparent mismatch/contradictions

Extent of the problem: IoT



Risk as a composite measure

Formal definition:

Risk due to an adverse event e_i Risk_i = Likelihood_i x Impact_i Sometimes likelihood is split in two factors Likelihood_i = P{hole_i present}. P{exploitation|hole; present} A specific time-frame, perhaps a year, is presumed for the likelihood.

In classical risk literature, the internal component of Likelihood is termed "Vulnerability" and external "Threat". Both are probabilities. There the term "vulnerability" does not mean a security bug, as in computer security.

Likelihood & Impact scales

Quantitative or descriptive levels

- Number of levels may depend on resolution achievable
- Scale: Logarithmic, Linear or combined
- Risk = Likelihood x Impact
 - Log(Risk) = Log(Likelihood) + Log(Impact)
- If "Score" is proportional to Log value
 - Risk score = Likelihood score + Impact score
 - Adding scores valid if scores represent logarithmic values.
 - Example:
 - Likelihood = 10%, impact = \$100,000 ⇒ **Risk = \$10,000**
 - Scores: Log(0.10) = -1, log (100000) = 5 ⇒ Risk score = 4

Risk Matrix

- Likelihood and Impact divided into levels
 - Each level quantitatively/qualitatively defined
- Cells marked by the overall risk
 - Low, Medium, High, Extreme etc.
- Equal risk regions along the diagonal, valid provided score scales are logarithmic.

	Consequences						
Likelihood	Insignificant	Minor	Moderate	Major	Severe		
Almost certain	м	н	н	E	E		
Likely	м	м	н	н	E		
Possible	L	м	м	н	E		
Unlikely	L	М	м	м	н		
Rare	L	L	м	м	н		

LIKELIHOOD		C	ONSEQUENCE	S			
(probability) How likely is the event to occur at some time in the	What is the Se event act	What is the Severity of injuries /potential damages / financial impacts (if the risk event actually occurs)? (Logarithmic Scale, property industry specific matrix)					
(Linear Scale time specific matrix)	Insignificant	Minor	Moderate	Major	Catastrophic		
-j	No Injuries First Aid No Envir Damage << \$1,000 Damage	Some First Aid required Low Envir Damage << \$10,000 Damage	External Medical Medium Envir Damage <<\$100,000 Damage	Extensive injuries High Envir Damage <<\$1,000,000 Damage	Death or Major Injuries Toxic Envir Damage >>\$1,000,000 Damage		
Almost certain -	MODERATE	HIGH	HIGH	CRITICAL	CRITICAL		
expected in normal circumstances (100%)	RISK	RISK	RISK	RISK	RISK		
Likely –	MODERATE	MODERATE	HIGH	HIGH	CRITICAL		
probably occur in most circumstances (10%)	RISK	RISK	RISK	RISK	RISK		
Possible -	LOW	MODERATE	HIGH	HIGH	CRITICAL		
might occur at some time. (1%)	RISK	RISK	RISK	RISK	RISK		
<mark>Unlikely –</mark>	LOW	MODERATE	MODERATE	HIGH	HIGH		
could occur at some future time (0.1%)	RISK	RISK	RISK	RISK	RISK		
Rare -	LOW	LOW	MODERATE	MODERATE	HIGH		
Only in exceptional circumstances 0.01%)	RISK	RISK	RISK	RISK	RISK		

Security Holes: Types

- Software holes: Vulnerabilities
 - CVSS scores involving *exploitability* and *impact* is a type of risk measure.
- System/physical holes
- Personnel/Procedural holes:
 - e.g. Phishing
- Exploitation may involve multiple holes, perhaps of different types
- Classify them:
 - Target 2013 breach: credentials stolen from a HVAC contractor
 - Equifax 2017 breach: vulnerability patch not applied

Components of Likelihood of Exploitation

Internal

- Presence of a vulnerability (Vulnerability Discovery*)
- Vulnerability not patched

External

- Attacker's motivation level
- Technical capabilities, exploit availability*
- Network access to vulnerable system

Interface

- Attack surface* of vulnerable system
- Reachability* of vulnerability

Vulnerability Lifecycle

Vulnerabilities: "defect which enables an attacker to bypass security measures" [Schultz et al]



Exploit code ("exploit") : usually available after disclosure

Modeling Vulnerability Discovery

- Quantitative Vulnerability Assessment Alhazmi 2004-
- Discovery in Multi-Version Software Kim 2006,2007
- Seasonality in Vulnerability Discovery Joh 2008,2009

Motivation

- For defects: Reliability modeling and SRGMs have been around for decades.
- Assuming that vulnerabilities are special faults will lead us to this question:
 - To what degree reliability terms and models are applicable to vulnerabilities and security? [Littlewood et al].
 - The need for quantitative measurements and estimation is becoming more crucial.

Goal: Modeling Vulnerability Discovery

Developing a quantitative model to estimate vulnerability discovery.

- Using *calendar time*.
- Using equivalent effort.
- Validate these measurements and models.
 - Testing the models using available data
- Identify security Assessment metrics
 - Vulnerability density
 - Vulnerability to Total defect ratio

Time – vulnerability discovery model

What factors impact the discovery process?

- The changing environment
 - The share of installed base.
 - Global internet users.
- Discovery effort
 - Discoverers: Developer, White hats or black hats.
 - Discovery effort is proportional to the installed base over time.
 - Vulnerability finders' reward: greater rewards, higher motivation.
- Security level desired for the system
 - Server or client

Time – vulnerability discovery model

- Each vulnerability is recorded.
 - Available [NVD, vender etc].
 - Needs compilation and filtering.
- Data show three phases for an OS.
- <u>Alhazmi-Malaiya Logistic model</u> (AML)
 - Assumptions:
 - The discovery is driven by the rewards factor.
 - Influenced by the change of market share.



Time-vulnerability Discovery model

- 3 phase model S-shaped model.
- Phase 1:
 - Installed base –low.
- Phase 2:
 - Installed base—higher and growing/stable.
- Phase 3:
 - Installed base-dropping.

$$\frac{dy}{dt} = Ay(B - y)$$
$$y = \frac{B}{dt}$$



Time-based model: Windows 98



Time-based model: Windows NT 4.0



Usage --vulnerability Discovery model

- The data:
 - The global internet population.
 - The market share of the system during a period of time.
- Equivalent effort
 - The real environment performs an intensive testing.
 - Malicious activities is relevant to overall activities.

• Defined as
$$E = \sum_{i=0}^{n} (U_i \times P_i)$$





O. H. Alhazmi and Y. K. Malaiya, "Quantitative Vulnerability Assessment of Systems Software," Proc. Ann. IEEE Reliability and Maintainability Symp., 2005, pp. 616-621

Usage –vulnerability Discovery model

The model:

$$y=B(1-e^{-E\lambda_{vu}})$$

- Exponential growth with effort.
- The basic reliability model [Musa].
- Time is eliminated.



Effort-based model: Windows 98



Effort-based model: Windows NT 4.0



	Win NT 4.0
В	108
λ _{vu}	0.003061
X ²	15.05
X ² critial	42.5569
P-value	0.985

Discussion

- Excellent fit for Windows 98 and NT 4.0.
- Model fits data for all OSs examined.



- Deviation from the model caused by overlap:
 - Windows 98 and Windows XP
 - Windows NT 4.0 and Windows 2000
- Vulnerabilities in shared code may be detected in the newer OS.
- Need: approach for handling such overlap

Vulnerability density and defect

density

Defect density

Valuable metric for planning test effort

- Used for setting release quality target
- Some data is available
- Vulnerabilities are a class of defects
 - Vulnerability data is in the public domain.
 - Is vulnerability density a useful measure?
 - Is it related to defect density?
 - Vulnerabilities = 5% of defects [Longstaff]?
 - Vulnerabilities = 1% of defects [Anderson]?

Can be a major step in measuring security.

Vulnerability density and defect density

- Vulnerability densities: 95/98: 0.003-0.004 NT/2000/XP: 0.01-0.02
- □ **V_{KD}/D_{KD}**: 0.68-1.62% about 1%

System	MSLOC	Known Defects (1000s)	D_{KD} (/Kloc)	Known Vulner - abilies	V _{KD} (/Kloc)	Ratio V _{KD} /D _{KD}
Win 95	15	5	0.33	46	0.0031	0.92%
NT 4.0	16	10	0.625	162	0.0101	1.62%
Win 98	18	10	0.556	84	0.0047	0.84%
Win2000	35	63	1.8	508	0.0145	0.81%
Win XP	40	106.5*	2.66*	728	0.0182	0.68%*

Vulnerability Discovery in Multi-Version Software Systems

- Motivation
- Software Evolution
- Multi-version Software Discovery Model
 Apache, Mysql and Win XP data

Software Evolution

- The modification of software during maintenance or development:
 - □ fixes and feature additions.
 - Influenced by competition
- Code decay and code addition introduce new vulnerabilities
- Successive version of a software can share a significant fraction of code.

Code Sharing & Vulnerabilities

Observation

- Vulnerability increases after saturation in AML modeling
- Accounting for Superposition Effect
 Shared components between several versions of software



Multi-version Vulnerability Discovery Model



 $\Omega(t) = \frac{1}{BCe^{-ABt} + 1}$

B'

 $+ \alpha \frac{1}{B'C'e^{-A'B'(t-\varepsilon)}} + 1$

	Previous Version	Next Version	Shared Code Ratio α
Apache	1.3.24 (3-21- 2002)	2.0.35 (4-6- 2002)	20.16%
Mysql	4.1.1 (12-1- 2003)	5.0.0 (12-22- 2003)	83.52%

One vs Two Humps



Superposition affect

Examining Seasonality

- Is the seasonal pattern statistically significant?
- Periodicity of the pattern
- Analysis:
 - Seasonal index analysis with χ^2 test
 - Autocorrelation Function analysis
- Significance
 - Enhance VDMs' predicting ability

Prevalence in Month

Vulnerabilities Disclosed

	WinNT	IIS	IE
	'95~'07	'96~'07	'97~'07
Jan	42	15	15
Feb	20	10	32
Mar	12	2	22
Apr	13	11	29
May	18	12	41
Jun	24	17	45
Jul	18	11	53
Aug	17	7	42
Sep	11	6	26
Oct	14	6	20
Nov	18	7	26
Dec	51	28	93
Total	258	132	444
Mean	21.5	11	37
s.d.	12.37	6.78	20.94



Seasonal Index

Seasonal Index Values						
	WinNT	IIS	IE			
Jan	1.95	1.36	0.41			
Feb	0.93	0.91	0.86			
Mar	0.56	0.81	0.59			
Apr	0.60	1.00	0.78			
May	0.84	1.09	1.11			
Jun	1.12	1.55	1.22			
Jul	0.84	1.00	1.43			
Aug	0.79	0.64	1.14			
Sep	0.51	0.55	0.70			
Oct	0.65	0.55	0.54			
Nov	0.84	0.64	0.70			
Dec	2.37	2.55	2.51			
χ^2_c	19.68	19.68	19.68			
χ_s^2	78.37	46	130.43			
p-value	3.04e-12	3.23e-6	1.42e-6			

Seasonal index: measures how much the average for a particular period tends to be above (or below) the expected value

H₀: no seasonality is present. We will evaluate it using the monthly seasonal index values given by [4]:

 $s_i = \frac{d_i}{d}$

where, s_i is the seasonal index for i^{th} month, d_i is the mean value of i^{th} month, d is a grand average

Autocorrelation function (ACF)

- Plot of autocorrelations function values
- With time series values of z_b, z_{b+1}, ..., z_n, the ACF at lag k, denoted by r_k, is [5]:

$$r_{k} = \frac{\sum_{t=b}^{n-k} (z_{t} - \bar{z})(z_{t+k} - \bar{z})}{\sum_{t=b}^{n} (z_{t} - \bar{z})^{2}}, \text{ where } \bar{z} = \frac{\sum_{t=b}^{n} z_{t}}{(n-b+1)}$$

- Measures the linear relationship between time series observations separated by a lag of time units
- Hence, when an ACF value is located outside of confidence intervals at a lag t, it can be thought that every lag t, there is a relationships along with the time line

Autocorrelation (ACF):Results



- Expected lags corresponding to 6 months or its multiple would have their ACF values outside confidence interval
- Upper/lower dotted lines: 95% confidence intervals.
- An event occurring at time t + k (k > 0) lags behind an event occurring at time t.
- Lags are in month.

Halloween Indicator

- "Also known as "Sell in May and go away"
- Global (1973-1996):
 - Nov.-April: 12.47% ann., st dev 12.58%
 - 12-months:10.92%, st. dev.
 17.76%
- 36 of 37 developing/developed nations
- Data going back to 1694
- "No convincing explanation"



Jacobsen, Ben and Bouman, Sven, The Halloween Indicator, 'Sell in May and Go Away': Another Puzzle(July 2001). Available at SSRN: http://ssrn.com/abstract=76248

CVSS: Common Vulnerability Scoring System

How important is a specific vulnerability?

- Essentially a risk measure
- Vulnerabilities with highest scores need addressing quickly. Those with lowest scores are low priority.
- CVSS v1: National Infrastructure Advisory Council (NIAC), 2005

CVSS v2: Forum of Incident Response and Security Teams (FIRST)

- **2007**
- Still common
- CVSS V3: 2015
 - Getting common

CVSS: Common Vulnerability Scoring System

Score formulas are based on metrics.

- Metrics use table look-ups.
- Base Score uses metrics intrinsic to a vulnerability. Each official vulnerability (with a cve number) has a base score.
 - BaseScore = f(impact, exploitability)
 - Formulas designed to yield a value between 0 (lowest)-10 (highest). There is no formal derivation or justification for the formula.
 - Score used for prioritizing effort.

CVSS Scores

- BaseScore uses metrics intrinsic to a vulnerability. Each official vulnerability (with a cve number) has a base score.
 - Mandatory.
 - Impact based on values of Confidentiality, Integrity, and Availability (CIA) impact values.
- TemporalScore = f(BaseScore, Exploit, Remediation). Varies with time.
- EnvironmentalScore = f(metrics modified by required CIA levels for an application). Depends on the user environment.

CVSS v2.0 Base Score

Formula

BaseScore = round_to_1_decimal(((0.6*Impact)+(0.4*Exploitability)-1.5)*f(Impact))

- □ f(impact)= 0 if Impact=0, 1.176 otherwise
- BaseScore ranges between 10-0
- □ How did they come up with this?
- No derivation, no validation, based on consensus in the committee based on member's expert opinions
- Exploitability sub-score measure of Likelihood of exploitation of the vulnerability.
 - Range 0-10
- Impact sub-score a measure of Impact.
 - Range 0-10

CVSS Base metric: Observation

- CVSS Base Score is a form of a risk measure.
- They could have computed CVSS Base Score by simply multiplying the Exploitability and the Impact sub-scores.
- It would result in a similar distribution of score with somewhat better resolution.
- CVSS Base Score for prioritizing vulnerabilities.
- V2 Base score
 - □ 7.0-10.0 High (V3: 7.0-8.9 High, 9.0-10 Critical)
 - □ 4.0-6.9 **Medium**
 - □ 0-3.9 Low (V3: 0.0 None, 0.1-3.9 Low)

CVSS 2.0 Exploitability Subscore

Exploitability = 20* AccessVector*AccessComplexity*Authentication

AccessVector:

- □ requires local access: 0.395
- adjacent network accessible: 0.646
- network accessible: 1.0

AccessComplexity:

- □ high: 0.35
- medium: 0.61
- Iow: 0.71

Authentication

- multiple instances of authentication: 0.45
- □ requires single instance of authentication: 0.56
- □ requires no authentication: 0.704

CVSS 2.0 Impact (C.I.A.) Subscore

Impact = 10.41*(1-(1-ConfImpact)*(1-IntegImpact)*(1-AvaiIImpact))

- Conflmpact
 - none: 0.0
 - **partial: 0.275**
 - □ complete: 0.660
- IntegImpact
 - none: 0.0
 - **partial:** 0.275
 - □ complete: 0.660
- AvailImpact
 - none: 0.0
 - partial: 0.275
 - complete: 0.660
- Weighted by required levels for specific environments for Environmental Score.

CVSS 2.0 other scores (not really used)

TemporalScore = round_to_1_decimal(BaseScore*Exploitability *RemediationLevel*ReportConfidence)

- Exploitability: Proven (1.0) to unproven (0.85)
- RemediationLevel: Official fix (0.85) to no fix (1.0)
- ReportConfidence: Confirmed (1.0) to unconfirmed (0.95)

EnvironmentalScore = round_to_1_decimal((AdjustedTemporal+ (10-AdjustedTemporal)*CollateralDamagePotential)*TargetDistribution)

Has CVSS worked?

Windows 7 Correlation among

- CVSS Exploitability
- Microsoft Exploitability metric
- Presence of actual exploits
- No significant correlation found.

Variables	Exploit Existence	MS-EXP	CVSS-EXP
Exploit			
Existence	1	-0.078	-0.146
MS-EXP	-0.078	1	-0.116
CVSS-EXP	-0.146	-0.116	1

A. Younis and Y.K. Malaiya, "Comparing and Evaluating CVSS Base Metrics and Microsoft Rating System", The 2015 IEEE Int. Conf. on Software Quality, Reliability and Security, pp. 252-261

Characterizing Vulnerability with Exploits

- 1 to 5 % of defects are vulnerabilities.
- Finding vulnerabilities can take considerable expertise and effort.
- Out of 49599 vulnerabilities reported by NVD,
 2.10% have an exploit.
- A vulnerability with an exploit written for it presents more risk.



• What characterizes a vulnerability having an exploit? Small sloc

Vulnerability	In- Degree	Out- Degree	CountPath	ND	СҮС	Fan-In	No of Invocation	SLOC	Exploit Existence
CVE-2009-1891	1	9	9000	6	68	45	2	211	NEE
CVE-2010-0010	4	9	145	4	11	16	4	38	EE
CVE-2013-1896	26	5	8	1	5	37	3	29	EE

Awad Youngish, Yashwant K. Malaiya, Charles Anderson, and Indrajit Ray. "**To Fear or Not to Fear That is the Question: Code Characteristics of a Vulnerable Function with an Existing Exploit**". 51 Proceedings of the Sixth ACM on Conference on Data and Application Security and Privacy (CODASPY), 2016, pp. 97-104.

Vulnerability Reward Programs (VPR)

- VRPs decreases the probability of an attacker acquiring a vulnerability and that reduces the likelihood of vulnerabilities discovery and exploitation.
- Vulnerabilities with a high CVSS scores and have no exploits or attacks may been explained by the impact of VRPs on vulnerabilities exploitation.

• We found significant correlation.

Spearman Correlation between CVSS Base score and VRPs Rating System						
	Correlation	CVSS Scores before clustering	CVSS Scores after clustering			
Firefox	Value	0.65	0.47			
	P-value	< 0.0001	< 0.0001			
Chrome	Value	0.53	0.59			
Chrome	P-value	< 0.0001	< 0.0001			

Awad Youngish, Yashwant K. Malaiya, and Indrajit Ray. "Evaluating CVSS Base Score Using Vulnerability Rewards Programs". The proceedings of the 31st International Conference on Systems Security and Privacy Protection (IFIP SEC 2016).

Vulnerability flow through markets



Types of Vulnerability Markets



Security Breach Cost Metrics

Total Cost of a Breach =

Incident investigation cost

- + Customer Notification/crisis management cost
- + Regulatory and industry sanctions cost
- + Class action lawsuit cost

 $\textit{Cost per Record} = \frac{\textit{Total cost of breach}}{\textit{number of affected records}}$



Significant Factors impacting Cost and Probability

Classification	Significant Factors	Source
Total number of affected records	Total number of affected records?	All
Type of data breaches	What is your organization's industry classification?	Symantec & IBM
	What types of information do your employees handle?	Symantec & IBM
Incident investigation cost	Data is in a centralized system/location?	Hub Int'l
	Actual fraud is expected already?	Hub Int'l
	Federal class action lawsuit filed?	Hub Int'l
	What do you think is the most likely cause of a data breach?	Symantec & IBM
	Is sensitive data encrypted on all laptops or removable storage?	Symantec & IBM
	How long does the business keep/retain sensitive information pertaining to employees,	IDT911
	customers, and patients?	
	What best describes your organization's privacy and data protection program?	Symantec & IBM
Crisis management cost	Number of Years for credit monitoring?	Hub Int'l
	What is the global headcount of your organization?	Symantec & IBM
	Is your organization's business continuity management team involved in the data breach	IBM
	incident response process?	
Regulatory and sanction cost	Is PCI compliance an issue?	Hub Int'l
Lawsuit cost	Actual fraud is expected already?	Hub Int'l
	Federal class action lawsuit filed?	Hub Int'l

A consolidated approach for estimation of data security breach costs, AM Algarni, YK Malaiya 2016 2nd International Conference on Information Management (ICIM), 26-39



Years	Gross Expenses	Insurance receivable	Net Expenses (before tax deductions)	Net Expenses (after tax deductions)	
2013	\$61m	\$44m	\$17m	\$11m	
2014	\$191m	\$46m	\$145 m	\$94m	
2015	N/A	N/A	\$39	\$28	
Total	\$252m	\$90m	\$201m	\$133m	
Raw cost per card= \$6.30 (40 million cards affected)					

A consolidated approach for estimation of data security breach costs, AM Algarni, YK Malaiya 2016 2nd International Conference on Information Management (ICIM), 26-39



The breach cost vs. breach size



Verizon 2015 data, the claim amount vs. breach size (ranges from single digits to 108 million records)



Overall risk evaluation model



Details in Abdullah Algarni's dissertation: Quantitative economics of security: software vulnerabilities and data breaches, CSU



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